



Soft and Hard X-ray Microscopy

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**Advanced Photon Source,
Argonne National Laboratory**

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SPring-8

Outline

1. Fundamentals

resolution

contrast

sources

optics

2. Direct methods

projection imaging

full-field imaging

scanning

3. Indirect methods

microdiffraction

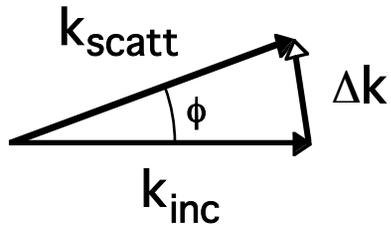
coherent diffraction

holography

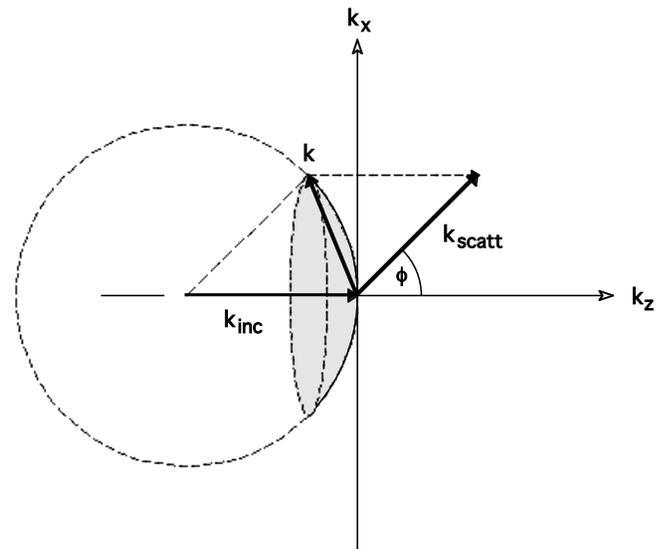
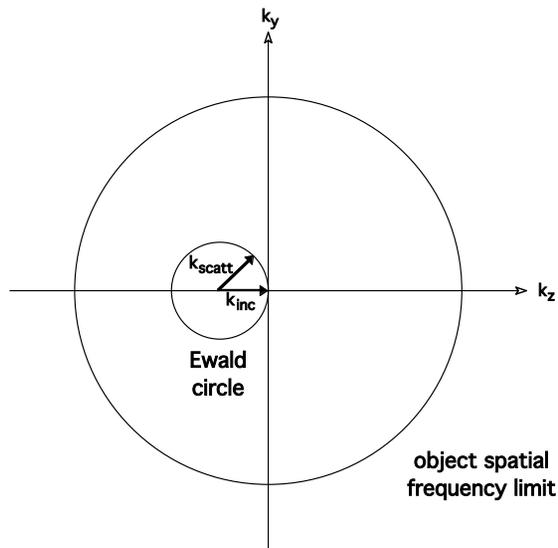
References:

1. M. Howells, "Soft-x-ray microscopes," *Physics Today* 38, 22 (Aug. 1985).
2. J. Kirz, "Soft X-ray microscopes and their biological applications," *Q. Rev. Biophys.* 28, 1 (1995).
3. J. Als-Nielsen and D. McMorrow, *Elements of Modern X-ray Physics* (Wiley, New York, 2000).
4. D. Attwood, *Soft X-Rays and Extreme Ultraviolet Radiation: Principles and Applications* (Cambridge, 2007).

Image formation as a scattering process



Incident waves with initial momentum k_{inc} are elastically scattered into new direction k_{scatt} with momentum transfer Δk .



Ewald sphere is defined by conservation of momentum. Only spatial frequencies on the Ewald sphere are accessible to the imaging process, limiting attainable resolution.

Diffraction limits to resolution

Point-spread function

$$P(x,y) = \frac{\sin x}{x} \frac{\sin y}{y}$$

with $x = \frac{kax}{z}$, $y = \frac{kay}{z}$

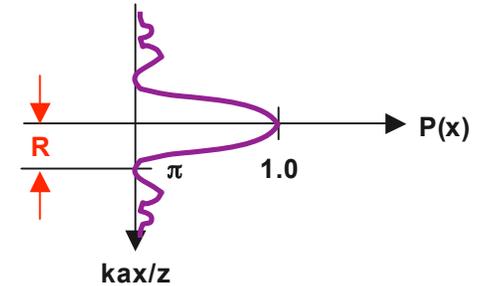
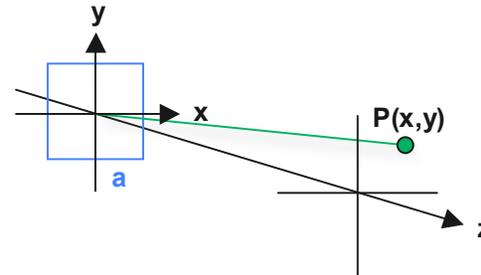
Transverse

$$R = 0.5 \frac{\lambda}{NA}$$

where

$$NA \sim \frac{a}{z}$$

$$k = \frac{2\pi}{\lambda}$$



Bragg's law

$$\Delta \vec{k} = \vec{k}_{inc} - \vec{k}_{scatt} \quad (0 \leq \Delta k \leq 2k_{inc})$$

$$k_x^2 + k_y^2 + (k_z + k_{inc})^2 = k_{inc}^2$$

For extreme-angle ray (xz plane, $k_y = 0$) with

$$k_x = \frac{2\pi}{2R} = \frac{2\pi}{\lambda} NA$$

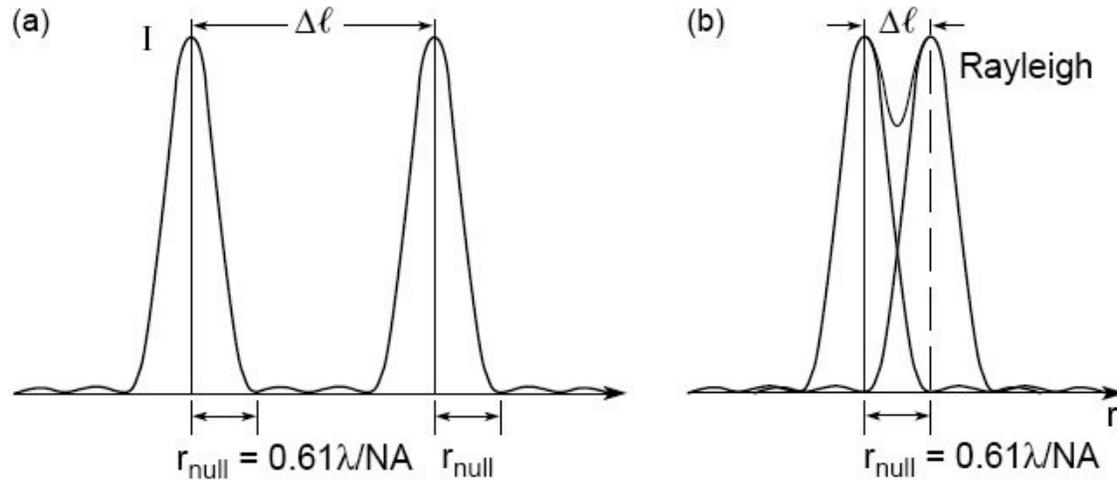
Longitudinal

$$DOF = \frac{\lambda}{(NA)^2}$$

and

$$k_z = \frac{k_x^2}{2k_{inc}} \quad (k_z \ll k_{inc})$$

What do we mean by "resolution"?



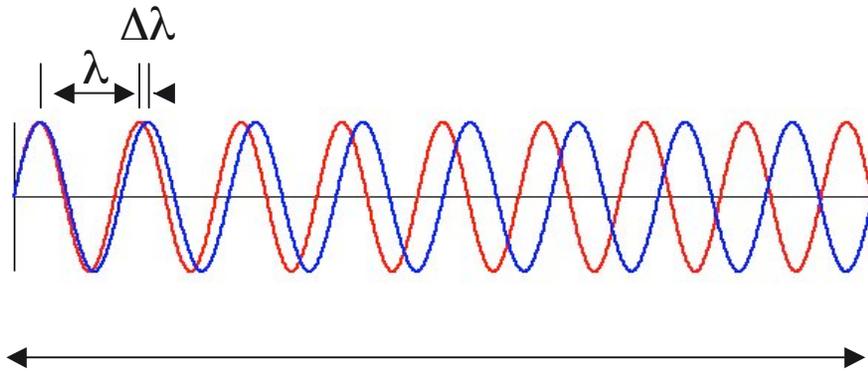
- Point sources are spatially coherent
- Mutually incoherent
- Intensities add
- Rayleigh criterion (26.5% dip)

Conclusion: With spatially coherent illumination, objects are “just resolvable” when

$$\text{Res}|_{\text{coh}} = \frac{0.61 \lambda}{\text{NA}} = 1.22 \Delta r$$

Coherence

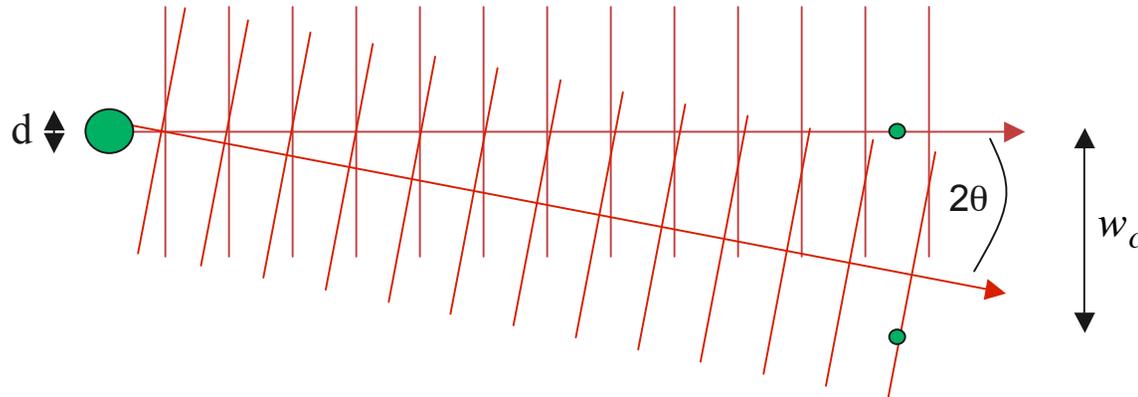
longitudinal coherence



$$l_c \sim \frac{\lambda^2}{\Delta\lambda}$$

$$\tau_c \sim \frac{\lambda^2}{c\Delta\lambda}$$

transverse coherence

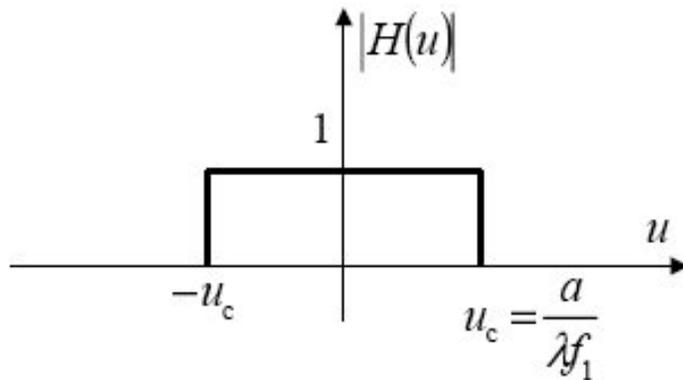


$$w_c \sim \frac{\lambda z}{d}$$

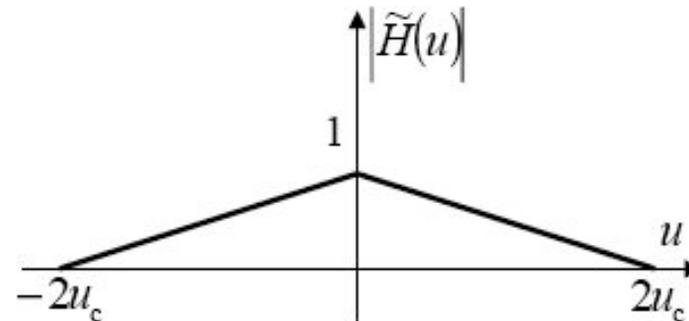
$$d \cdot \theta = \lambda / 2\pi$$

$$\Delta x \Delta p \geq \hbar / 2$$

Coherent vs. incoherent



Coherent illumination



Incoherent illumination

Scanning and full-field microscopy are *incoherent* methods

- Transfer function is linear in the field *intensities*
- Characterized by sloping function down to 2NA

Diffraction and holographic microscopy are *coherent* methods

- Transfer function is linear in the field *amplitudes*
- Characterized by flat top, sharp cutoff at limiting NA

Why use x-rays?

- Penetration through whole cells and thick materials with minimal multiple scattering: “clean” images and spectra
- Short wavelengths, so high spatial resolution is possible
- Short pulses, so high time resolution is possible
- Coupling to core-level electrons: element detection, “clean” measurement of electronic and chemical states
- Coupling to electronic spin via polarization: probe magnetic states and ordering

But: ionizing radiation, so repeated high-resolution imaging of radiation-sensitive samples (e.g. live cells) is not possible.

Contrast mechanisms in x-ray microscopy

- **Access a wealth of information**

- Absorption measure electron density
- Phase measure real part of refractive index
- Fluorescence measure elemental distribution
- Spectroscopy extract chemical state, spin state
- Diffraction reveal structure, strain, mag. charge

- **Natural sample contrast is possible; staining not required**
- **Image structure of thick samples, sectioning not required**
- **More penetrating, less damage, less charging than with electrons**

Refractive index and contrast

$$n = 1 - \delta - i\beta = 1 - \frac{r_e}{2\pi} \lambda^2 \sum_i n_i f_i(0)$$

$$A = A_0 \exp(-inkt)$$

$$k = 2\pi / \lambda$$

- Absorption contrast:

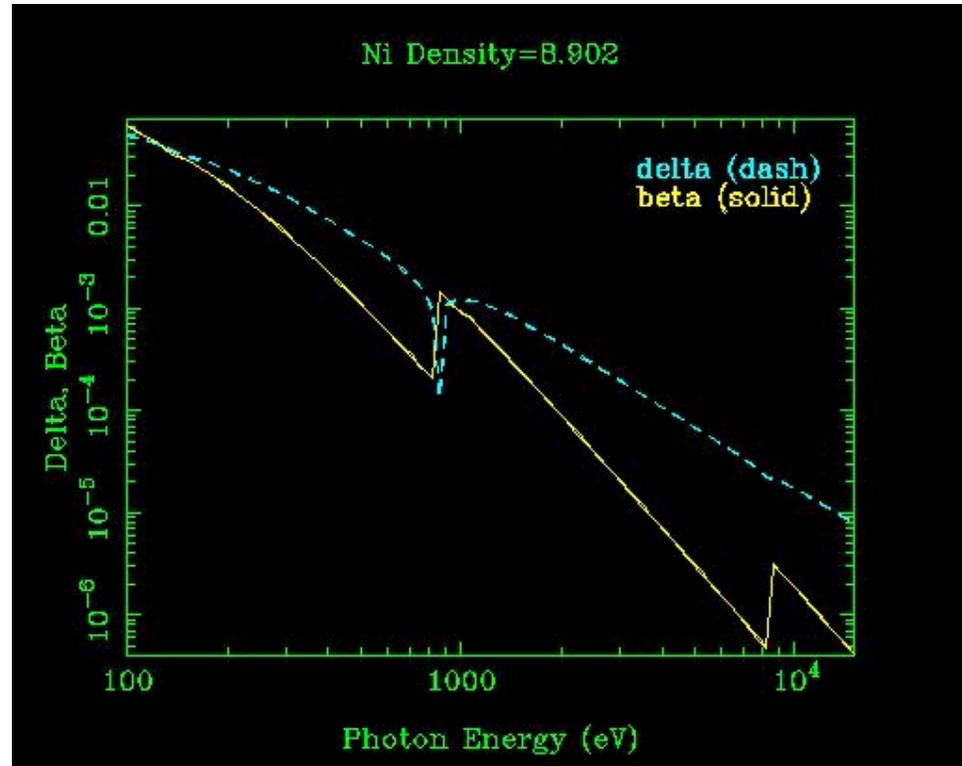
sensitive to $Im(n)$

$$\sim 2\pi\delta(x,y)t/\lambda$$

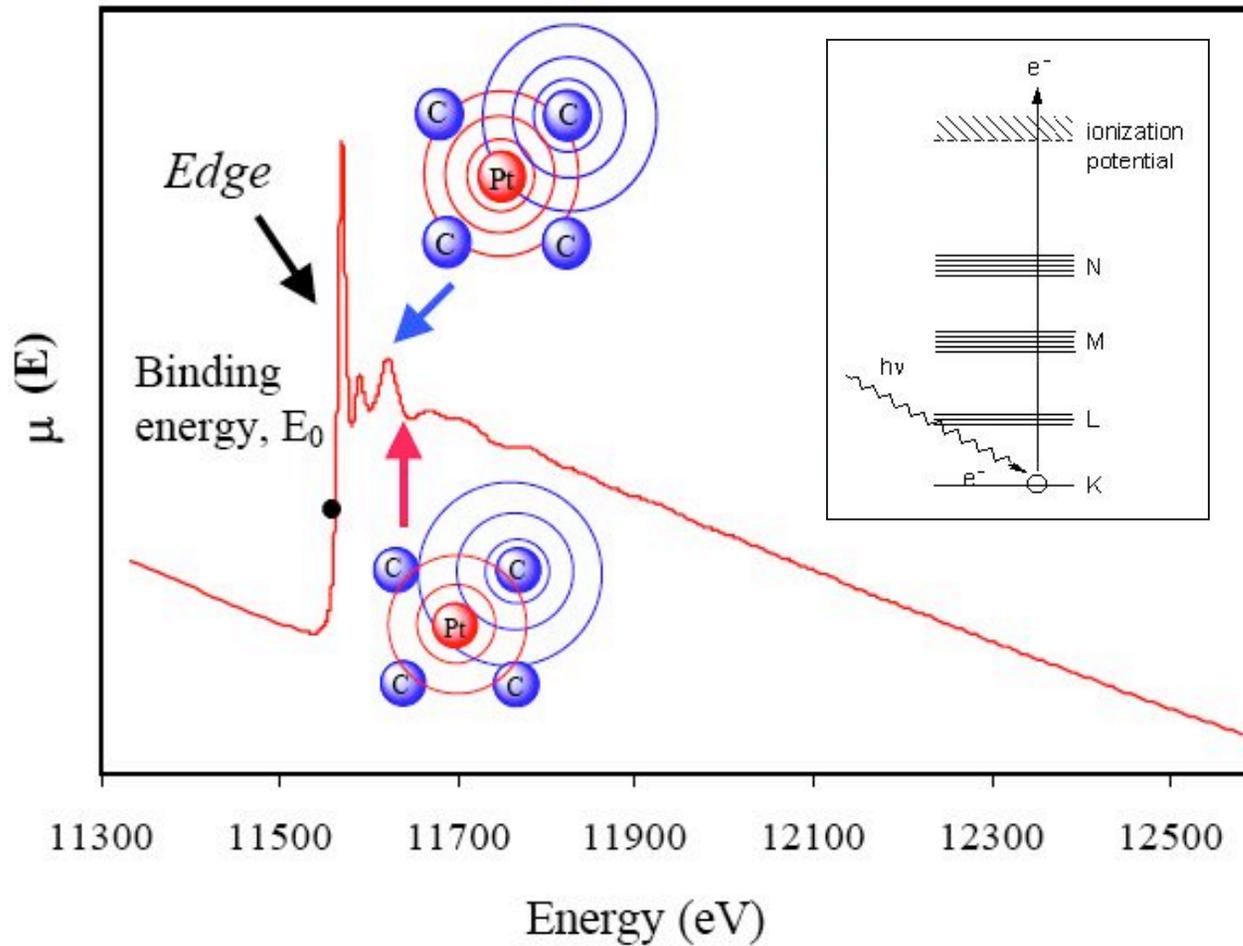
- Phase contrast:

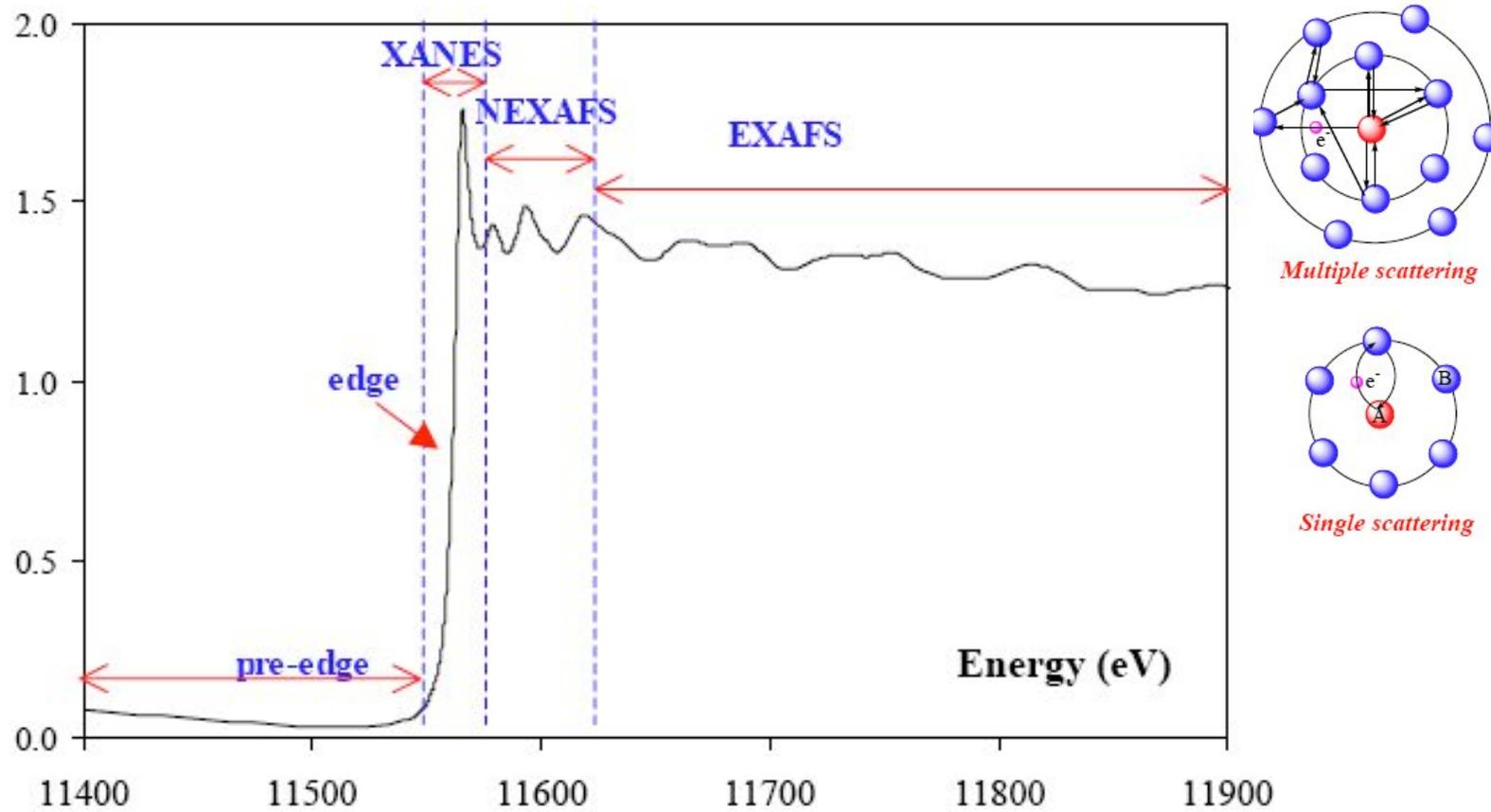
sensitive to $Re(n)$

$$\sim 4\pi\beta(x,y)t/\lambda$$

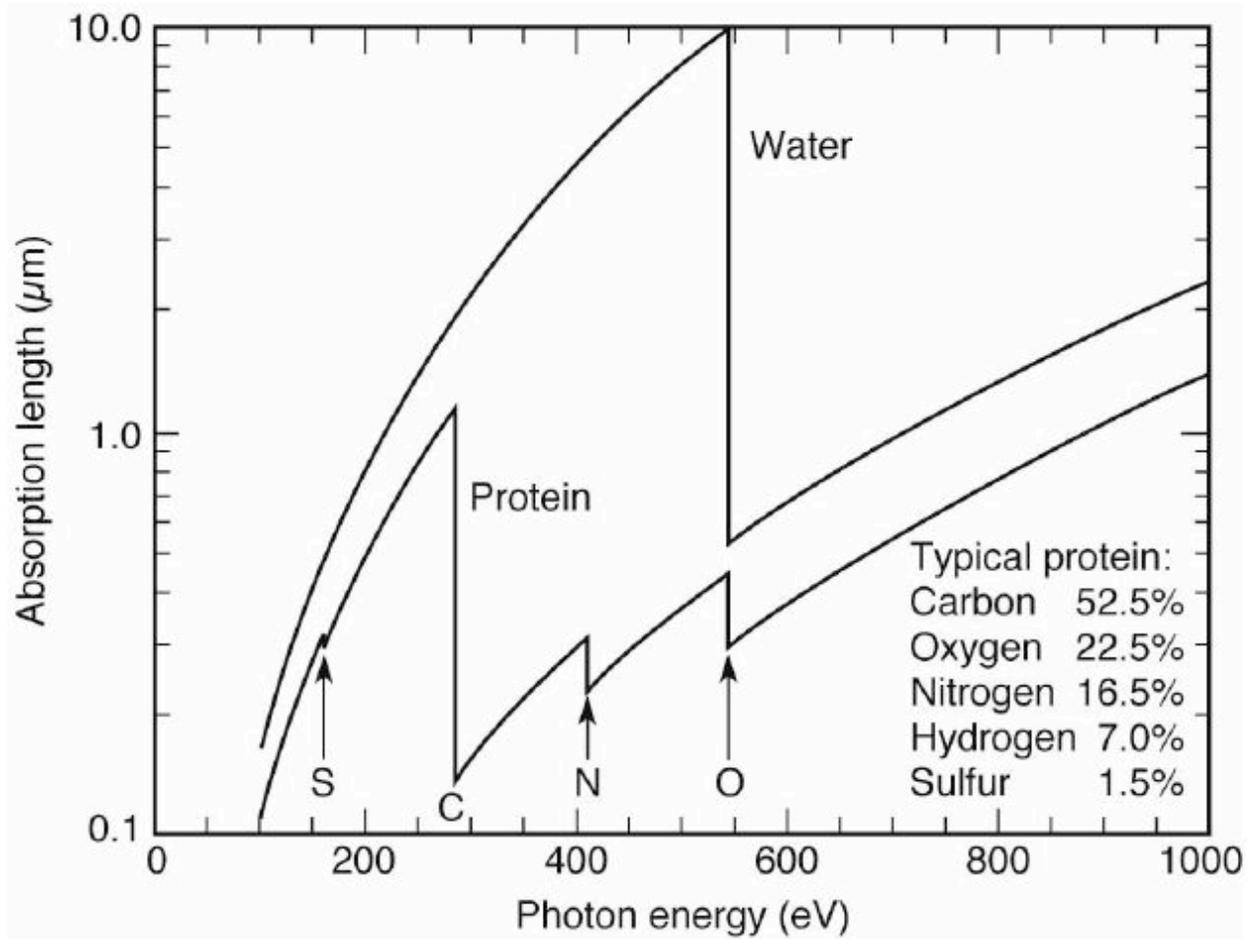


Elemental sensitivity at absorption edges

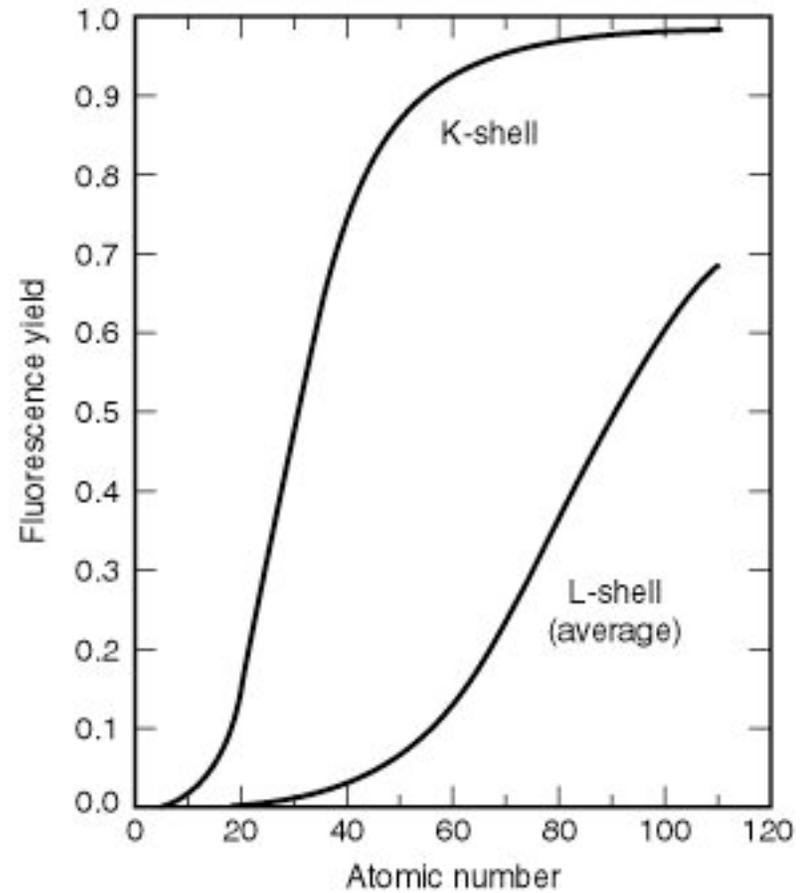
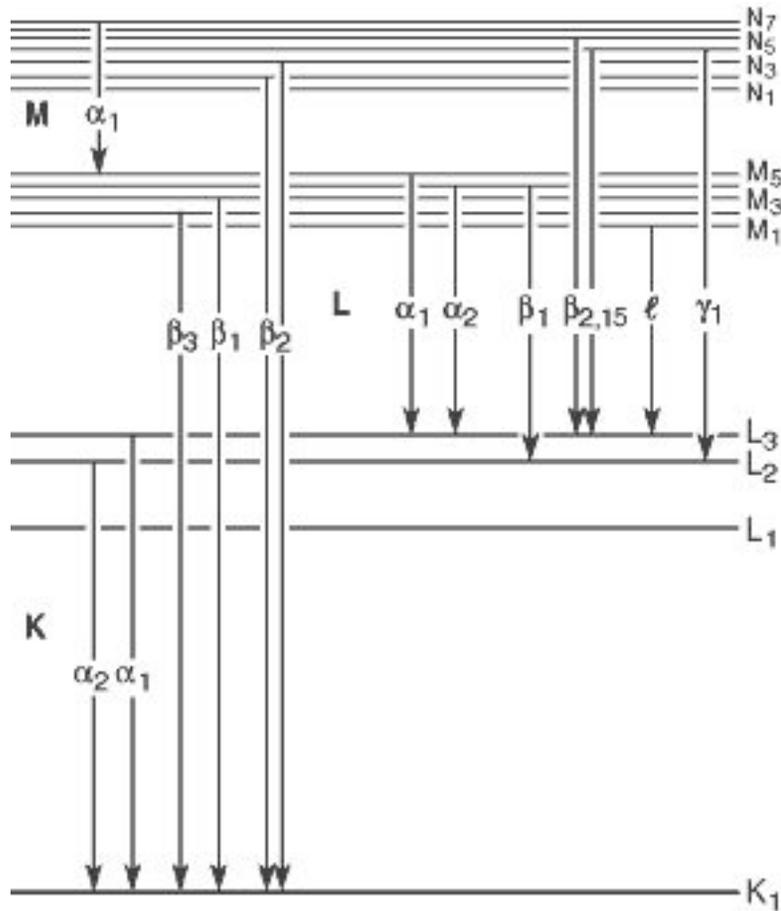




The "water window"



Fluorescence spectroscopy



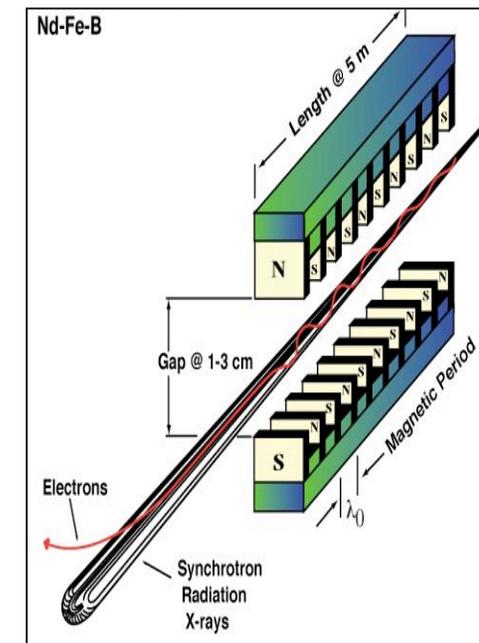
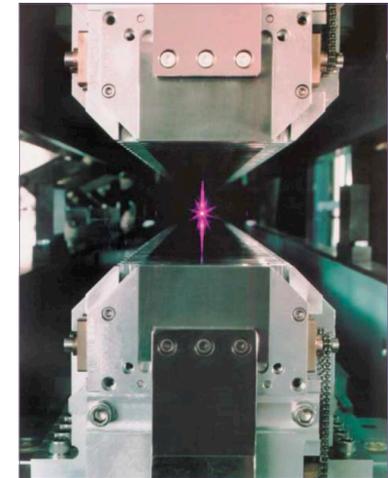
Why use synchrotrons?

Synchrotron sources offer

- Brilliance (small source, collimated)
- Tunability (IR to hard x-rays)
- Polarization (linear, circular)
- Time structure (short pulses)

➤ **Undulators produce the most brilliant x-ray beams available**

$B = \text{photons/source area, divergence, bandwidth}$



Undulator radiation

- SR sources (except FEL) are incoherent, but highly forward directed due to relativistic effects
 $\theta \sim 1/\gamma$
- Spatial and temporal filtering (pinholes, monochromators) is needed to select the coherent flux
 $F_c \sim \lambda^2 B$
- Only the coherent flux can be focused into a diffraction-limited spot or be used to form interference fringes



Focusing optics for x-rays

Achieving high NA is challenging because x-rays interact weakly

$$n = 1 - \delta - i\beta$$

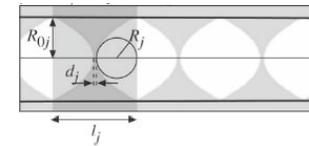
$$\delta, \beta \sim 10^{-3} \text{ to } 10^{-6}$$

⇒

$$|n| \approx 1$$

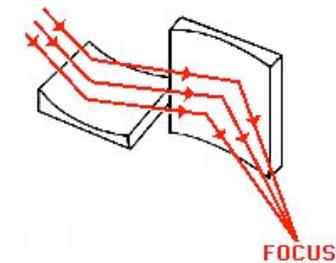
Refractive (compound refractive lenses)
Low efficiency, highly chromatic, aberrations

~ 50 nm



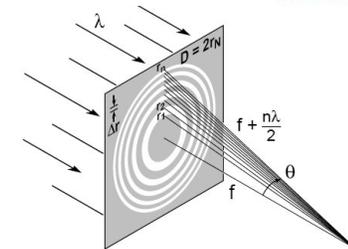
Reflective (Kirkpatrick-Baez mirrors)
High efficiency, achromatic, limited to ~10 nm

~ 40 nm



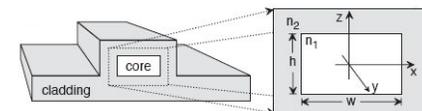
Diffractive (Fresnel zone plates, MLLs)
Moderate efficiency, limited to ~10 nm except MLL

~ 20 nm



Waveguides
Low efficiency, 2D is challenging

~ 20 nm



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VOLUME 180, NUMBER 3

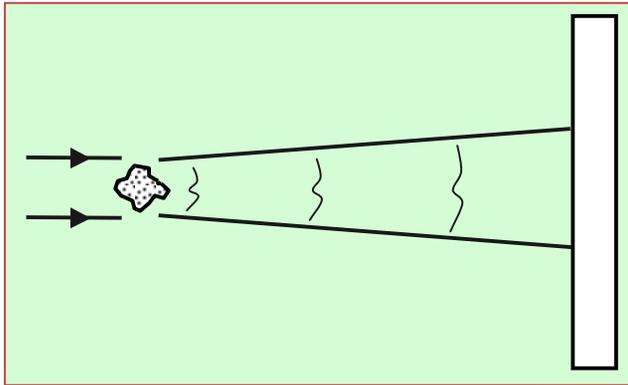
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THE X-RAY MICROSCOPE

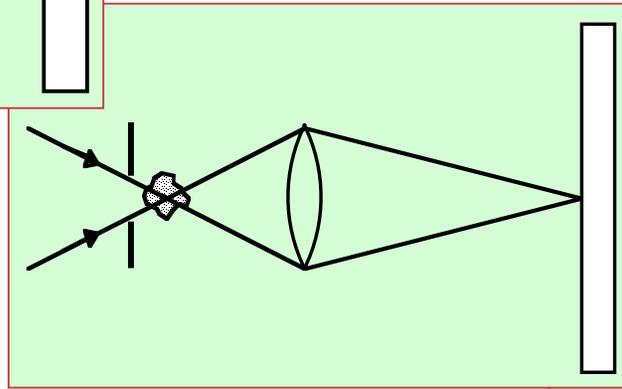
by Paul Kirkpatrick

It would be a **useful complement to** microscopes using light or electrons, for X-rays combine short wavelengths, giving fine resolution, and penetration. The main problems standing in the way have now been solved. **44**

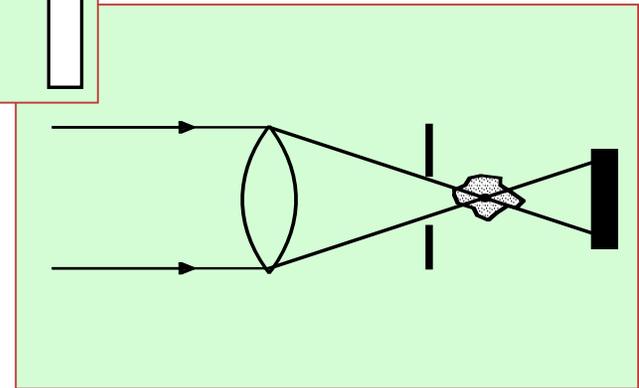
2. Direct methods



Projection

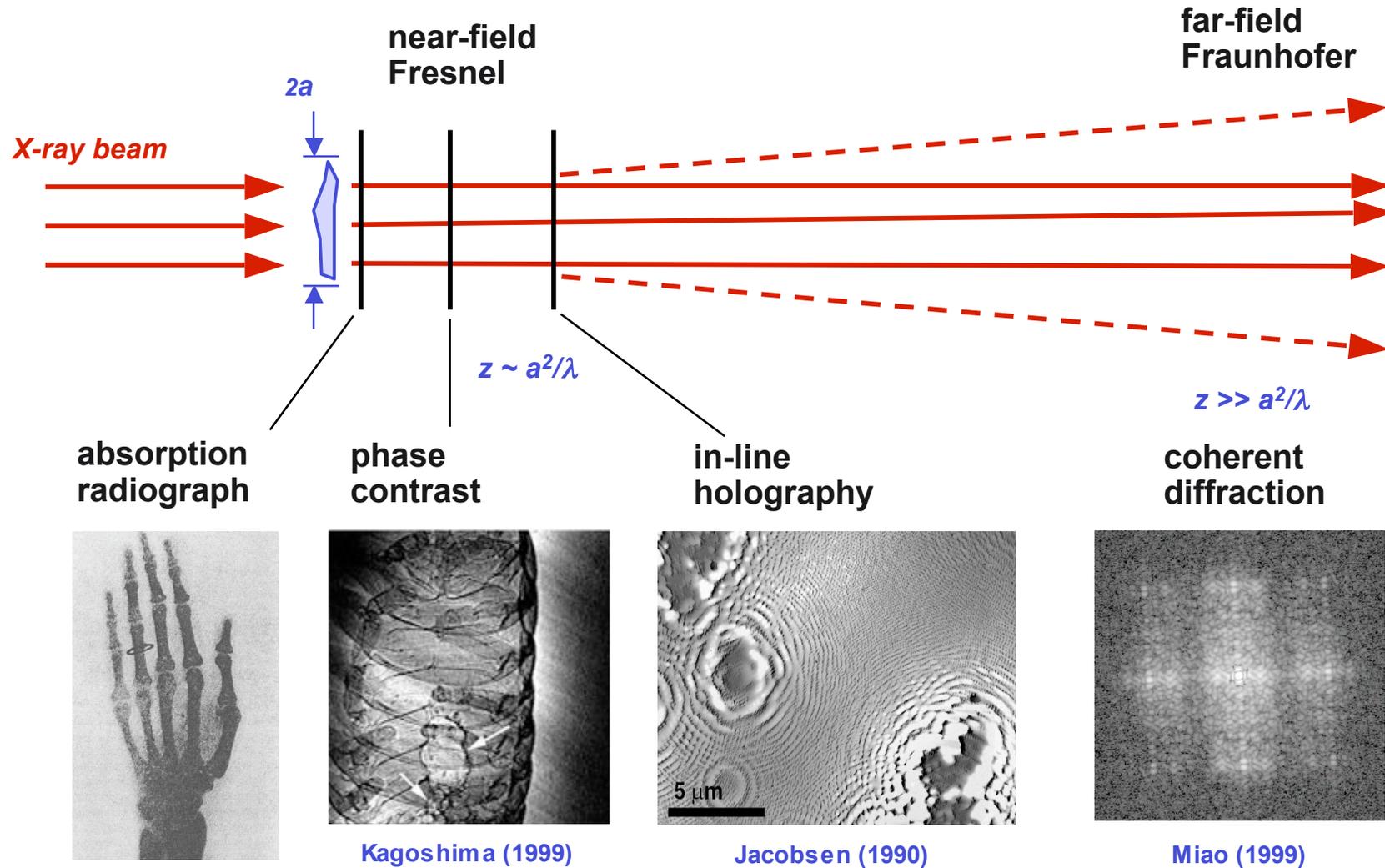


Imaging

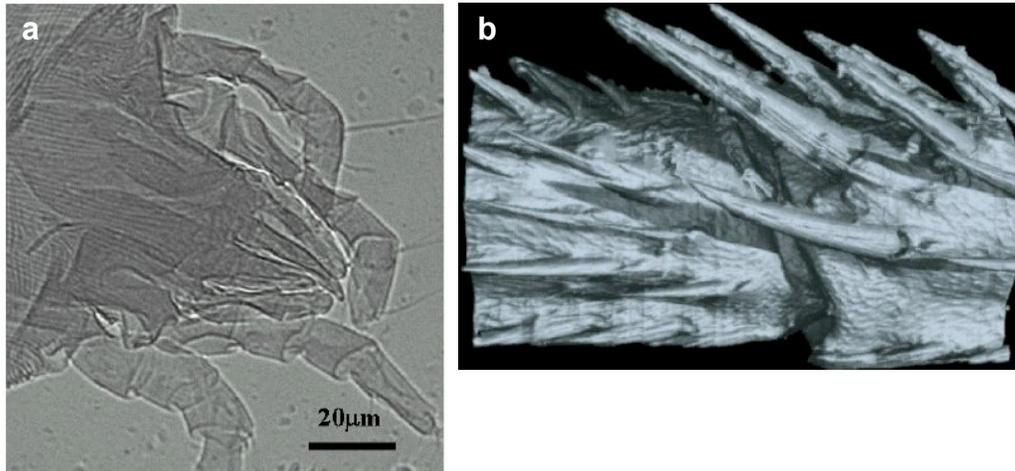


Scanning

Different regimes of x-ray imaging

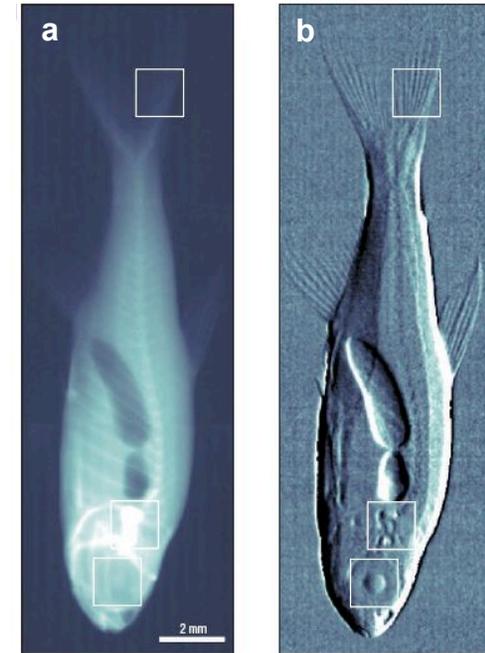


Phase contrast: tool of choice for low-absorption samples



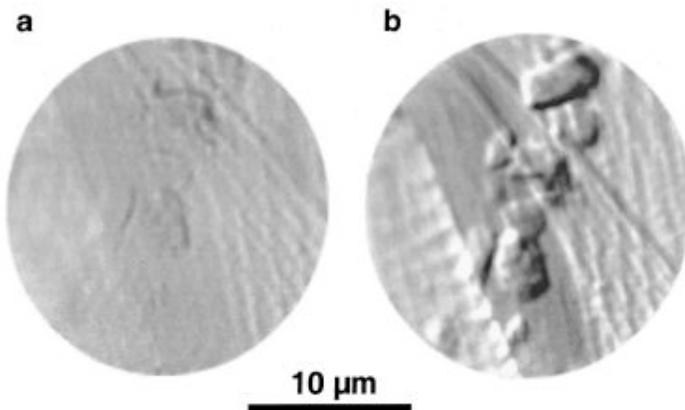
(a) Dust mite and (b) tomographically reconstructed fly leg joint, recorded with ~ 8 keV x-rays and propagation phase contrast.

S. Mayo, Opt. Express 11, 2289 (2003)



Small fish, recorded with three-grating method and a standard x-ray tube (40 kV/25 mA). (a) Transmission. (b) Differential phase contrast.

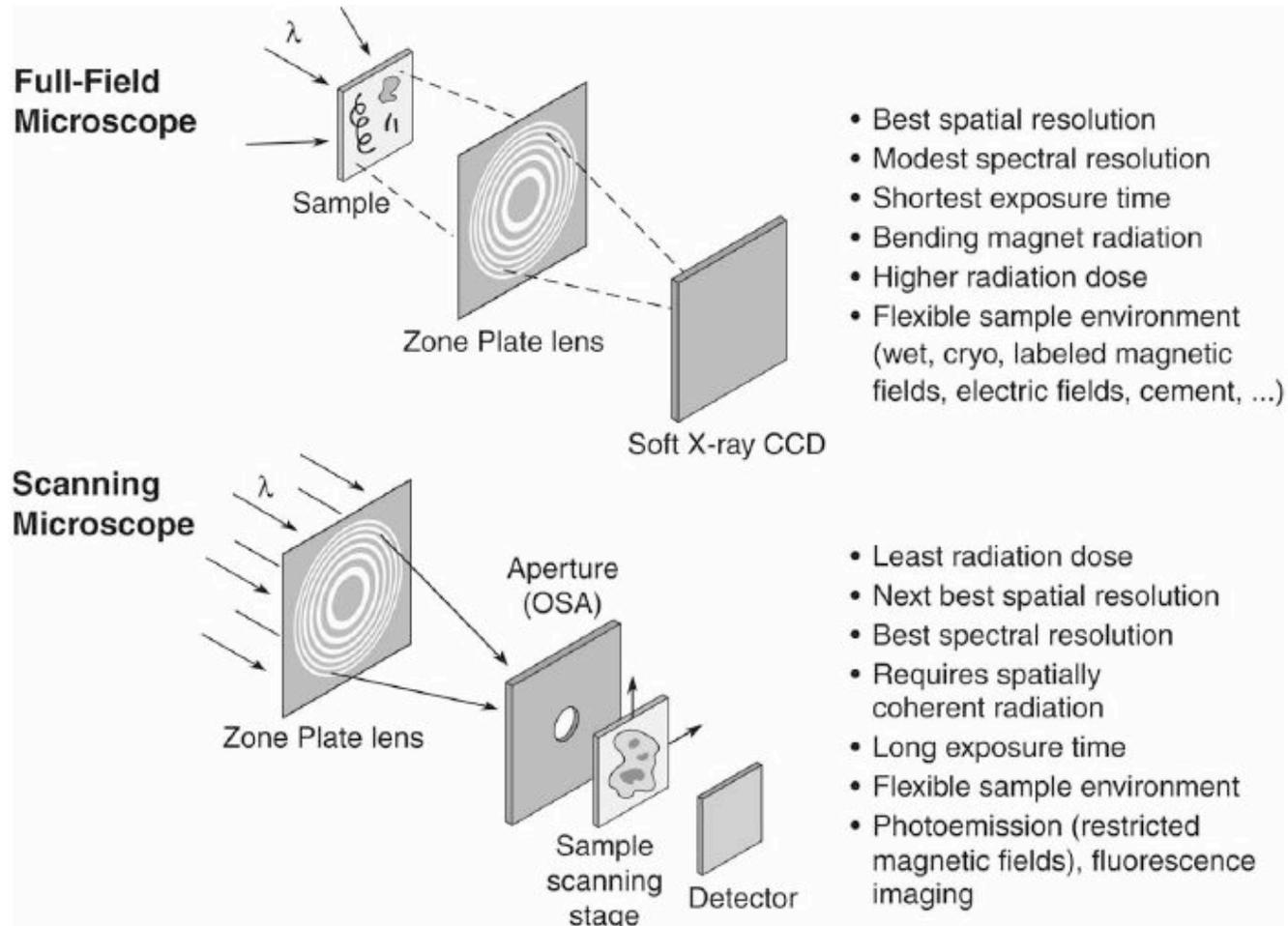
F. Pfeiffer, Nature Phys. 2, 258 (2006)



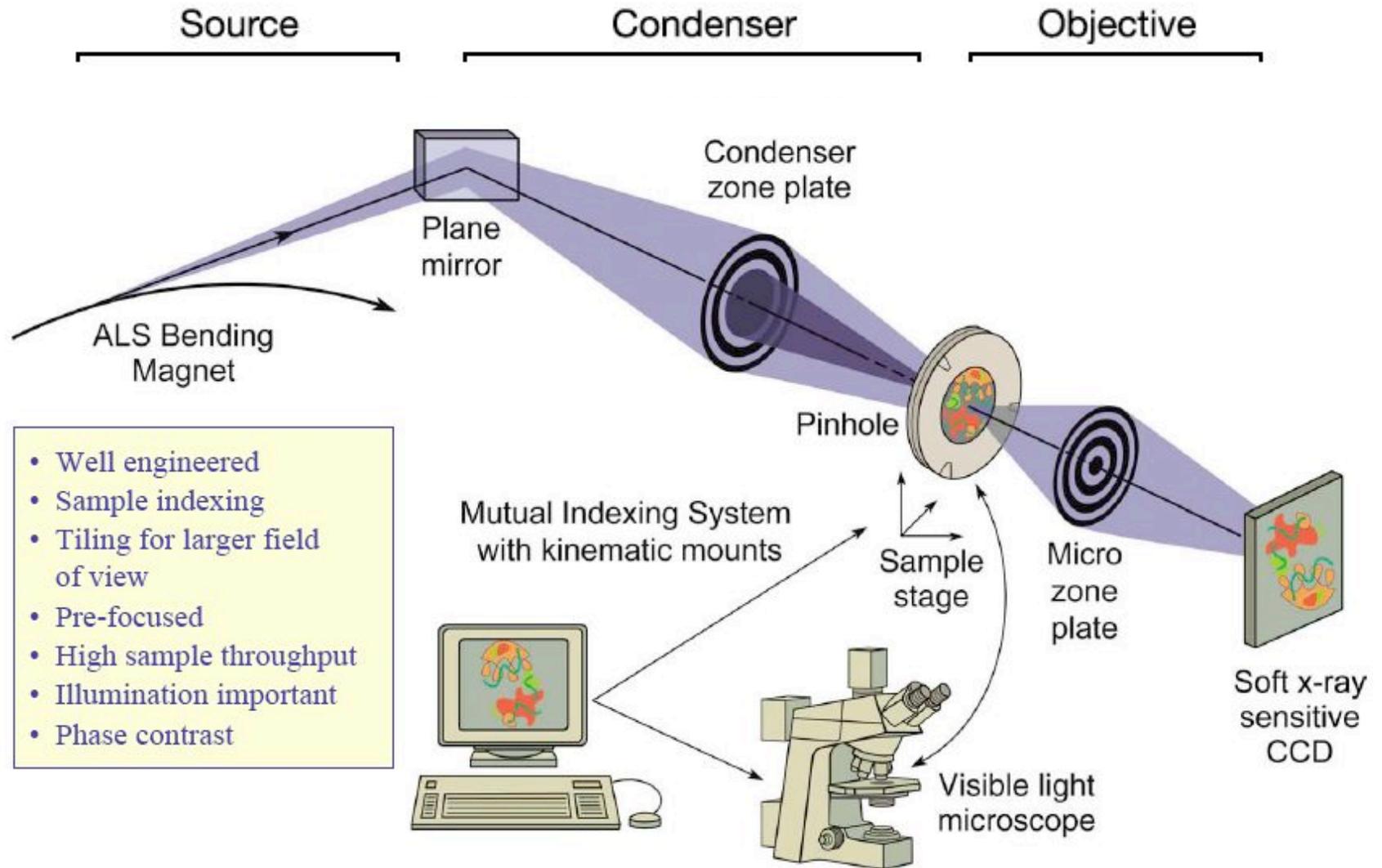
Moth wing, recorded with 4 keV x-rays. (a) Bright-field. (b) Differential interference contrast.

B. Kaulich, T. Wilhein, J. Opt. Soc. Am. A19, 797 (2002)

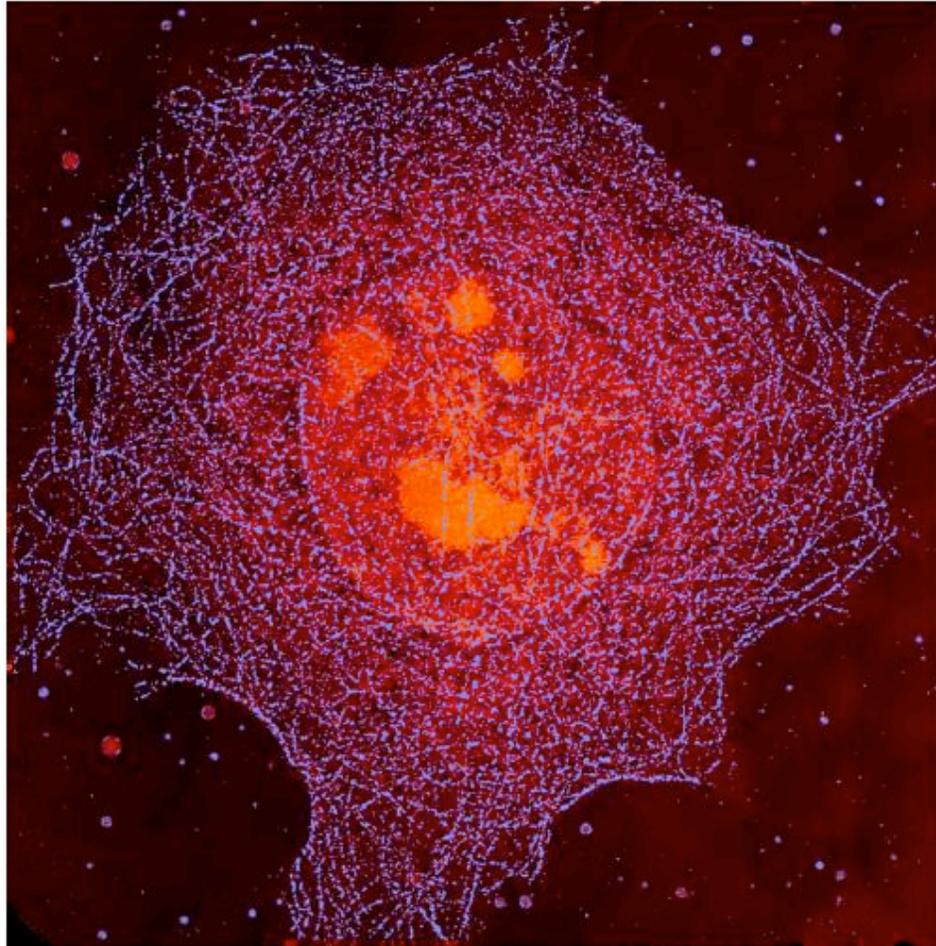
Full-field and scanning x-ray microscopes



XM-1 microscope at the ALS



Wet specimens can be studied by x-ray microscopy



$\hbar\omega = 520 \text{ eV}$

$32 \mu\text{m} \times 32 \mu\text{m}$

Ag enhanced Au labeling
of the microtubule network,
color coded blue.

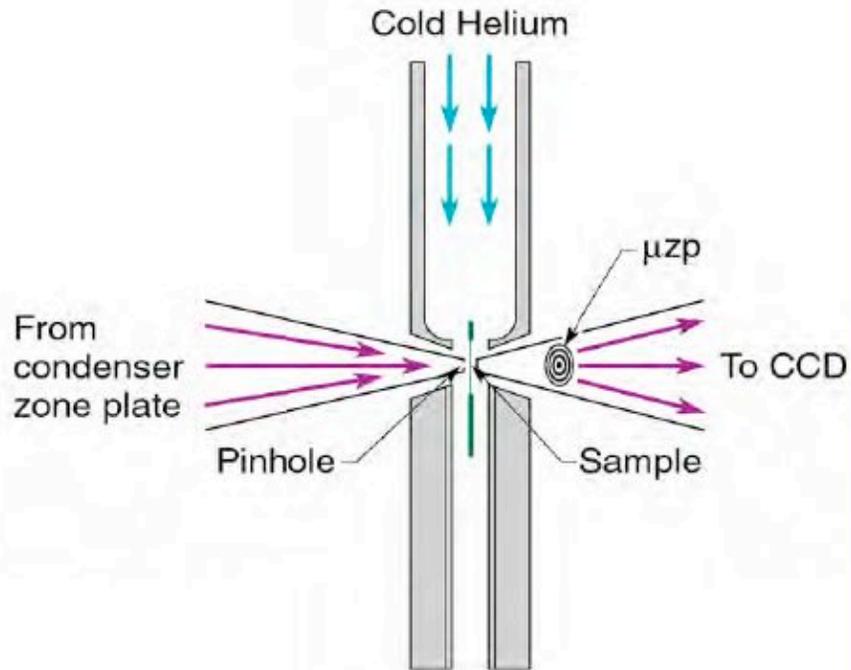
Cell nucleus and nucleoli,
moderately absorbing,
coded orange.

Less absorbing aqueous
regions coded black.

W. Meyer-Ilse et al.
J. Microsc. 201, 395 (2001)

Whole, hydrated mouse epithelial cell

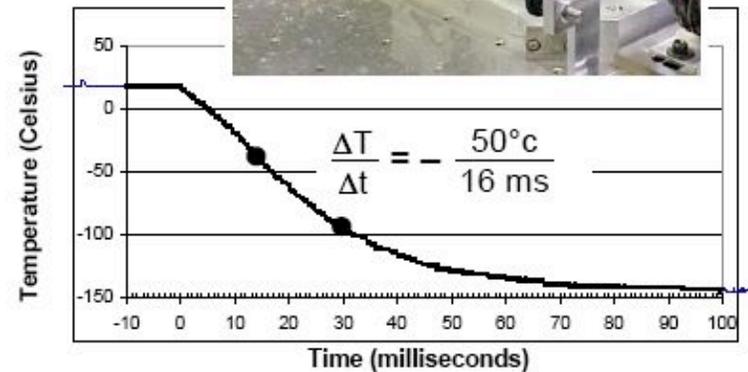
Cryo-preparation of sample mitigates radiation damage



Helium passes through LN, is cooled, and directed onto sample windows

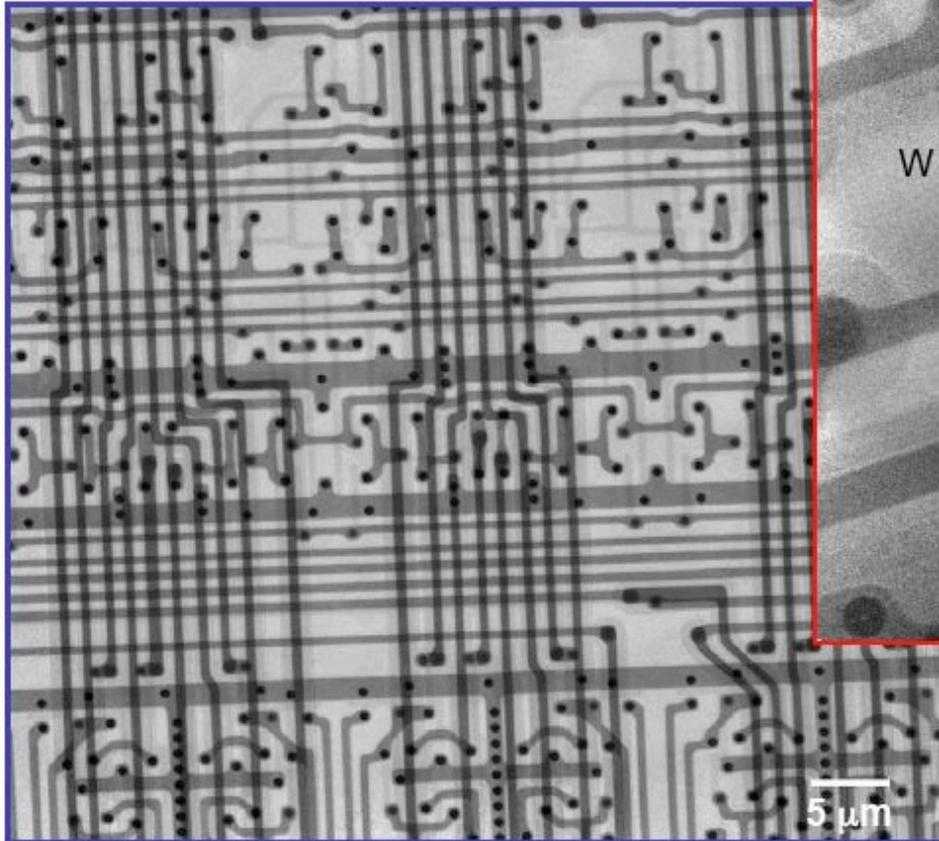


Fast Freeze

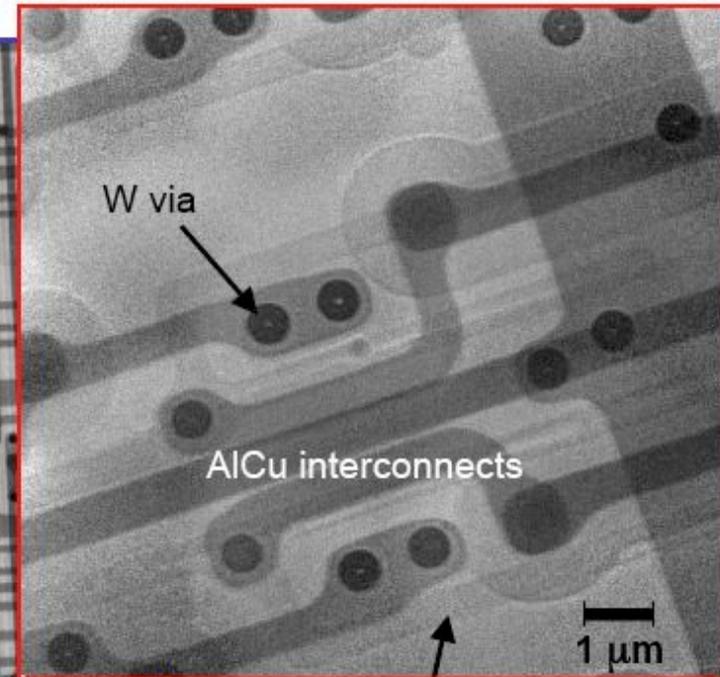


Interconnects in chips are more "hardy"

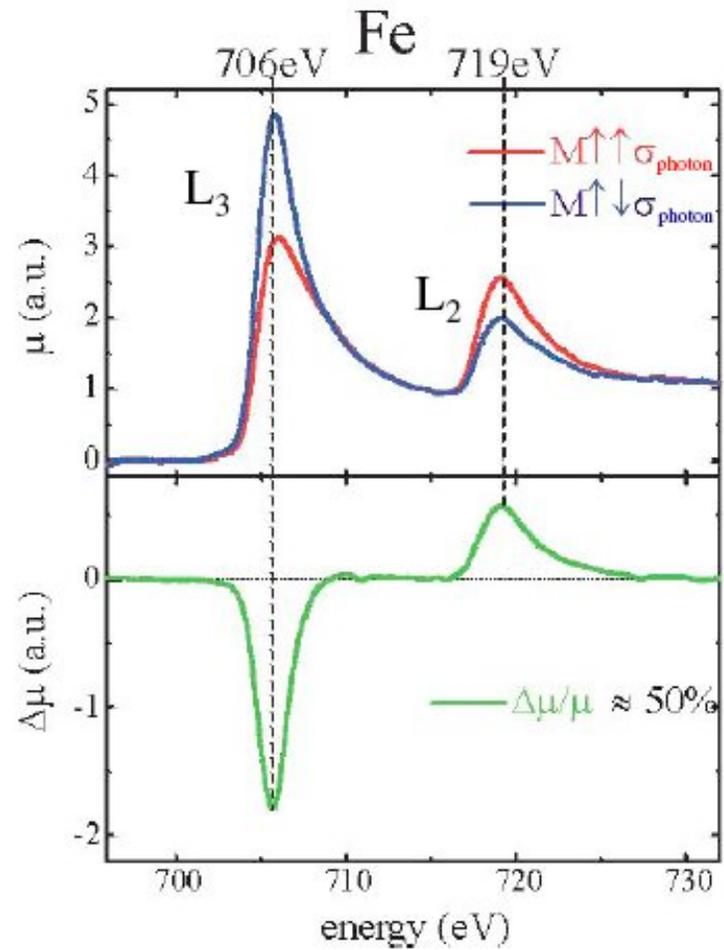
Intact microprocessor
(for anti-lock brakes)



Magnified region

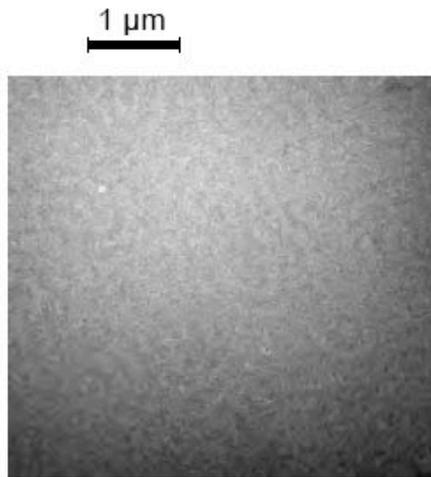


Circular dichroism contrast using polarized x-rays

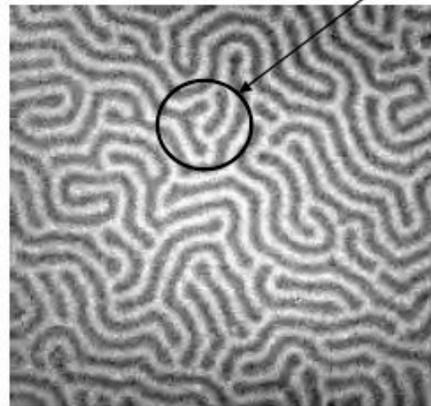


Magnetic x-ray microscopy

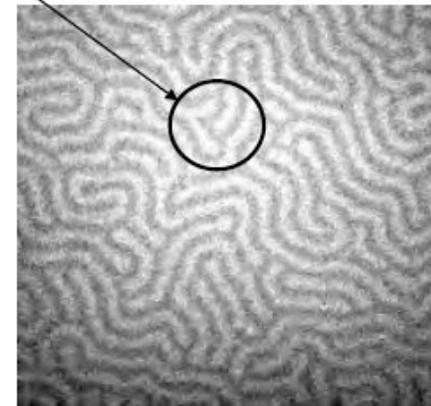
FeGd Multilayer



$\hbar\omega = 704$ eV
below Fe L-edges



$\hbar\omega = 707.5$ eV
Fe L₃-edge

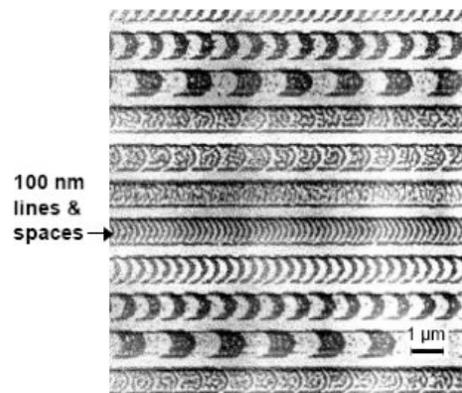


$\hbar\omega = 720.5$ eV
Fe L₂-edge

Contrast reversal

**Magnetic recording materials:
FeTbCo multilayer with Al cap layer**

P. Fischer (MPI), G. Denbeaux (CXRO)



Fe L₃ @ 707.5 eV

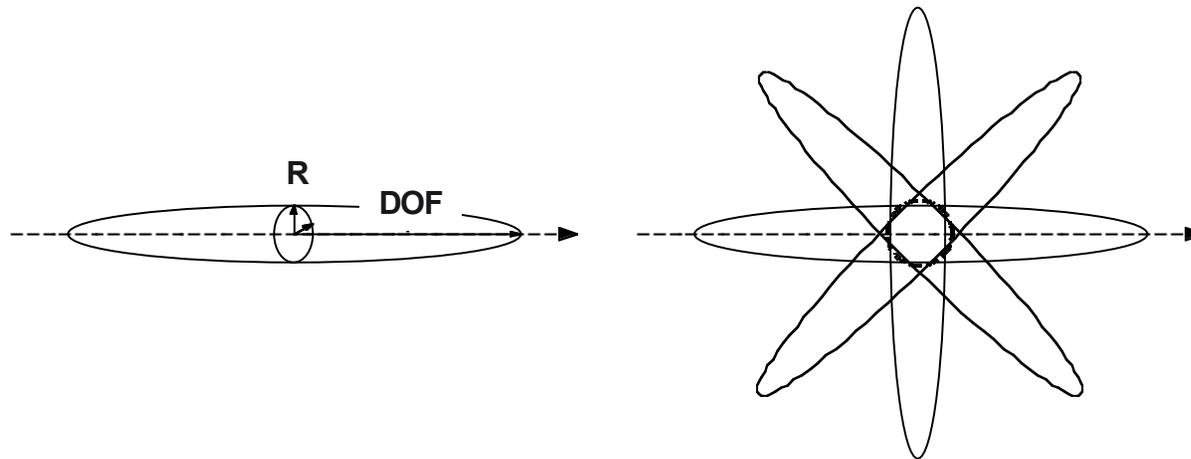
3D imaging

$$R \approx 0.61 \lambda / NA$$

$$DOF \approx 1.22 \lambda / (NA)^2 = 2 R^2 / (0.61 \lambda)$$

$$|n| \approx 1 \Rightarrow NA \ll 1 \Rightarrow DOF \ll R$$

Synthesize larger NA with multiple views



Cannot improve R , only DOF by tomography

Computed tomography

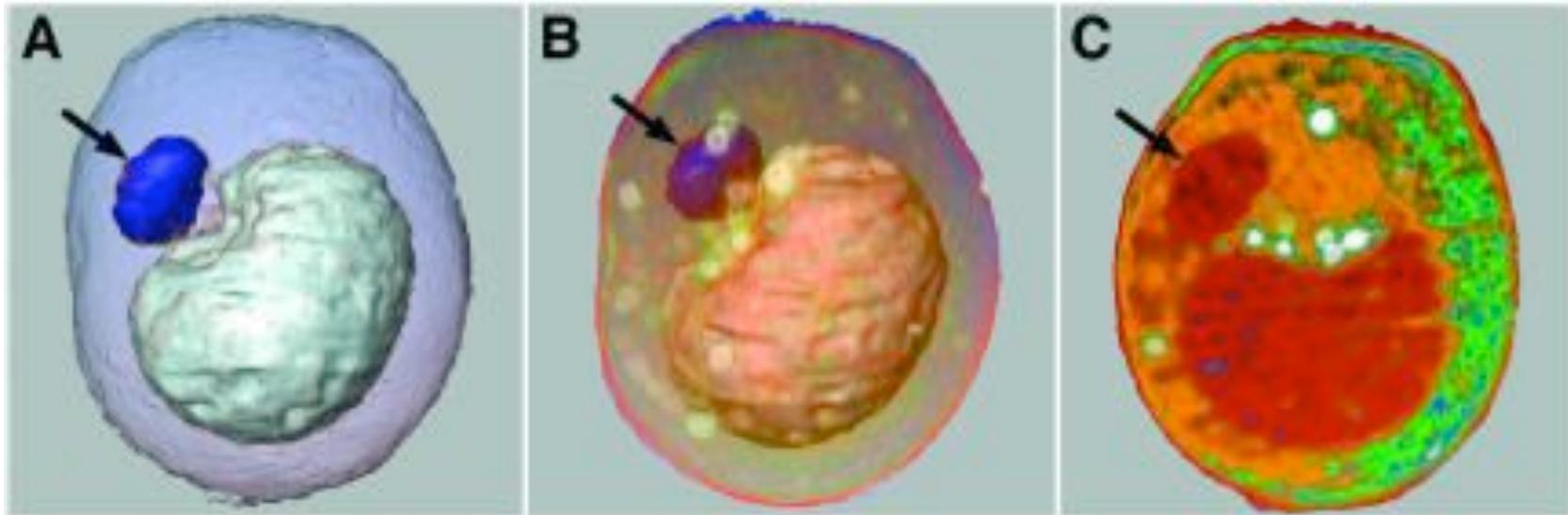
- 1 Record many projections through sample over wide angular range. Projections at angles θ contain:

$$I(x, y, \theta) = I_0 e^{-\int \mu_{\theta}(x', y', z') dz'}$$

- 2 Reconstruct 3D sample density from suite S of projections

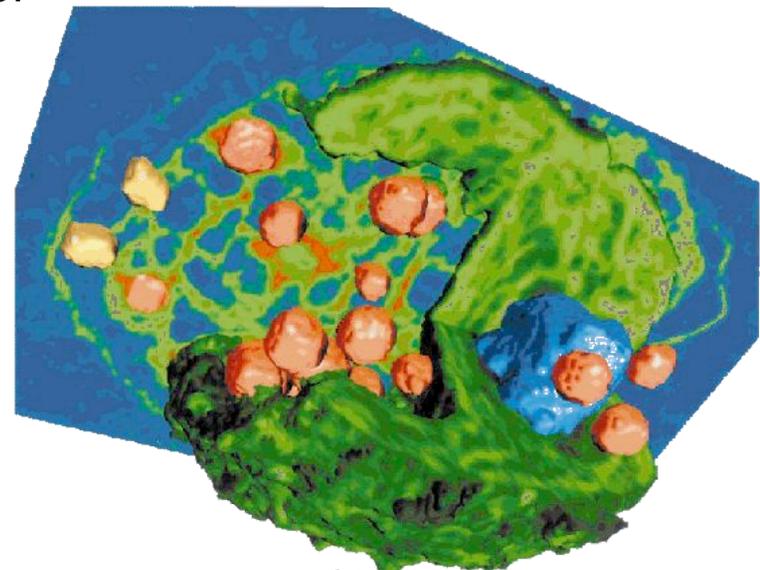
$$\text{Invert } S\{I(x, y, \theta)\} \Rightarrow \mu(x, y, z)$$

Soft x-ray nanotomography



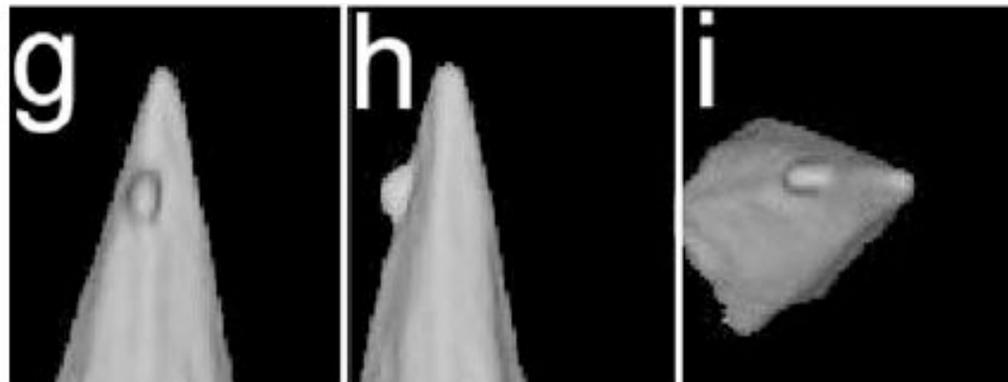
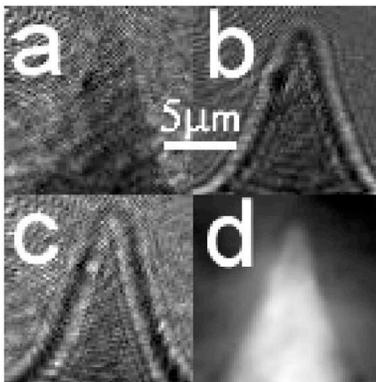
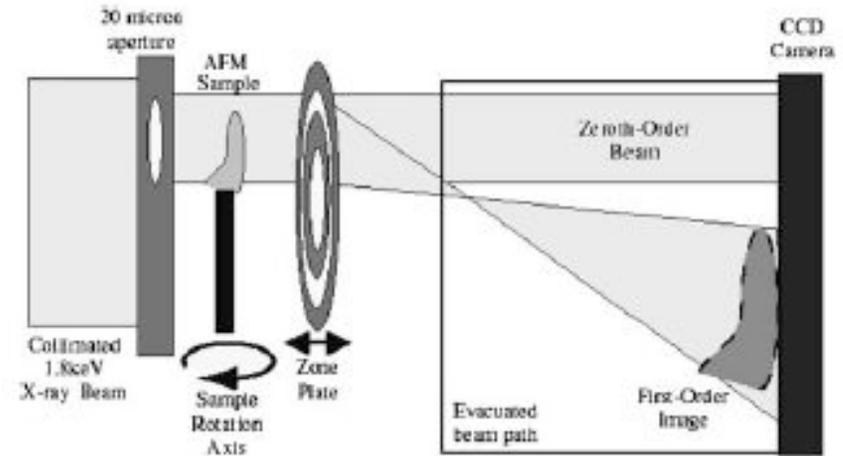
Frozen hydrated yeast *Saccharomyces cerevisiae* C. Larabell, M. Le Gros, *Mol. Biol. Cell* **15**, 957 (2004)

Frozen hydrated alga *Chlamydomonas reinhardtii*: D. Weiß, G. Schneider, *et al.*, *Ultramicroscopy* **84**, 185 (2000)



Quantitative phase tomography

- Defocus series (a, b, c) and phase (d) of a silicon AFM tip
- Quantitative 3D reconstructions of real part of refractive index from $\pm 70^\circ$ tomographic projections through tip
- Calculated $\delta = 5.1 \times 10^{-5}$
Measured $\delta = 5.0 \pm 0.5 \times 10^{-5}$

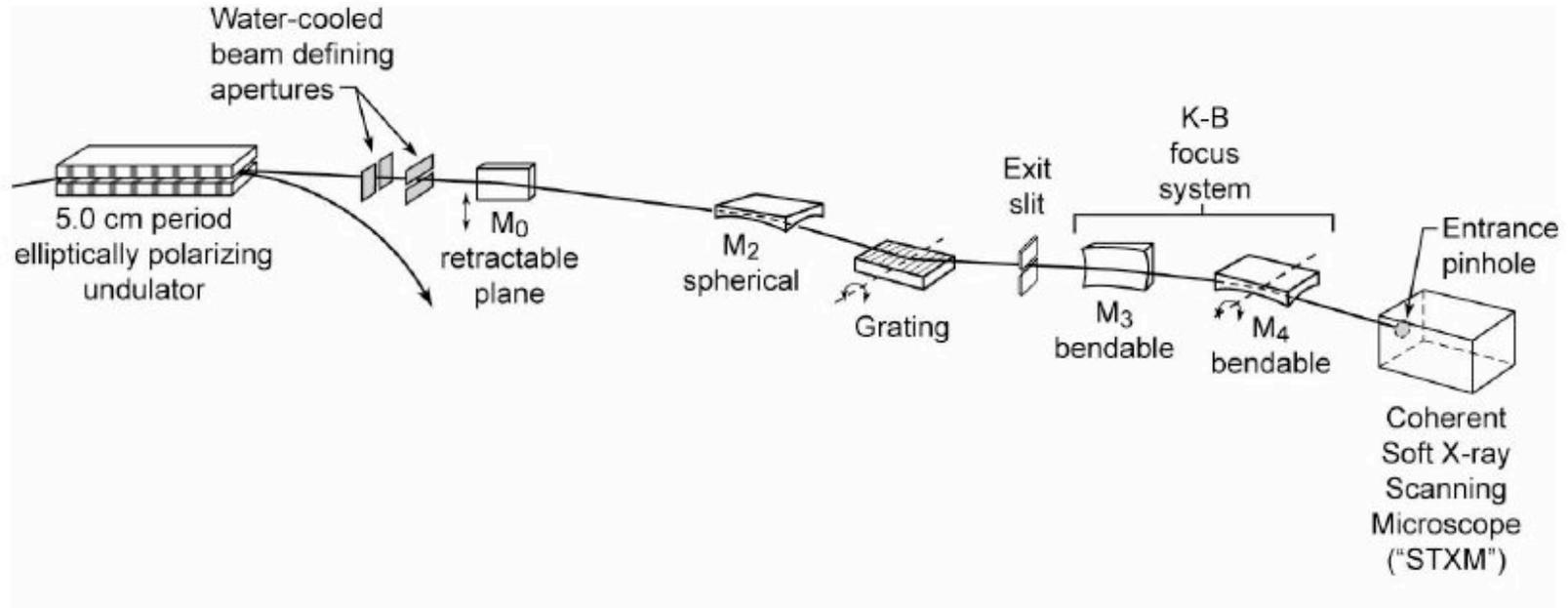


P. McMahon et al., *Opt. Commun.* 217, 53 (2003)

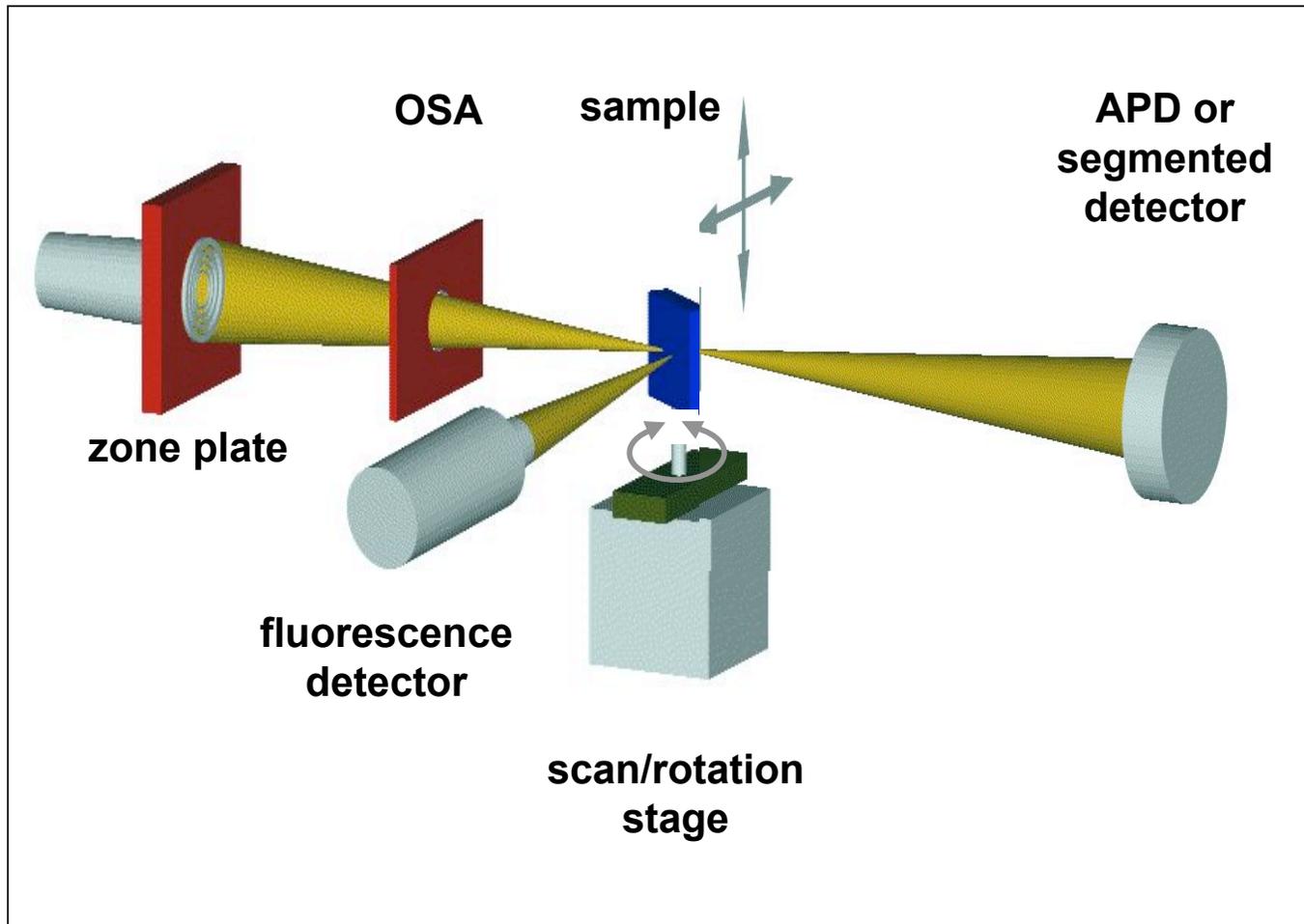
Full-field microscopy with hard x-rays



Beamline for scanning microscopy (soft x-ray)



1-4 keV scanning x-ray microscope at APS 2-ID-B



X-ray probe

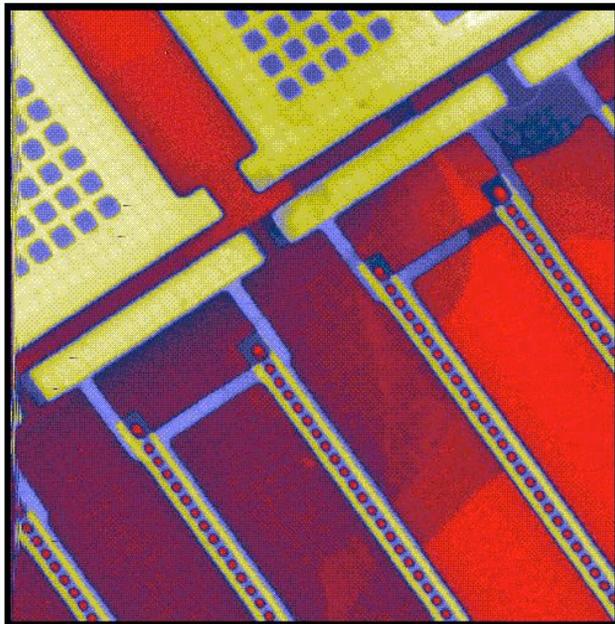
- Fresnel ZP
- 60 nm spot
- 10^8 - 10^9 ph/s

Contrast modes

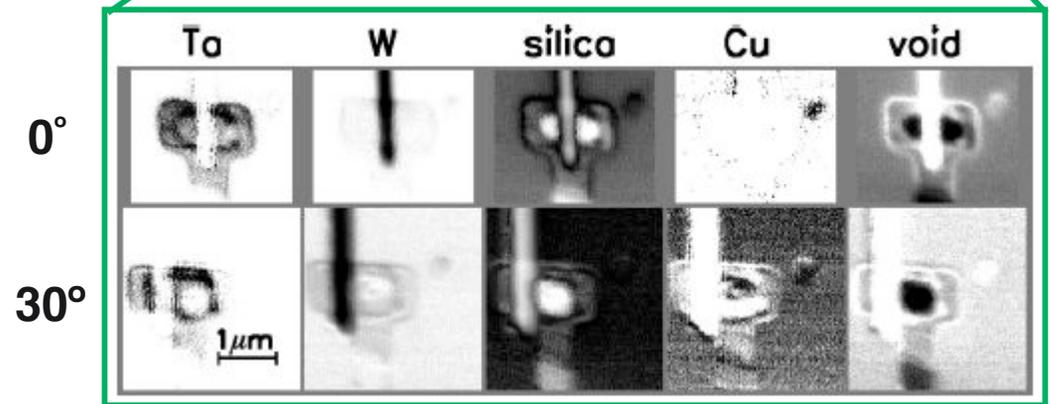
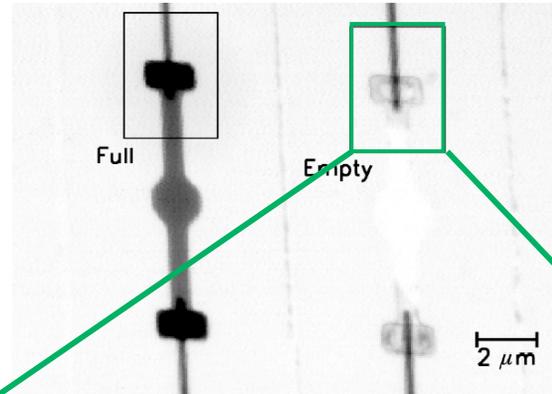
- Transmission
- Fluorescence
- Micro-XANES

Defects in buried interconnects

Example: Ta-lined Cu interconnect, W vias



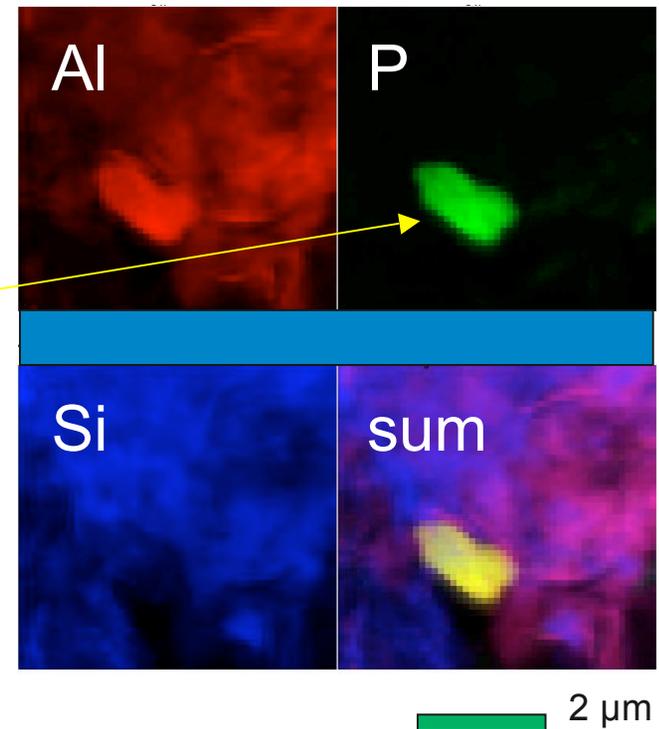
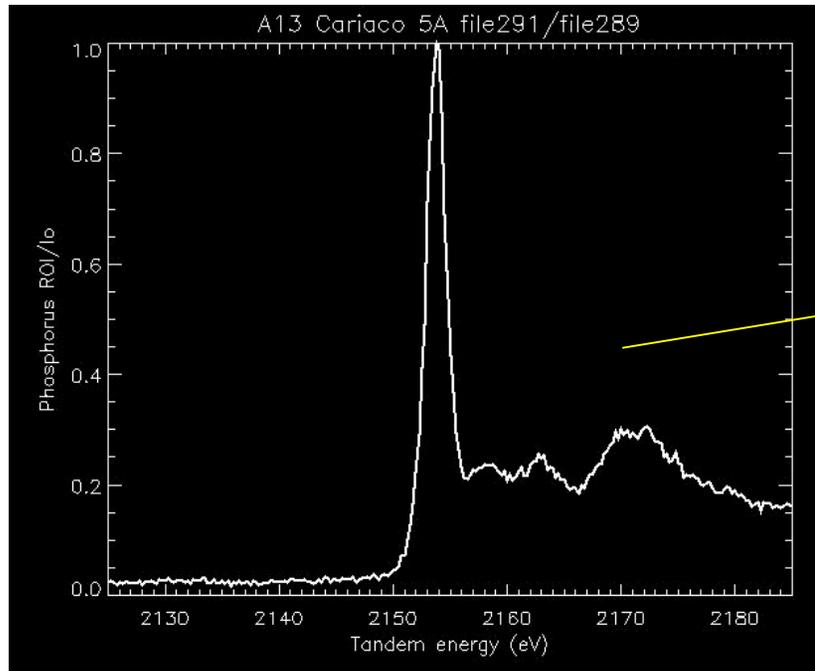
10 μm



Z. Levine et al., *J. Appl. Phys.* 95, 405 (2004)

X-ray spectromicroscopy is valuable to study P speciation

Marine sediments contain complex, heterogeneous P chemistry.
P typically shows little covariance with most other elements.

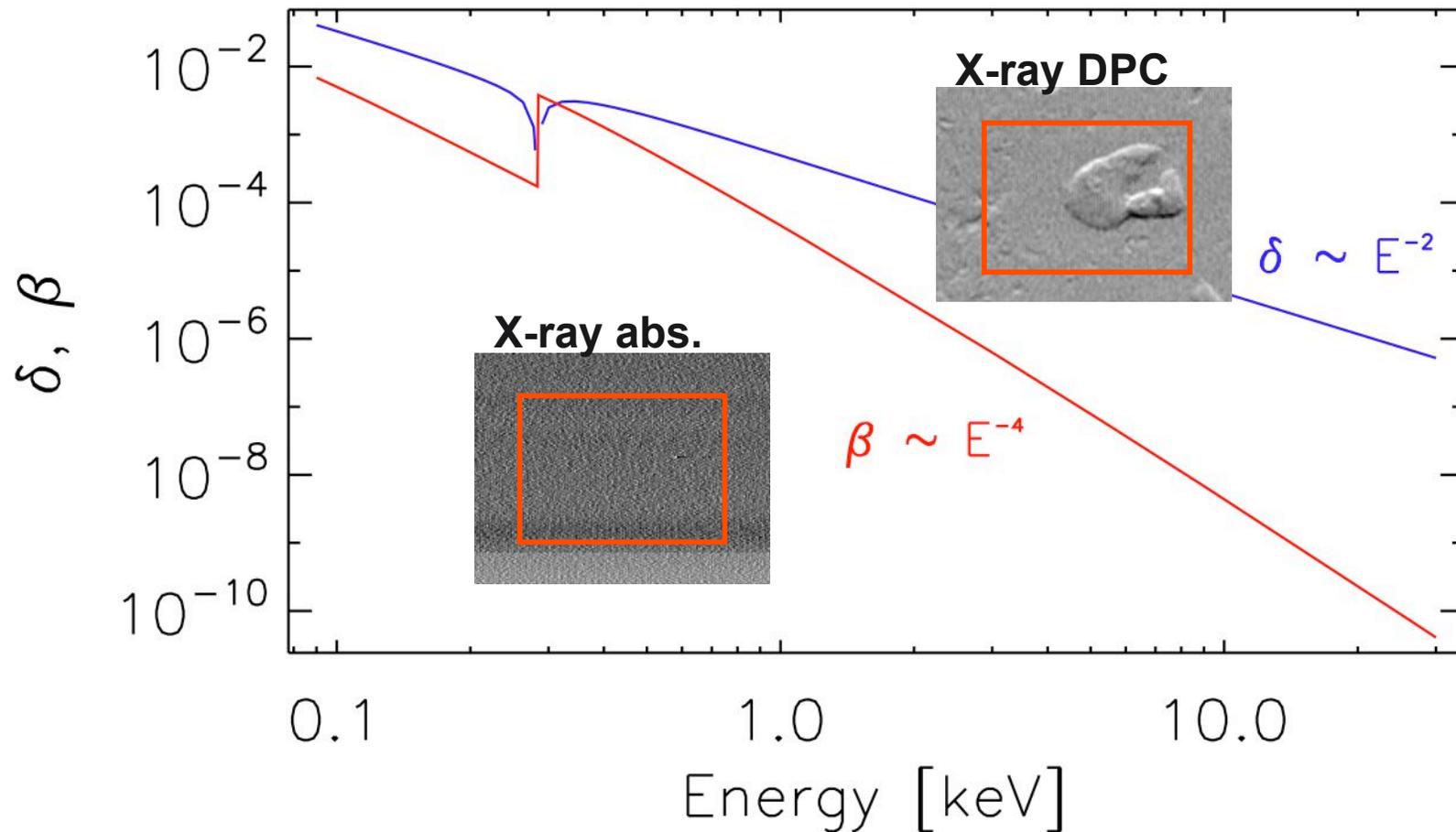


- Occasionally find odd P-containing minerals with distinctive P-XANES that do not match closely with any known Al-phosphate mineral
- Previously unknown in marine samples - Riverine or Aeolian source?

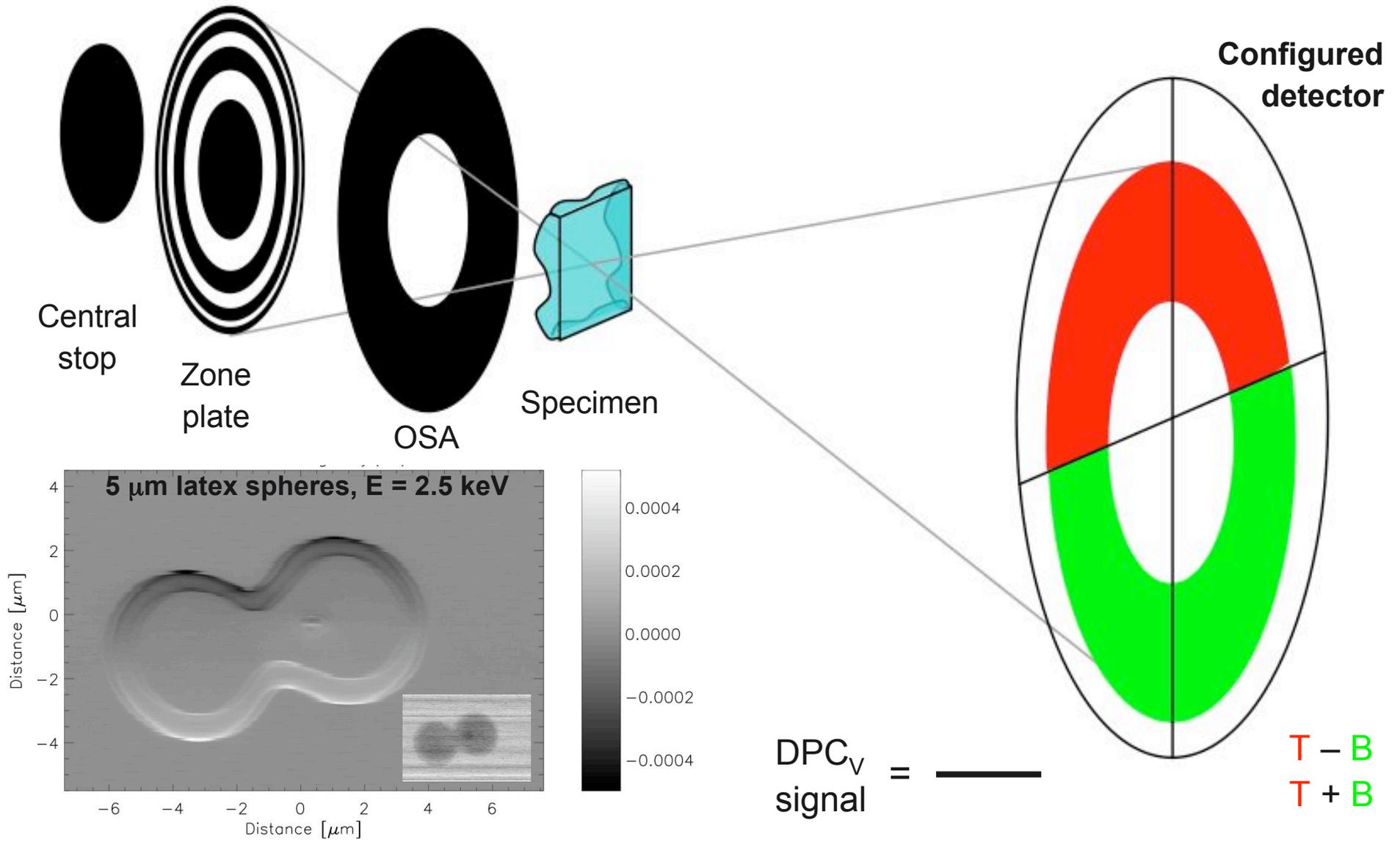
J. Brandes et al., *Marine Chem.* 103, 250 (2007)

Use phase contrast for biological specimens

Complex transmission function: $\exp(i \delta kt) \exp(-\beta kt)$
phase shift absorption

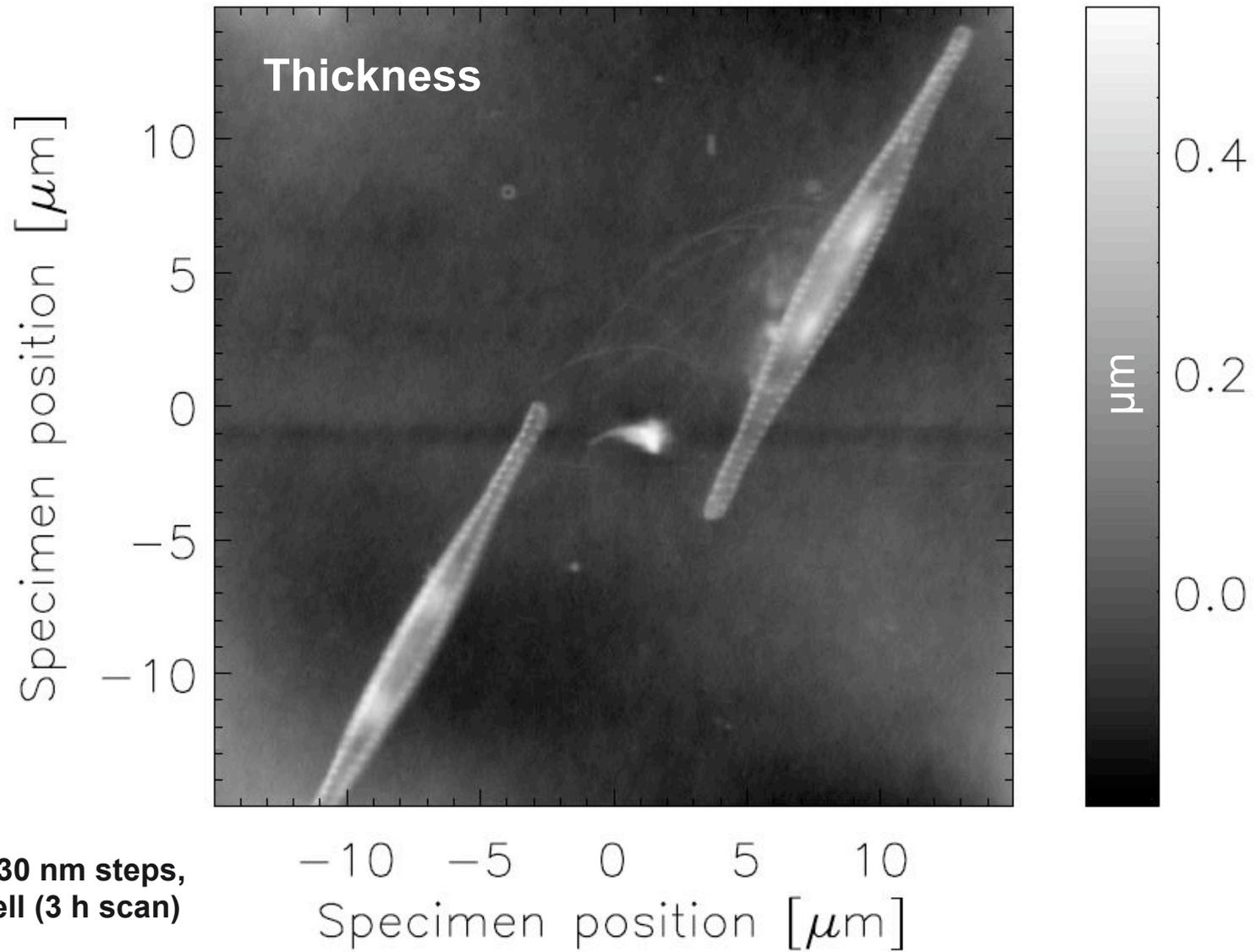


STXM: differential phase contrast



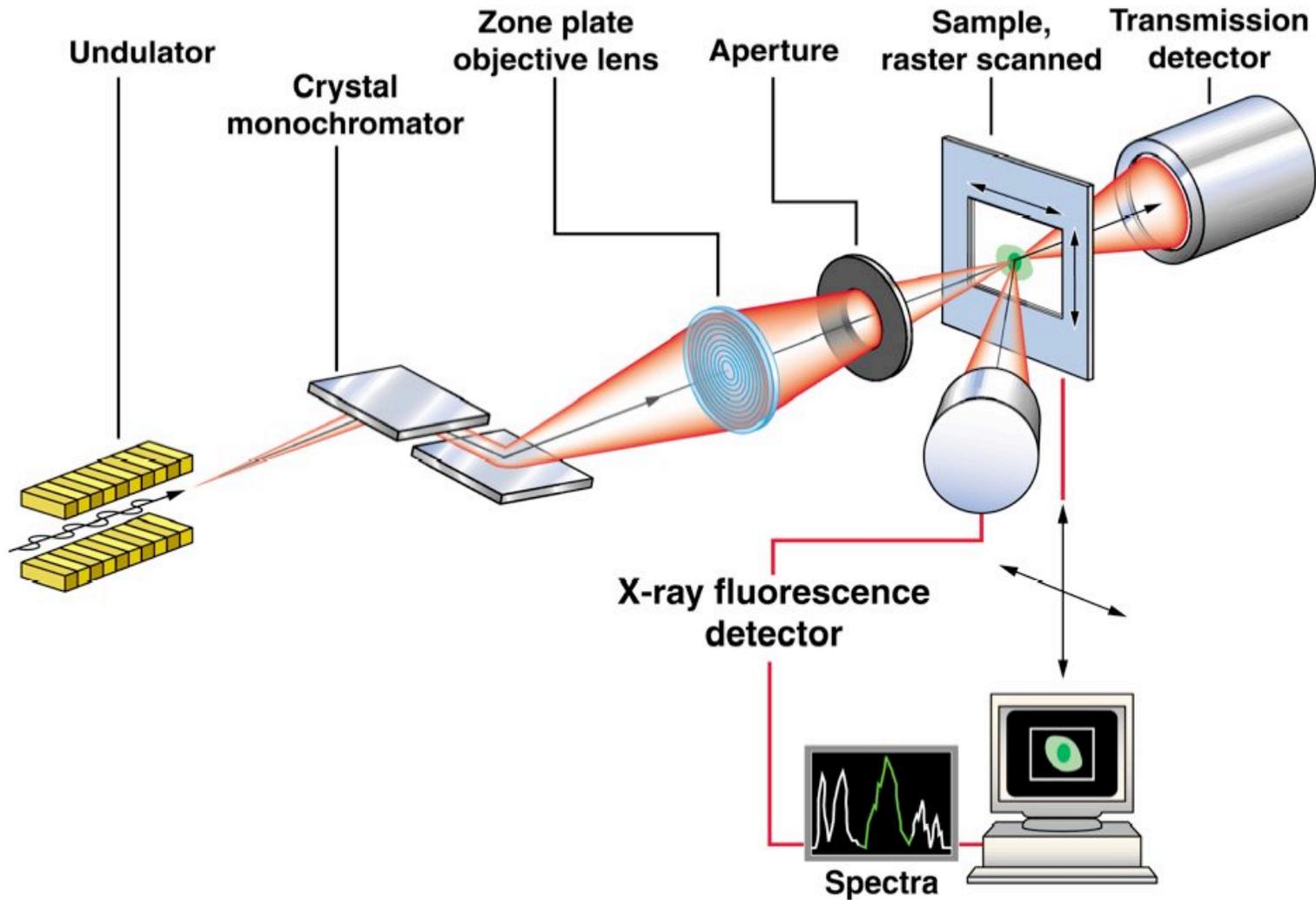
M. de Jonge et al., *PRL* 163902, (2008)

Pennate diatoms



2535 eV, 30 nm steps,
5 ms dwell (3 h scan)

Hard x-ray scanning fluorescence microscope



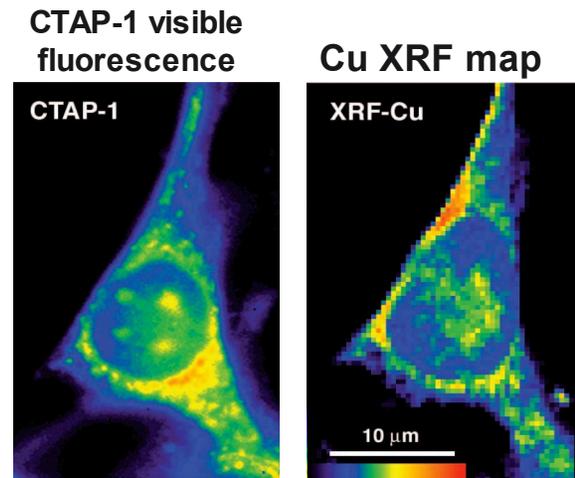
Copper is an essential trace element for all life forms

- **Catalyzes production of highly reactive oxygen species**

⇒ oxidative damage to lipids, proteins, DNA, etc

- **Defects in regulatory processes may led to:**

- ✓ Menkes syndrome
- ✓ Wilson's disease
- ✓ Amyotropic lateral sclerosis (ALS)
- ✓ Alzheimer's disease

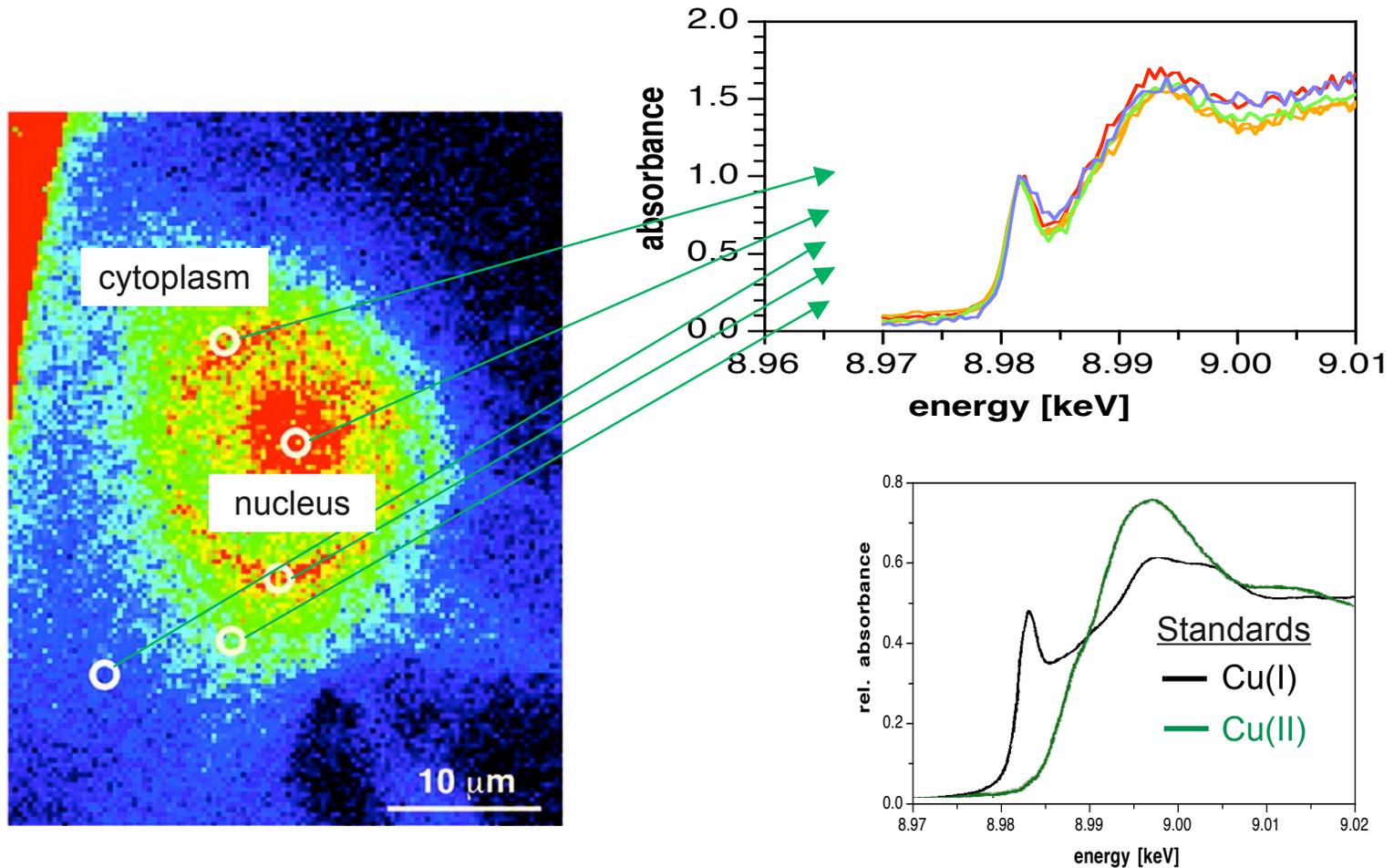


Mouse fibroblast cell + 150 μM CuCl₂

- **Need to be understand cellular uptake, trafficking, storage of Cu**
- **Novel Cu(I) fluorescent sensor (CTAP-1) was recently developed**

⇒ *Does it reflect the true cellular distribution?*

μ -XANES indicates Cu(I) is present (reducing environment)

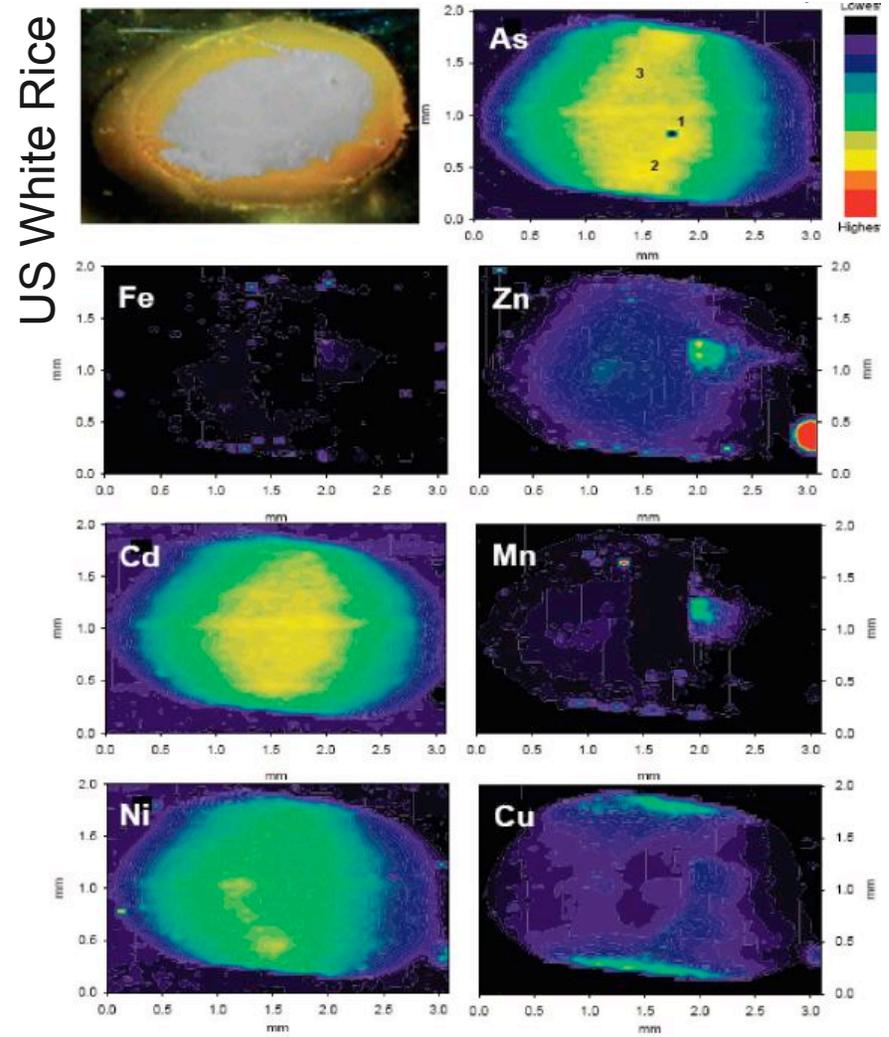


L. Yang et al., *Proc. Natl. Acad. Sci.* 102, 11179 (2005)

Arsenic distribution and speciation in rice grains

A. Meharg, E. Lombi, P. Williams, K. Scheckel, J. Feldmann, A. Raab, Y. Zhu, and R. Islam, *Environ. Sci. Technol.* 42, 1051 (2008)

- There is worldwide concern over elevated arsenic concentrations in regions where rice paddy fields are irrigated with As contaminated groundwater.
- Rice production increasingly occurs in As and metal contaminated soils in Asia
- S-XRF was utilized to locate As in polished (white) and unpolished (brown) rice grains from the United States, China, and Bangladesh
- As dispersed in white rice but localized in the pericarp and aleurone layer of brown rice - Cu, Fe, Mn, and Zn localization followed that of As in brown rice
- μ -XANES and bulk extraction revealed the presence of mainly inorganic As and dimethylarsinic acid (DMA)
- Percentage of DMA present in the grain increased along with total As.



3. Indirect methods

- **Microdiffraction**
 - Scanning (monochromatic/Bragg)
 - 3D differential-aperture x-ray microscopy (white/Laue)

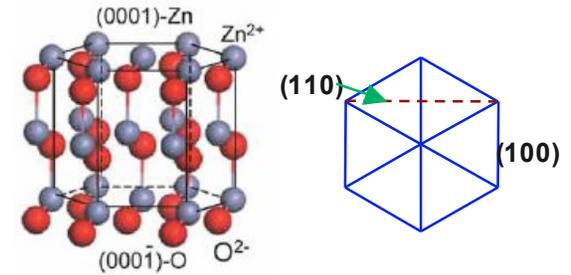
- **Coherent diffraction imaging**

- **Holography**

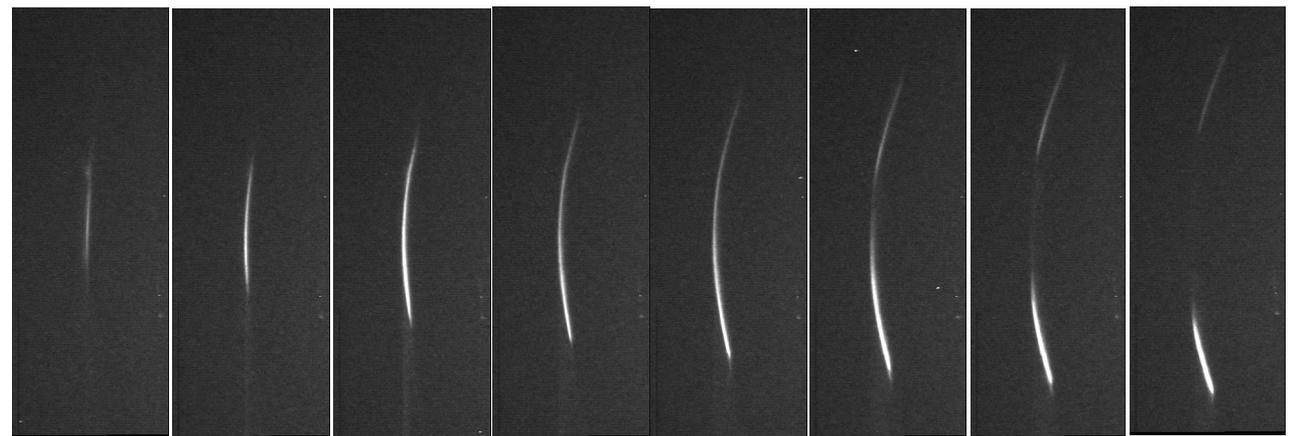
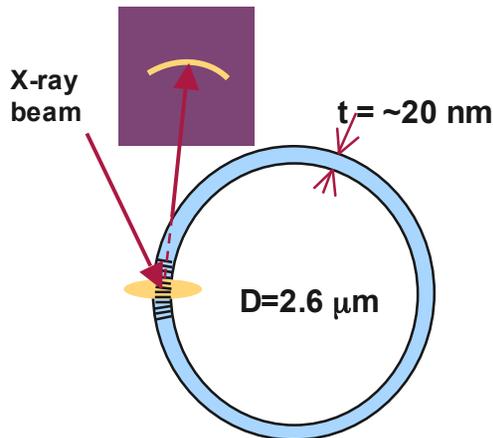
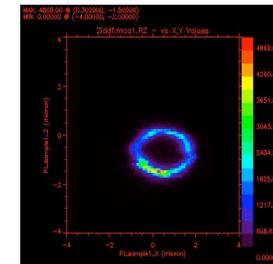
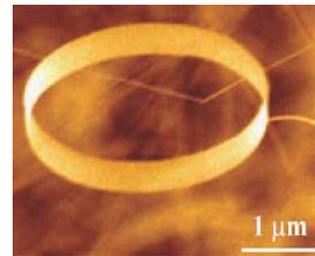
Is there lattice strain in zinc oxide nano-rings?

Termination at Zn (+) and O (-) results in spontaneous polarization along the c-axis resulting in formation of nano-rings

Internal lattice strain and distribution needed to study balance between mechanical and electronic configurations for nano-sensor applications.



X-ray fluorescence (Zn K α) map

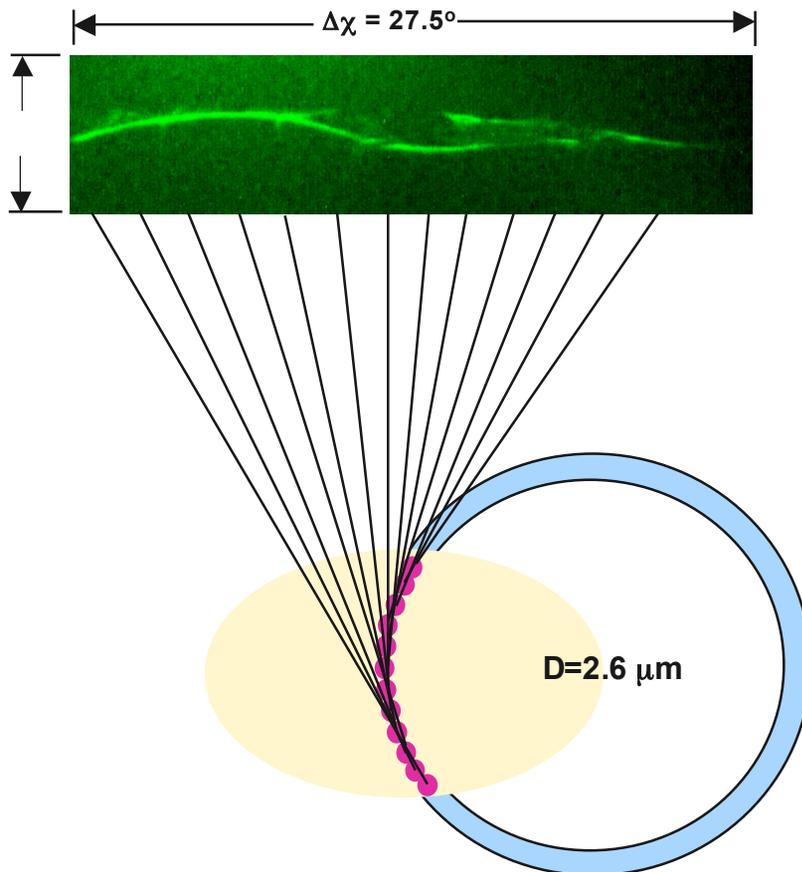


Diffraction of Zn (110) from a section of the ring. Patterns were taken at angles θ across the rocking curve width

X-ray nanodiffraction explains strains

Image (220) reflections from ZnO nanoring with CCD using 10 keV x-rays

Patterns cover a θ angular range of 0.6°

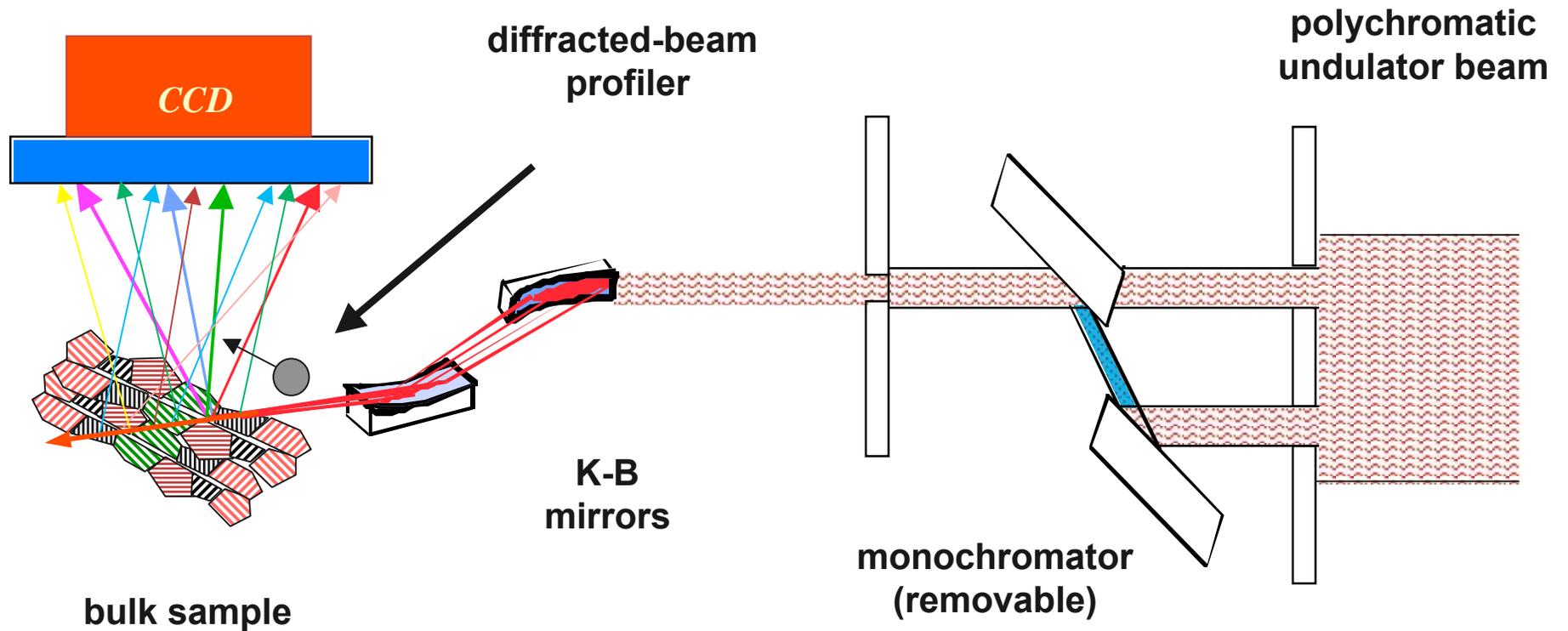


- Might expect that coiling stress would cause a continuous strain distribution from compressive to tensile across the ring width.
- The two branches of the diffracted intensity indicate existence of two strain domains, with as much as 1.8% difference in the (220) plane spacing.
- Data show the structure either collapses into distinct domains across the ring width, or exhibits strain that varies little in width but continuously up to 2.4% along the ring arc.

Y. Xiao et al., *JSR* 12, 124 (2005)

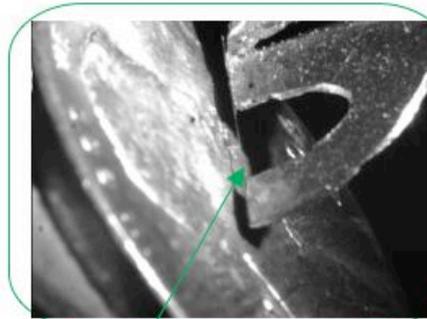
Differential-aperture x-ray microscopy

3D depth-resolved, white-beam Laue diffraction technique



B. Larson et al., *Nature* 415, 887 (2002)

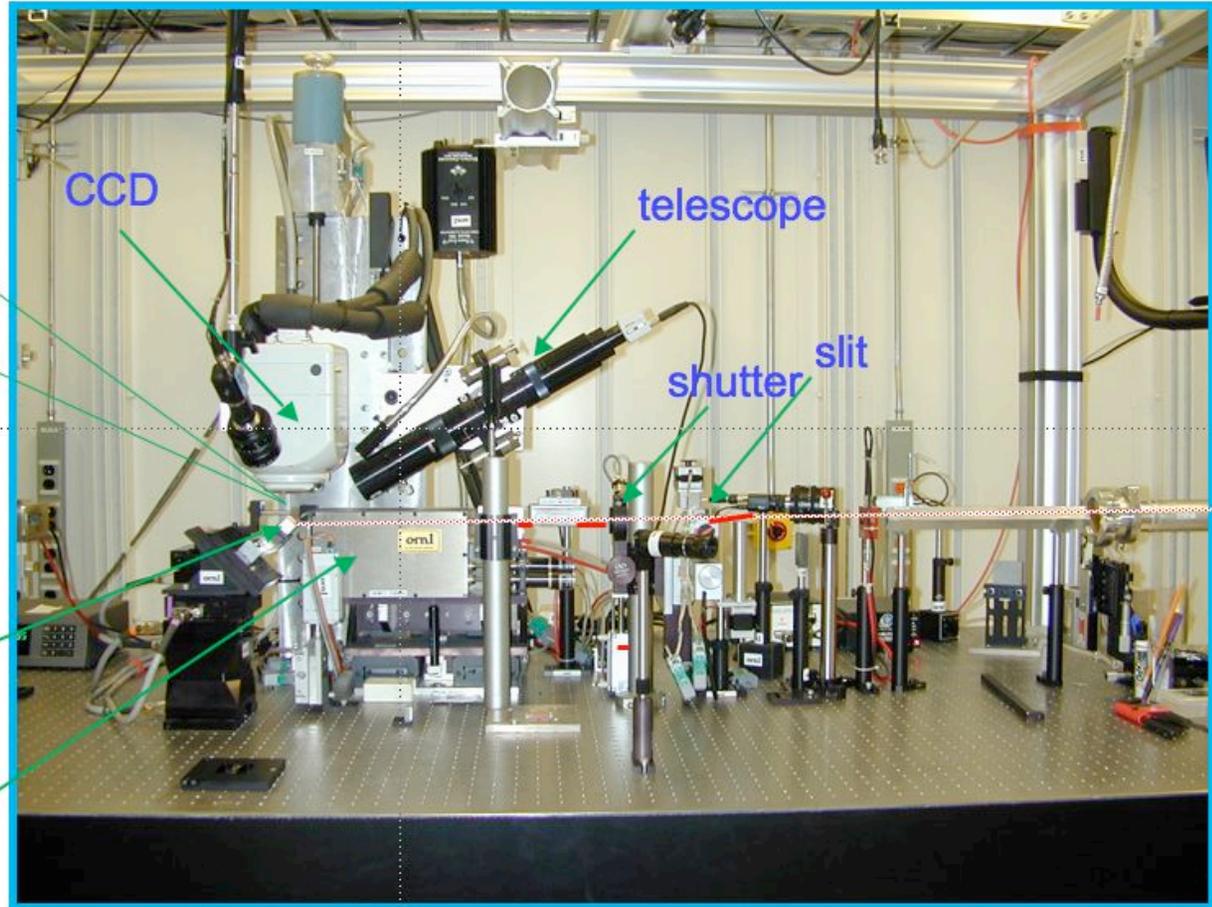
3D diffraction microscope at APS beamline 34-ID-E



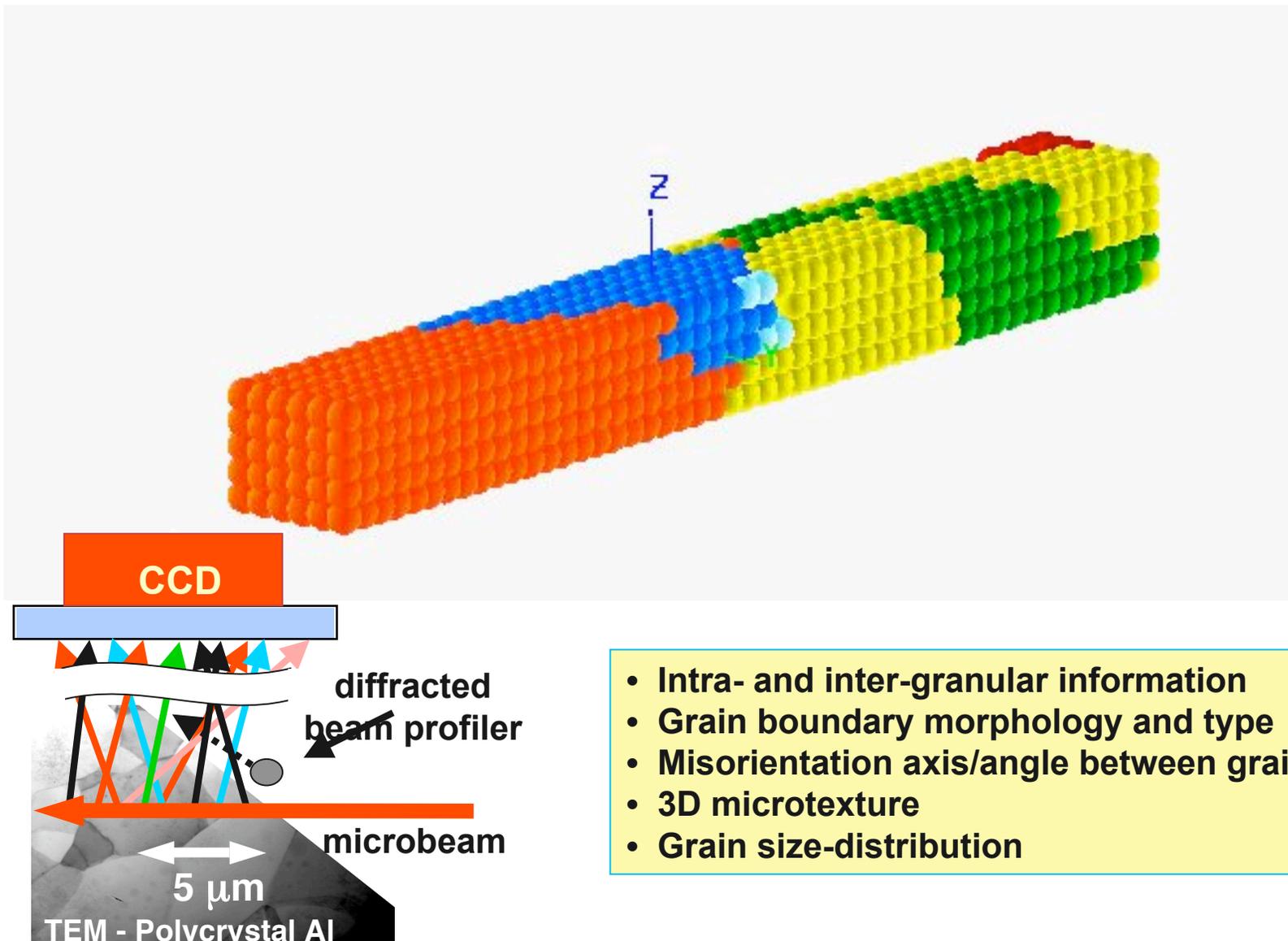
Differential aperture
(wire scan, ~ 200 mm
above sample surface)

Sample stage

K-B focusing
mirrors

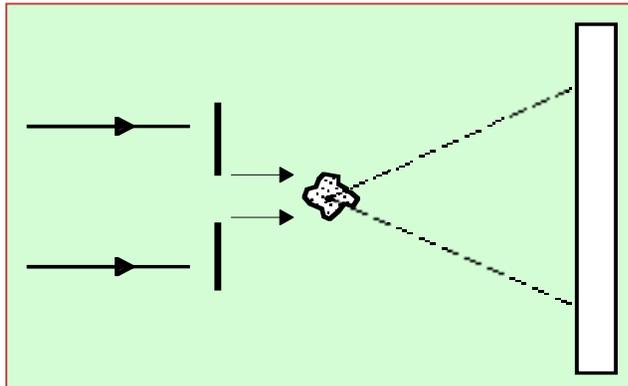


DAXM illuminates the 3D structure of aluminum



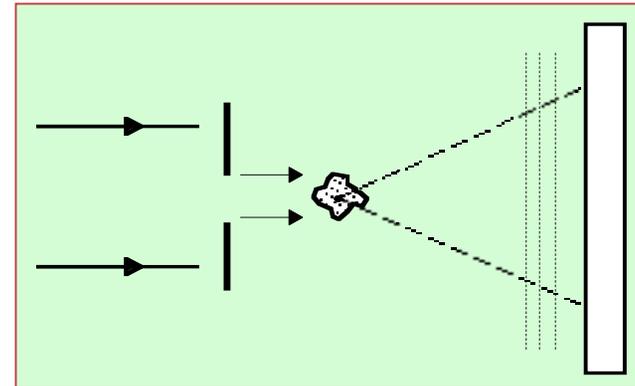
W. Yang, et al., *Micron* 35, 431 (2004)

Coherent diffraction and holography: "lensless" imaging



Coherent Diffraction

- Object wave (diffraction) is detected directly
- Diffraction intensity corresponds to autocorrelation of object



Holography

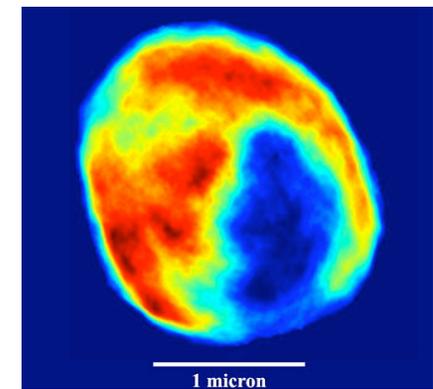
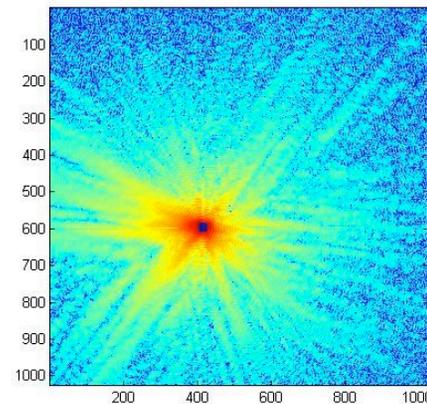
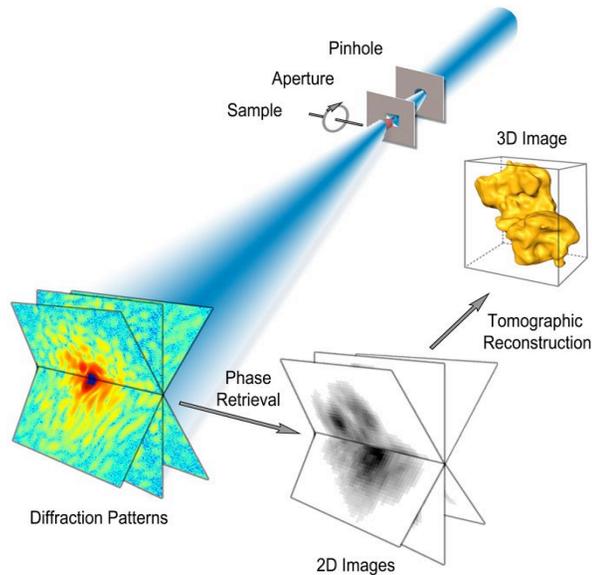
- Coherent reference wave interferes with object wave to form hologram
- Hologram intensity corresponds to convolution of object and reference

Resolution:	transverse	$\sim \lambda/NA$
	longitudinal	$\sim \lambda/(NA)^2$
Contrast:		$\propto f_1^2 + f_2^2 $

Coherent diffraction x-ray imaging

Lensless method - resolution limited only by wavelength, signal

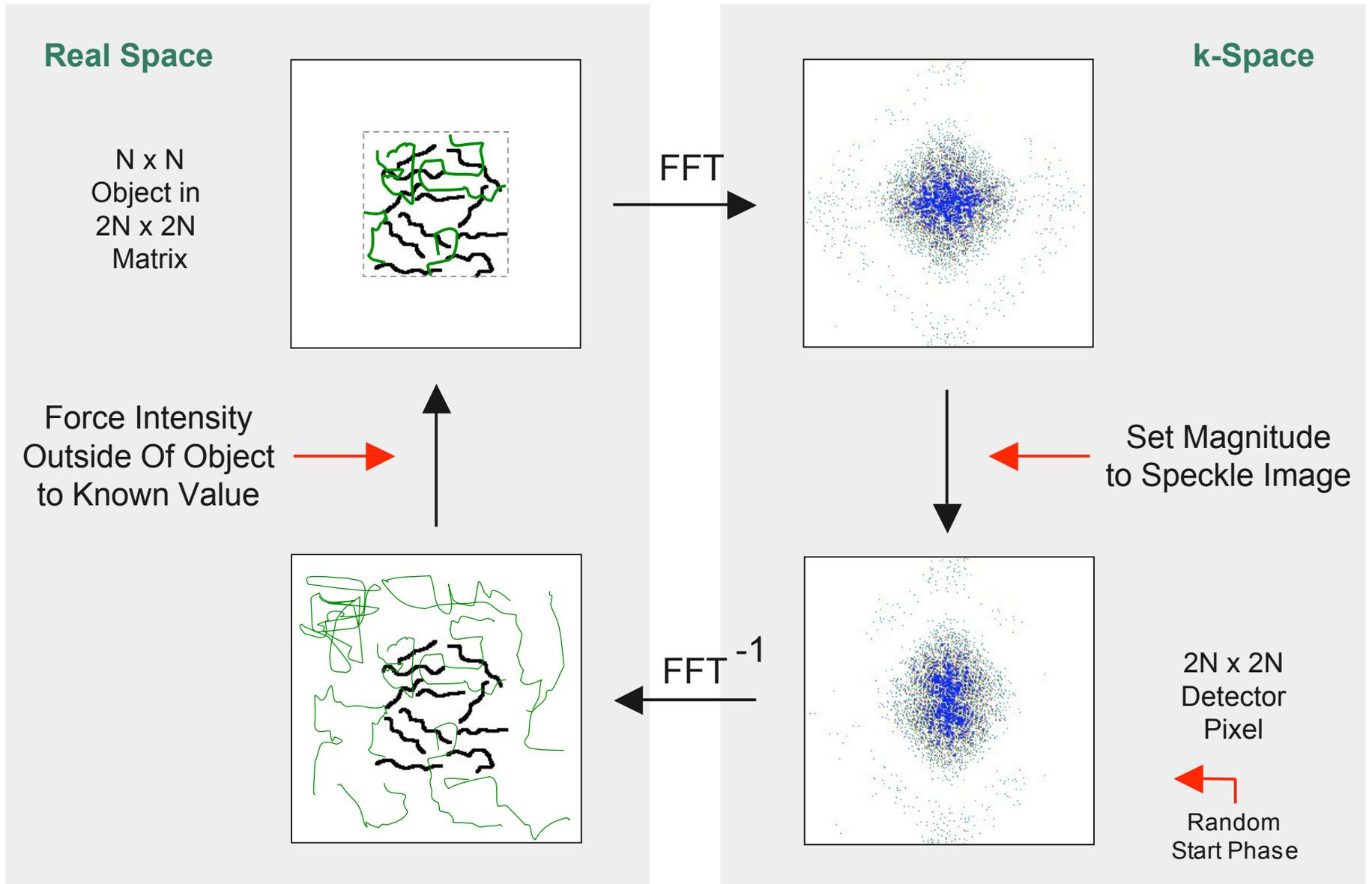
- **Two-step process: record coherent diffraction pattern, recover object structure numerically (iterative phase retrieval)**
- **Sensitive to phase as well as absorption of the specimen**
- **Get 3D by tomographic methods; no depth of field limit**
- **But: must assume some *a priori* information to recover phase, e.g. known object extent or illumination profile**



resolution $\sim \lambda / \text{angular size}$

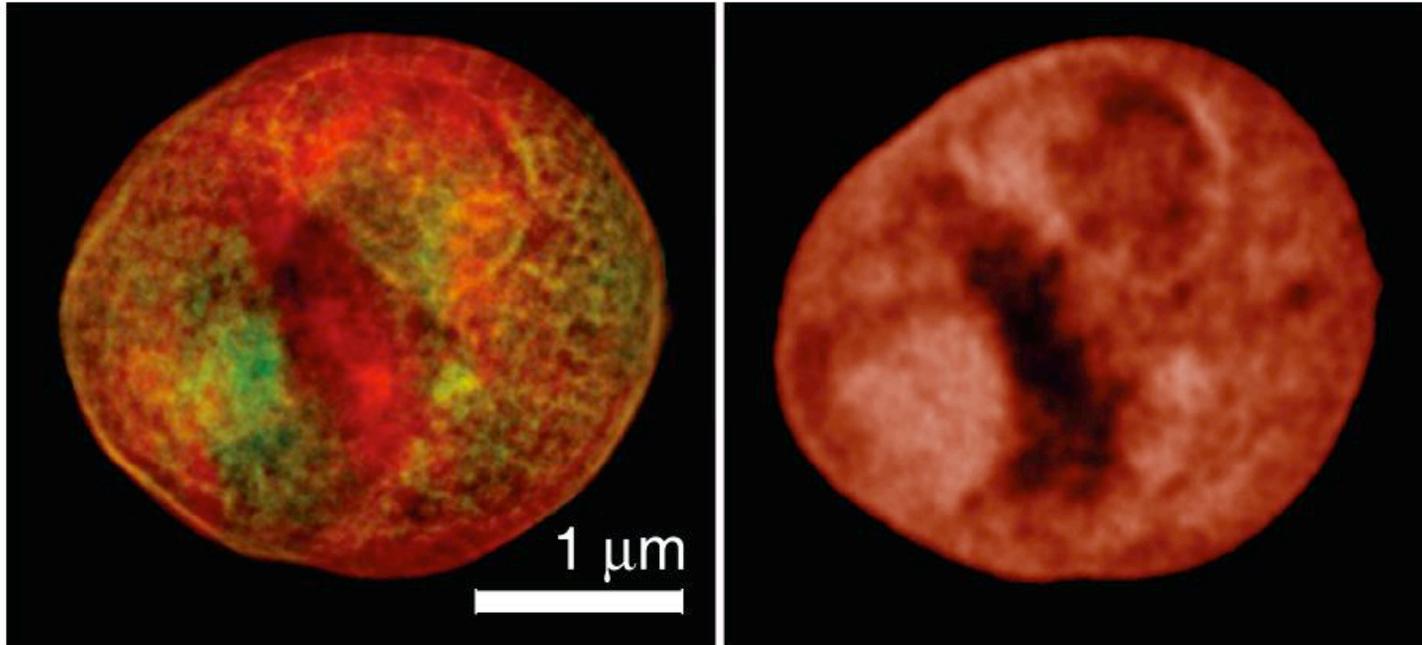
J. Miao, et al., *Nature* 400, 342 (1999)

Iterative phase retrieval



R. Gerchberg and W. Saxton, *Optik* 35, 237 (1972); J.R. Fienup, *Appl. Opt.* 21, 2758 (1982)

Freeze dried yeast cell imaged by coherent x-ray diffraction

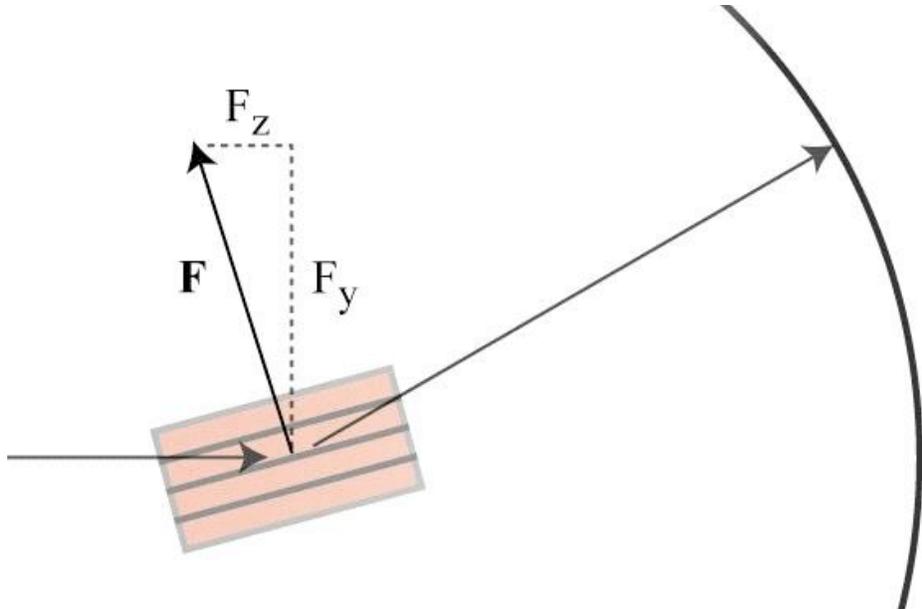


Diffraction reconstruction (data taken at 750 eV; absorption as brightness, phase as hue).

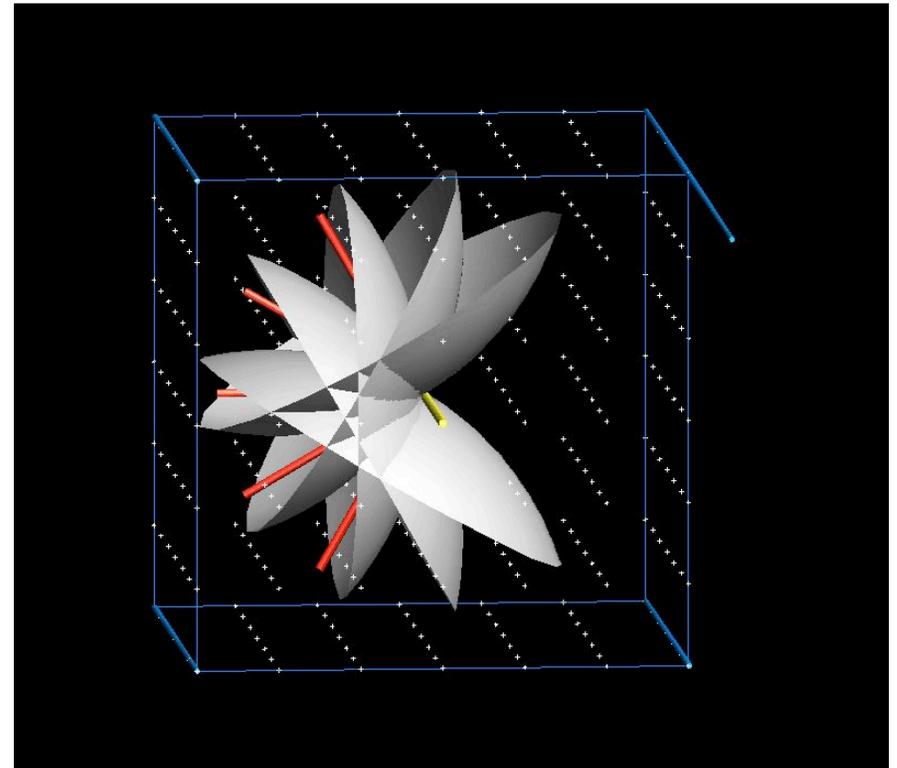
Stony Brook/NSLS STXM image with 45 nm Rayleigh resolution zone plate at 520 eV (absorption as brightness)

D. Shapiro et al., *PNAS* 102, 15343 (2005)

Diffraction microscopy in 3D

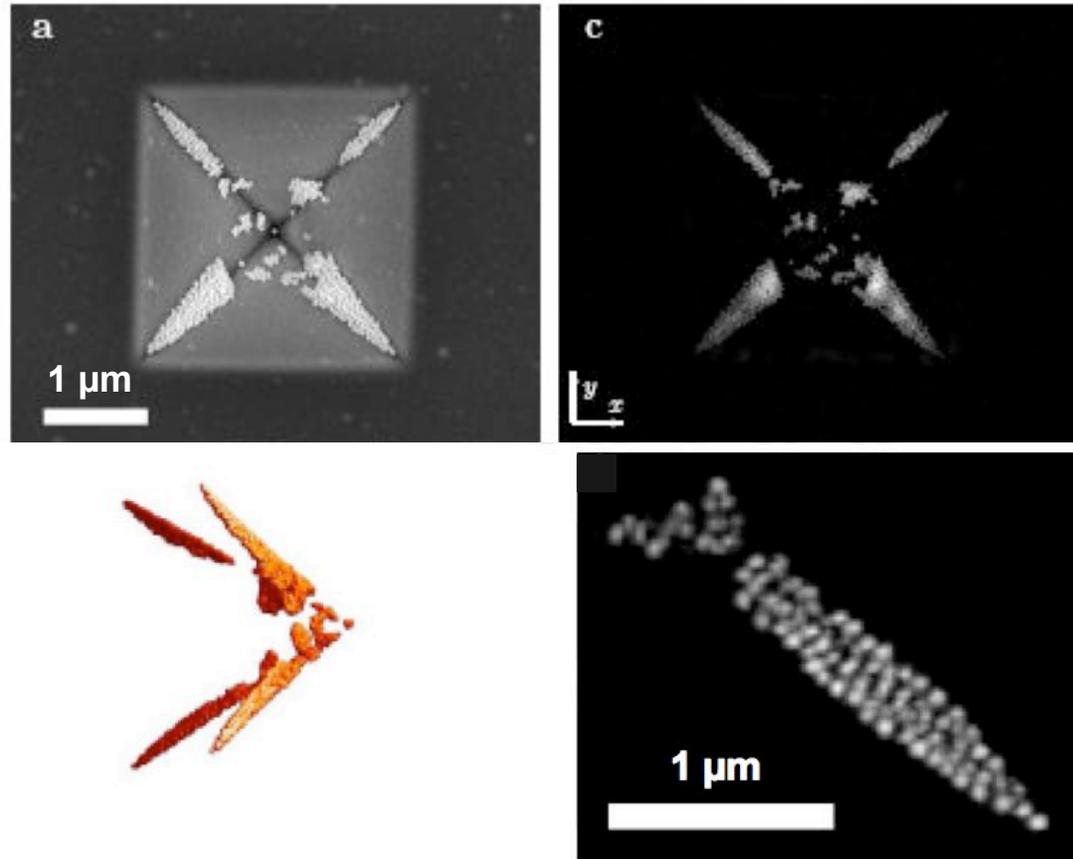


Bragg gratings that diffract to a certain angle represent a specific transverse and longitudinal periodicity (Ewald sphere)



Data collection over a series of rotations about an axis fills in 3D Fourier space for phasing

3D coherent diffraction imaging

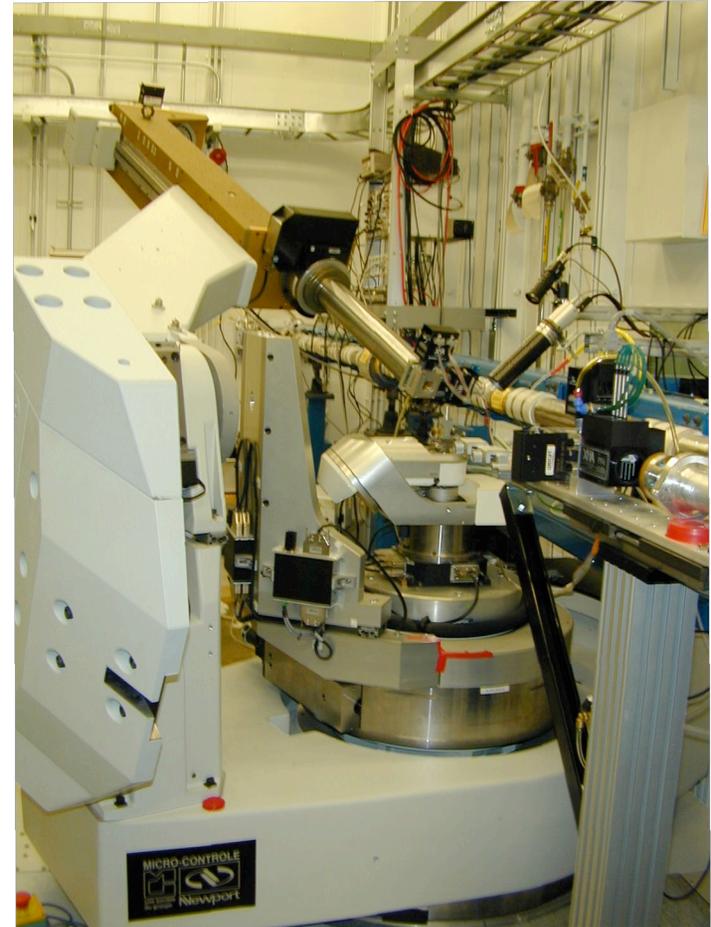


(a) SEM of pyramidal indentation in a 100-nm Si_3N_4 membrane lined with 50-nm Au spheres. (b) 3D image reconstructed from 123 diffraction projections spanning -57° to $+66^\circ$, using reality and positivity constraints. (c) Large DOF projection. (d) Enlarged region of (c).

H. Chapman et al., *JOSA A*23, 1179 (2006)

Coherent x-ray diffraction can reveal strain in crystals

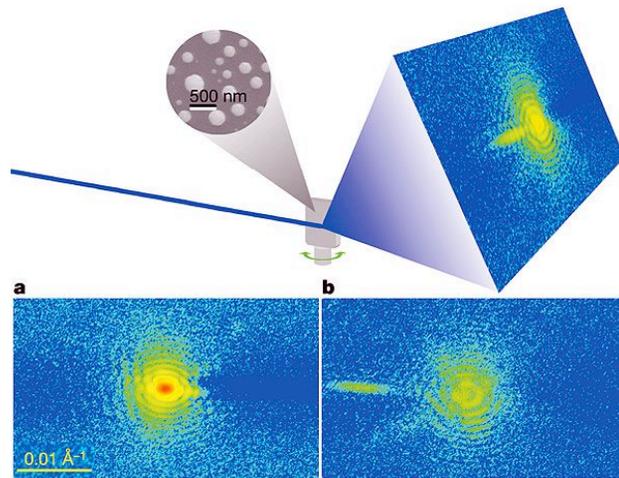
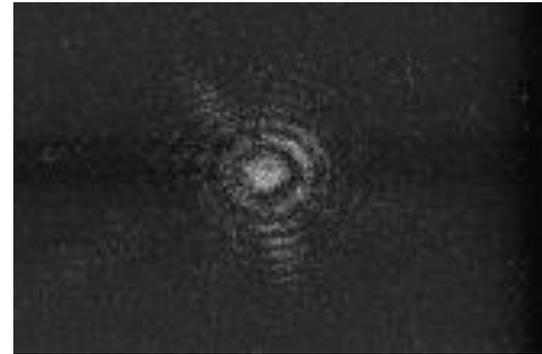
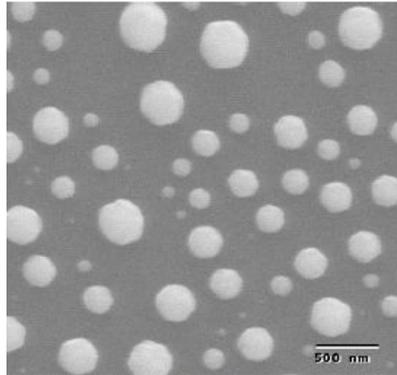
- Double crystal monochromator selects temporal coherence
- Precision slits select spatially coherent fraction of hard x-ray beam
- Diffractometer is used to locate Bragg peaks from an isolated nanocrystal
- Rocking curves around Bragg peak are recorded to obtain 3D data



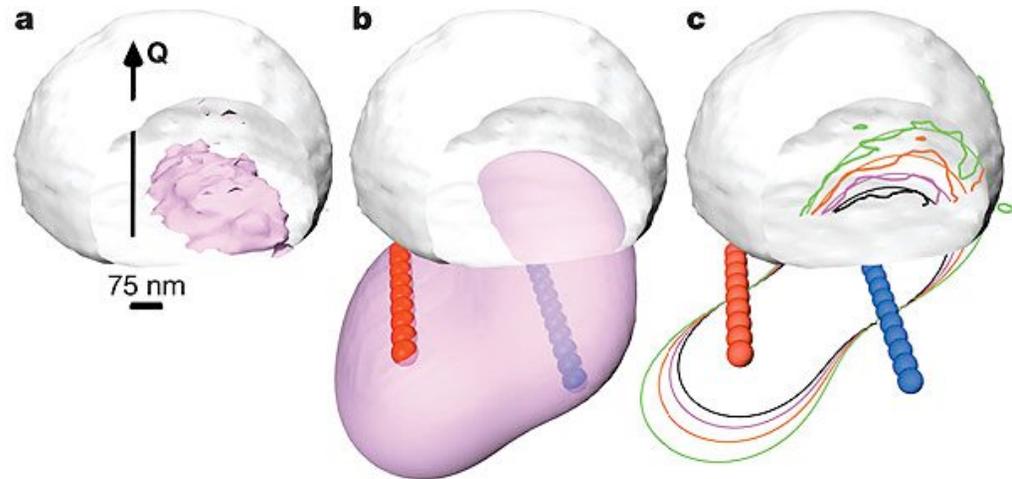
Setup at APS 34-ID-C beamline

Mapping crystal strain in 3D by CDI

0.5 μm Pb crystal grown on SiO_2 substrate



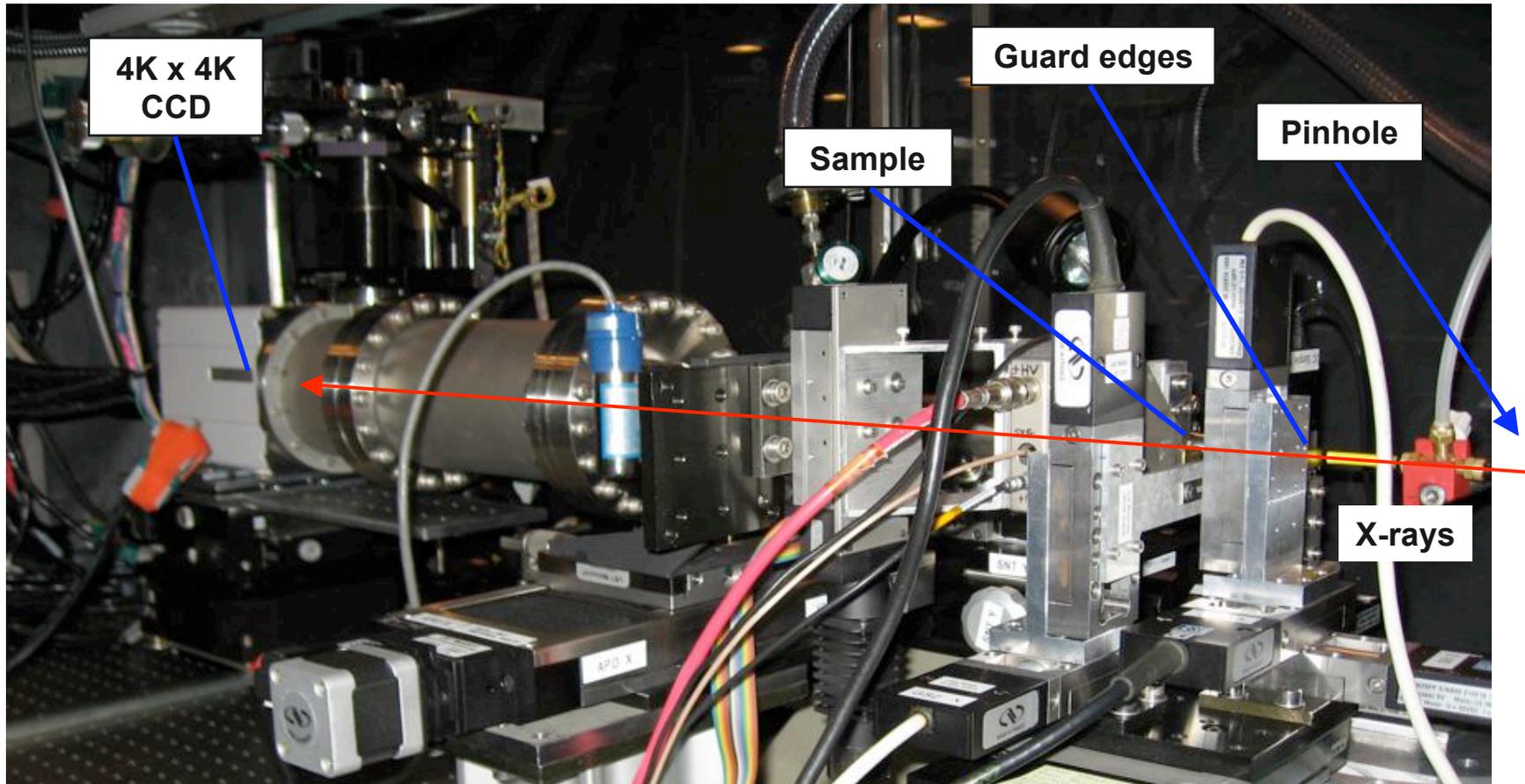
Map series of diffraction patterns about (111) Bragg peak



Diffraction data reconstructed by HIO

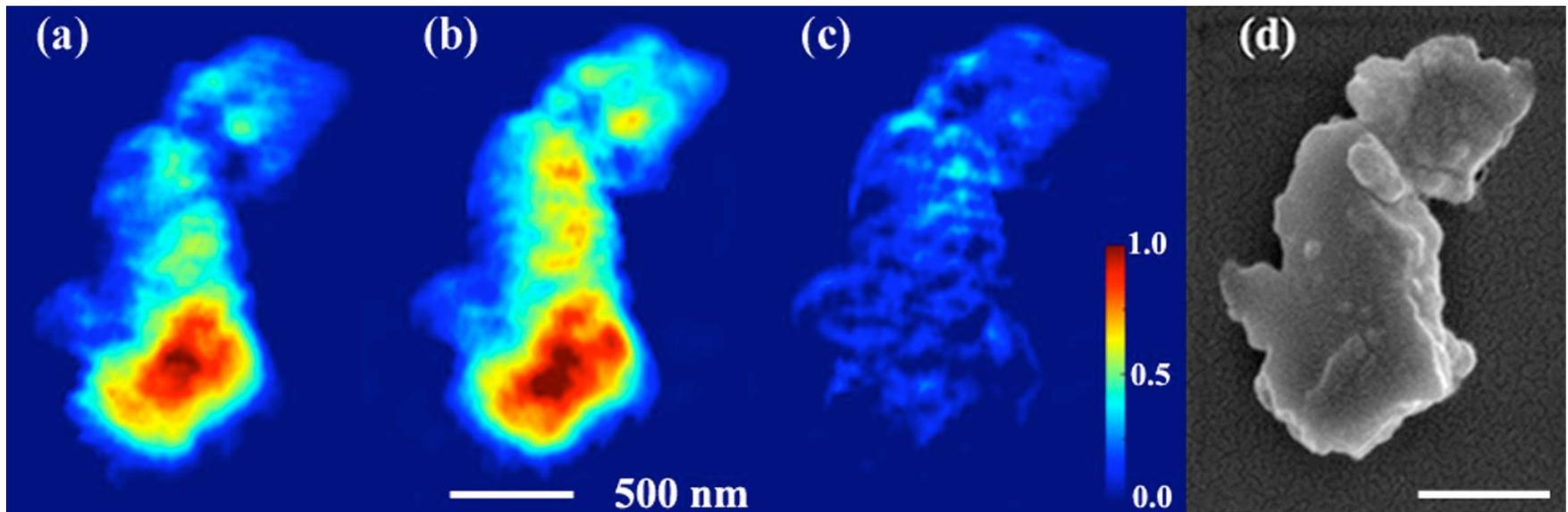
M. Pfeifer et al., *Nature* 442, 63 (2006)

CDI setup at APS beamline 2-ID-B (1-4 keV)



Buried structures can be probed with element specificity

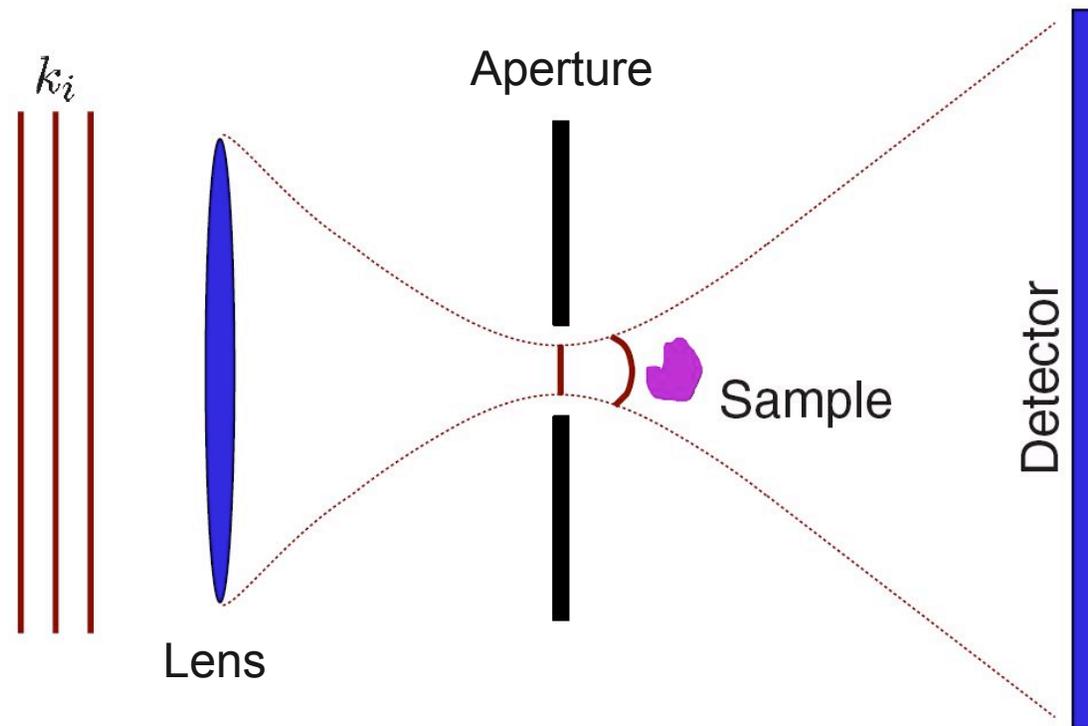
In contrast to weak segregation theory, Bi is locally concentrated in Bi-doped Si crystals



- (a) Image below Bi M5 edge (2550 eV)
- (b) Image above the Bi M5 edge (2595 eV)
- (c) Difference
- (d) SEM image

C. Song et al., *PRL* 100, 025504 (2008)

Curved object illumination aids unique phase recovery

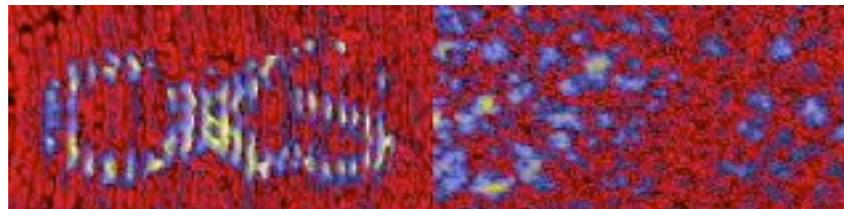


- Lens illuminates object with curved wavefront, defines field of view
- Object illumination is reconstructed by back-propagation, used to retrieve phase of object wave by iterative methods

K. Nugent et al., *PRL* 91, 203902 (2003)

... and converges faster

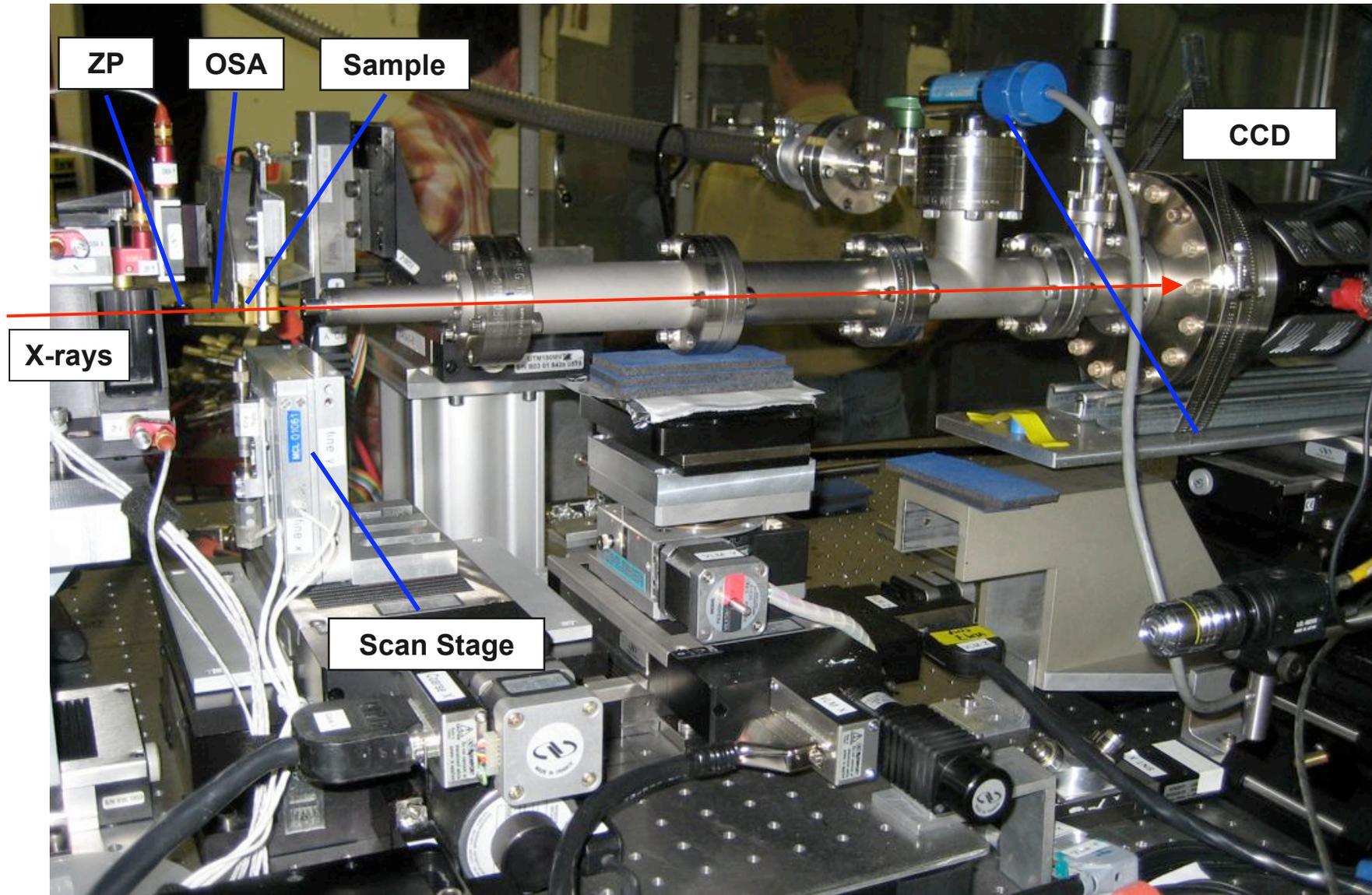
Original



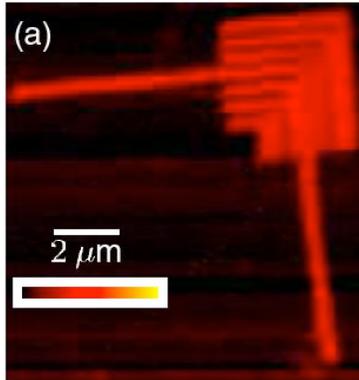
**curved beam
illumination**

**plane wave
illumination**

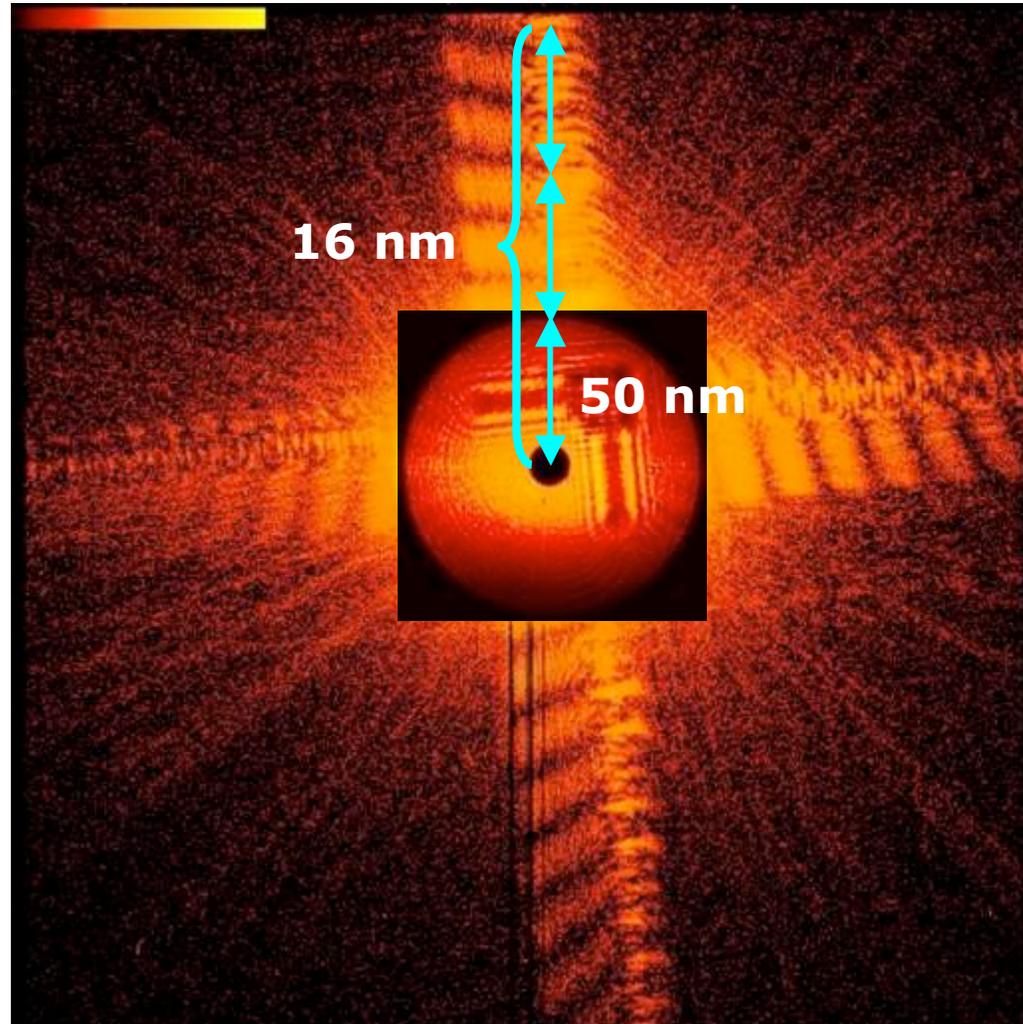
FCDI setup



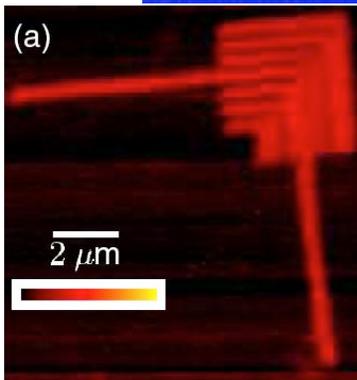
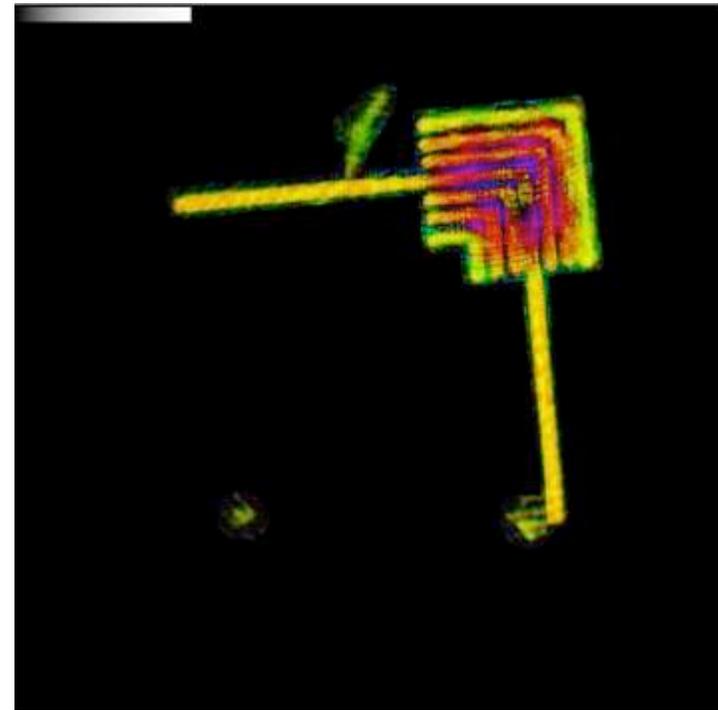
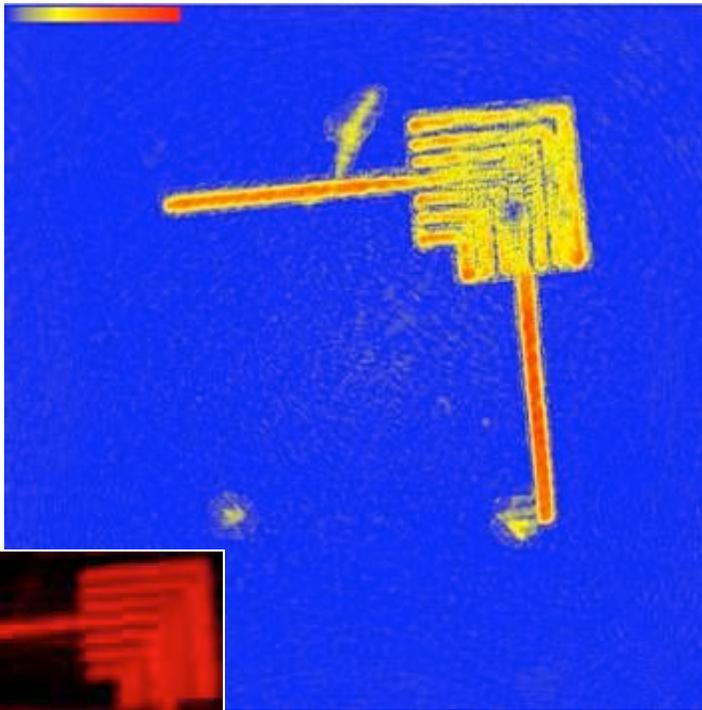
Fresnel coherent diffraction imaging of a gold test pattern



STXM image (1.8 keV)



Images reconstructed by FCDI



STXM image (1.8 keV)

Phase

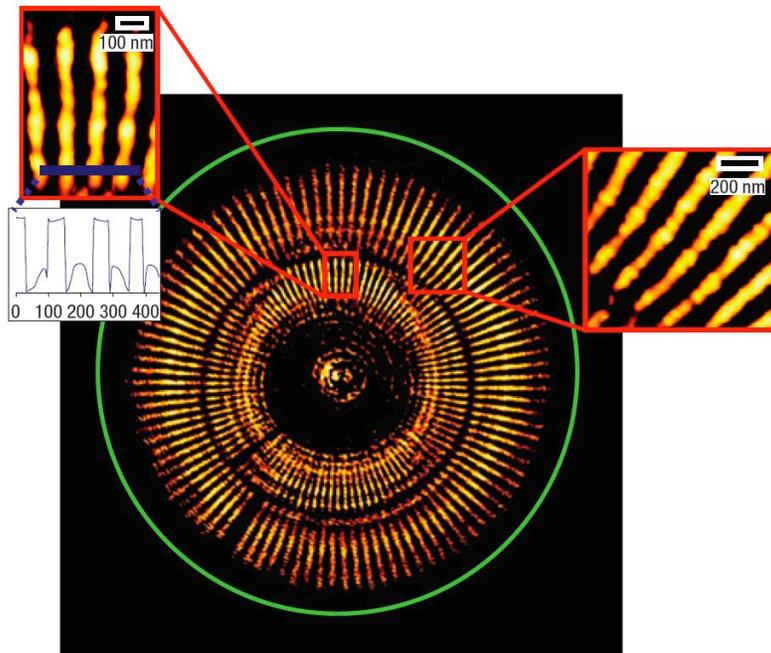
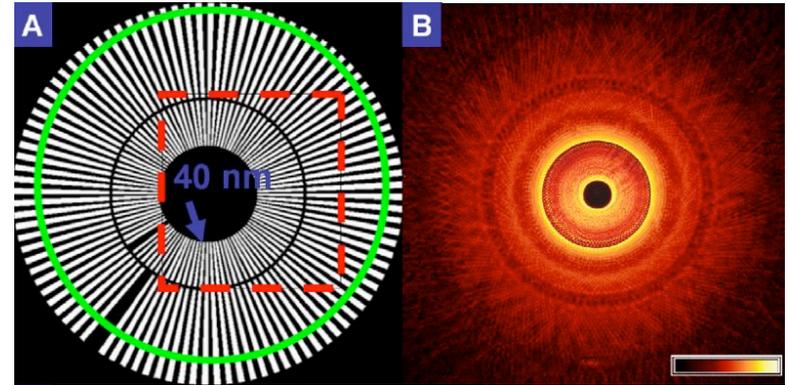
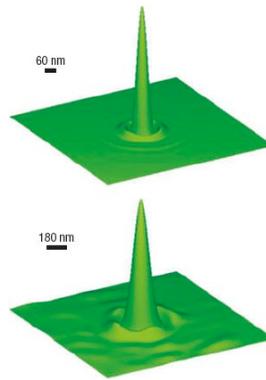
Magnitude with
color-encoded phase

G. Williams et al., *PRL* 97, 022506 (2006)

"Keyhole" FCDI

Use reconstructed illumination profile to determine support in extended sample

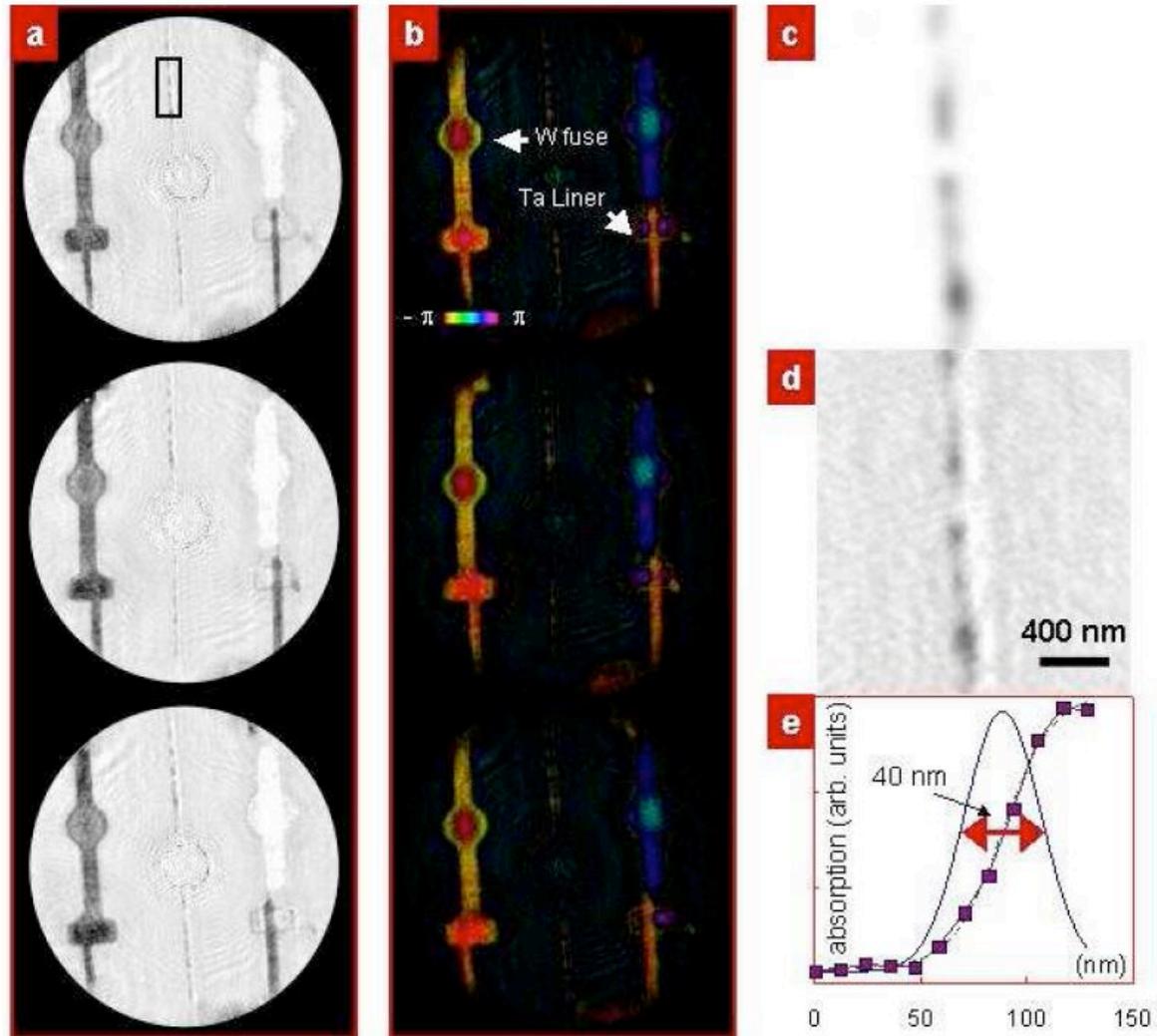
H. Quiney,
Nature Physics 2, 101 (2006)



Ability to study extended samples is essential for many real-world problems!

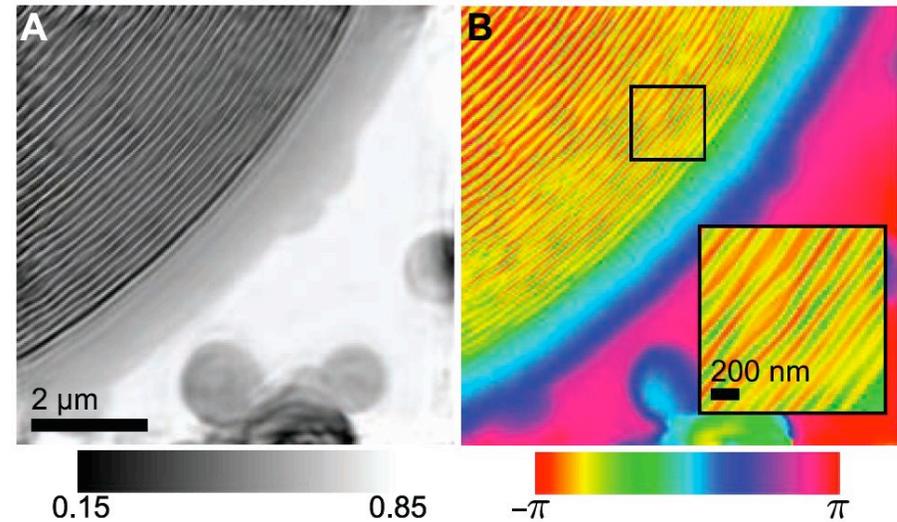
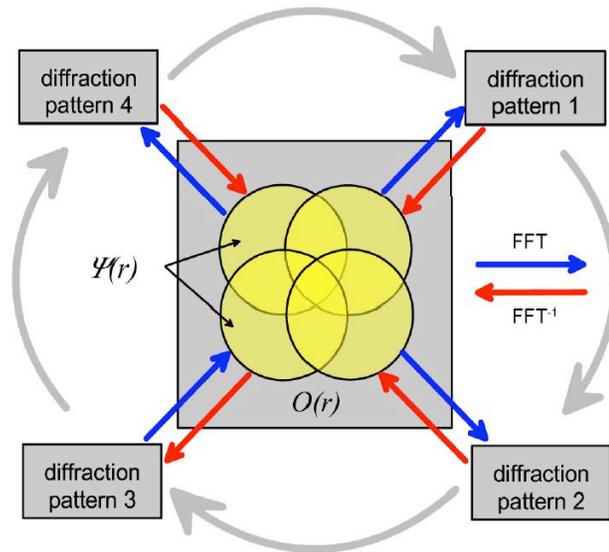
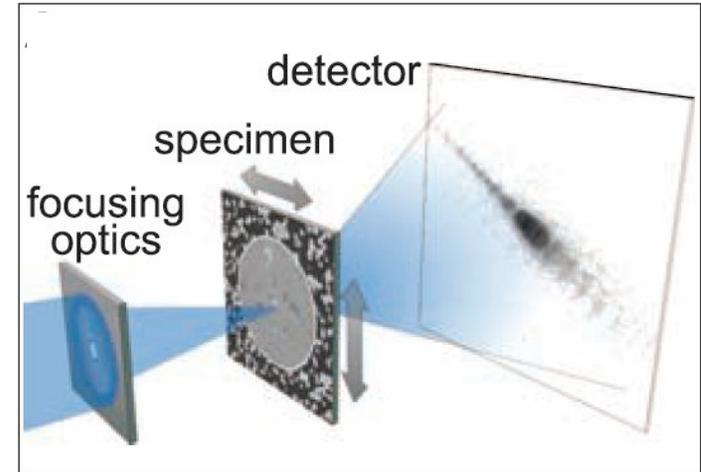
B. Abbey et al., *Nature Physics* 4, 394 (2008)

Recent results ("fuse bay" structure)

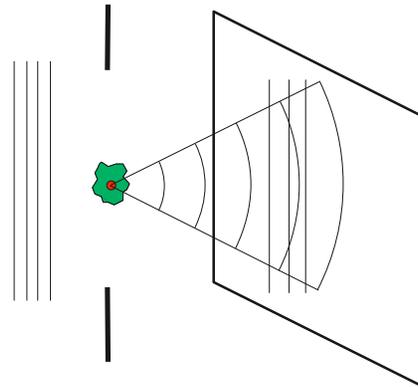


Alternative approach: ptychography

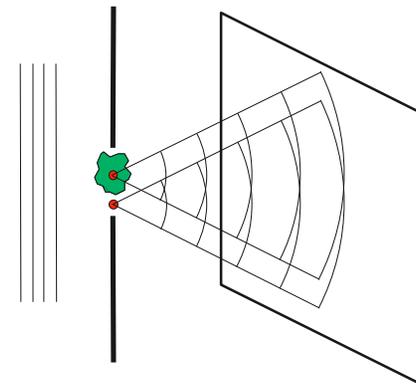
- R. Hegerl et al., Phys. Chemie 74, 1148 (1970)
- H. Faulkner and J. Rodenburg, PRL 93, 023903 (2004)
- J. Rodenburg et al., Phys. Rev. Lett. 98, 034801 (2007)
- P. Thibault et al., Science 321, 379 (2008)



Holography



Gabor



Fourier transform

Record hologram

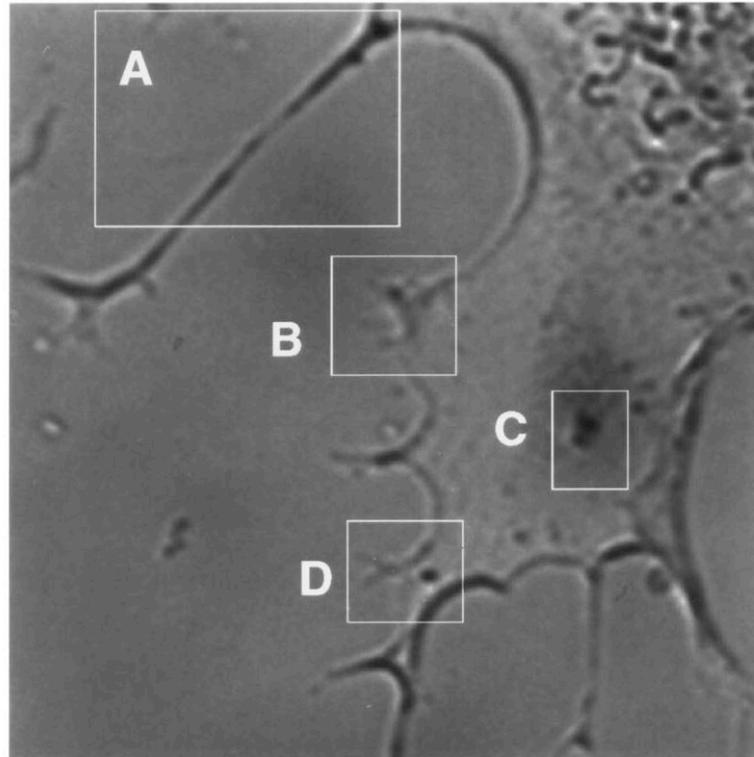
$$I = |a+b|^2 = |a|^2 + |b|^2 + a^*b + ab^*$$

Reconstruct

$$\begin{aligned} bI &= b|a|^2 + b|b|^2 + a^*bb + abb^* \\ &= aI_b + b(I_a + I_b) + \text{background} \end{aligned}$$

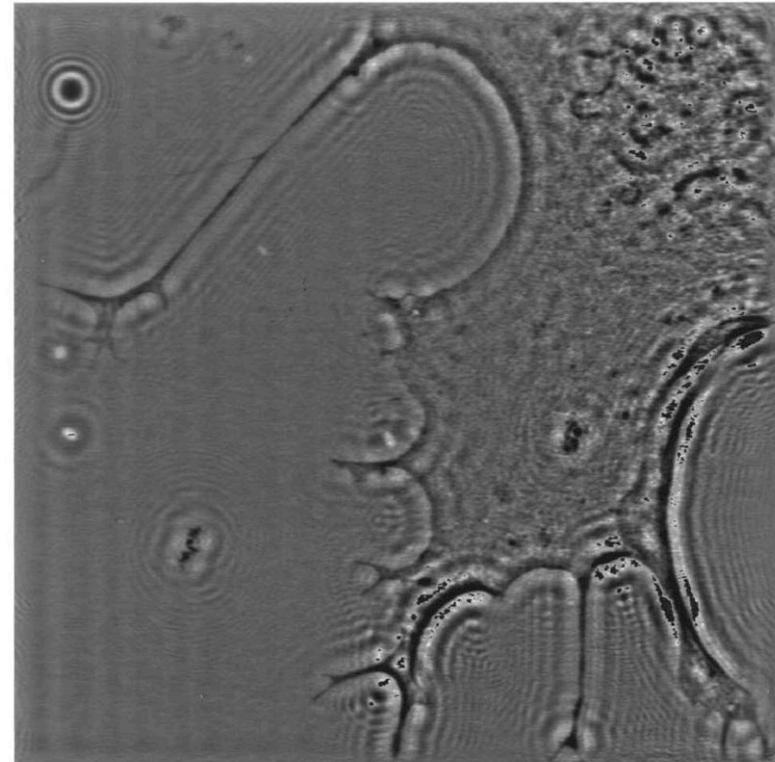
- Reference wave encodes magnitude and phase of object wave
- Reconstruct object wave by "re-illuminating" hologram with reference wave (or its C.C.)

Gabor holography



6.0 μm

Visible light



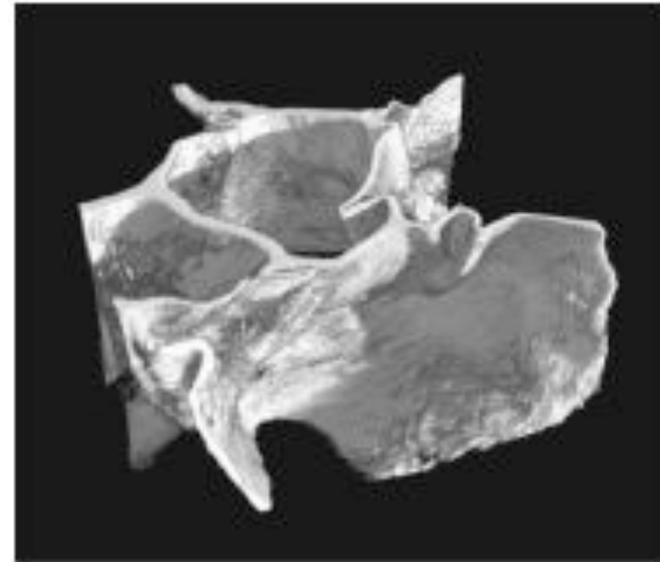
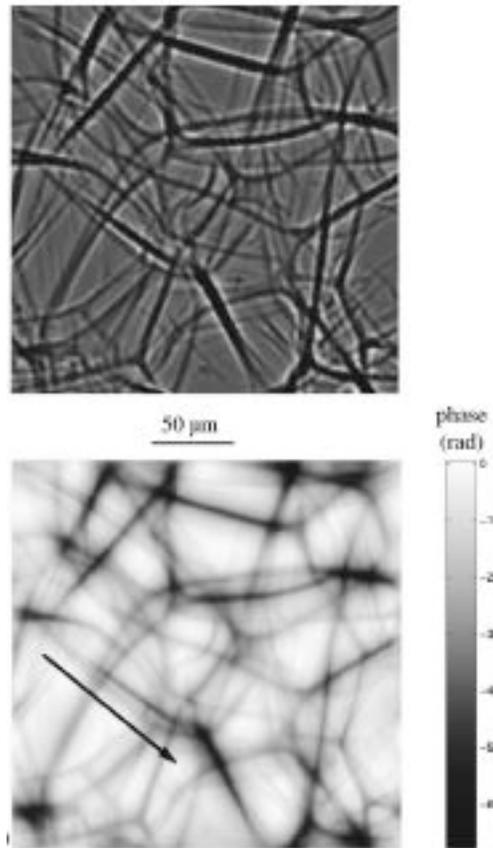
6.0 μm

X-ray

Reconstructed hologram (right) of a NIL8 hamster neural fibroblast recorded with 656 eV x-rays. Estimated dose was 7.5×10^5 Gy

S. Lindaas et al, *J. Opt. Soc. A.* 13, 1788 (1996)

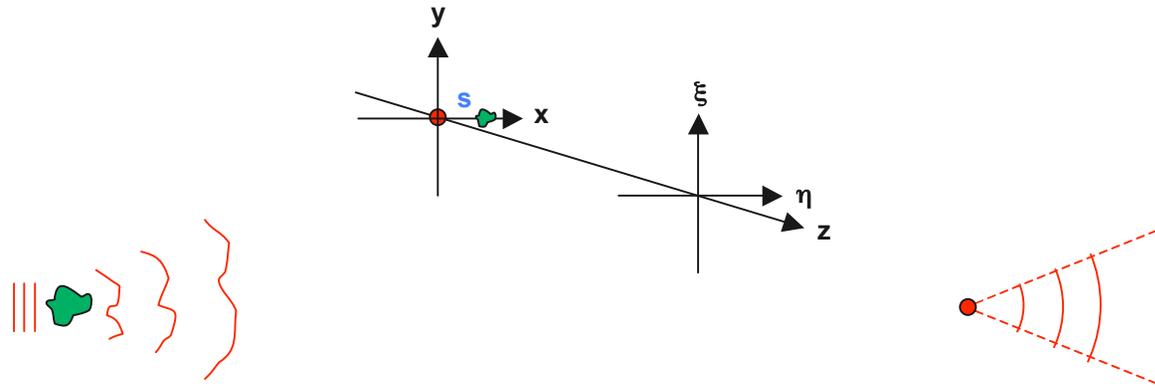
Hard x-ray holotomography



Phase-sensitive image quantitative phase map, and volume rendition of polystyrene foam (18 keV x-rays)

P. Cloetens et al., *Appl. Phys. Lett.* 75, 2912 (1999)

FT hologram formation



$$a(\xi, \eta) = \frac{e^{ikz}}{i\lambda z} \iint a(x-s, y) e^{\frac{ik}{2z}((x-\xi)^2 + (y-\eta)^2)} dx dy$$

object wave

$$b(\xi, \eta) = \frac{e^{ikz}}{i\lambda z} b_0 e^{\frac{ik}{2z}(\xi^2 + \eta^2)}$$

reference wave

$$I = |a+b|^2 = |a|^2 + |b|^2 + a^*b + ab^*$$

hologram intensity

Reconstruction

- Numerically take FT of hologram intensity to reconstruct
- Spatially separated primary, conjugate object waves result
- Weak curvature $f(x,y)$ on object wave can be ignored

Image terms: $a^*b + ab^* = \varphi(s\xi)F(\xi,\eta) + \varphi(s\xi)^*F(\xi,\eta)^*$

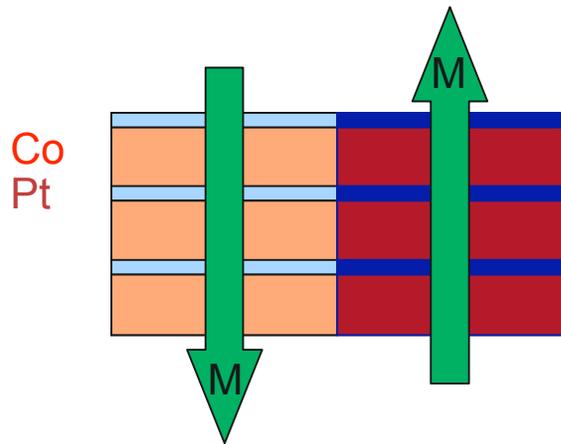
where: $F(\xi,\eta) = \frac{e^{ikz}}{i\lambda z} f(\xi,\eta) \iint a(x,y) f(x,y) e^{-\frac{ik}{z}(x\xi + y\eta)} dx dy$,

$\varphi(s,\xi) = e^{-\frac{ik}{z}s\xi}$ and $f(\xi,\eta) = e^{\frac{ik}{2z}(\xi^2 + \eta^2)}$

$$FT^{-1}\{a^*b + ab^*\} = f(x-s,y) a(x-s,y) + f(-(x-s),-y)^* a(-(x-s),-y)^*$$

CoPt magnetic labyrinth nanostructures

side view

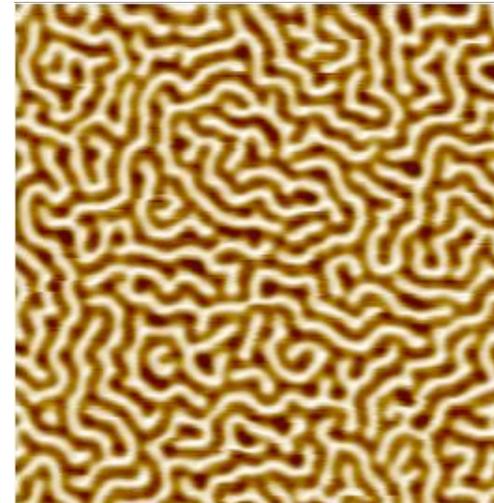


Sample: O. Hellwig (Hitachi)

SiN_x / Pt (24 nm) /
[Co (1.2 nm) / Pt (0.7 nm)]₅₀ /
Pt (1.5 nm)

perpendicular anisotropy → magnetic storage media

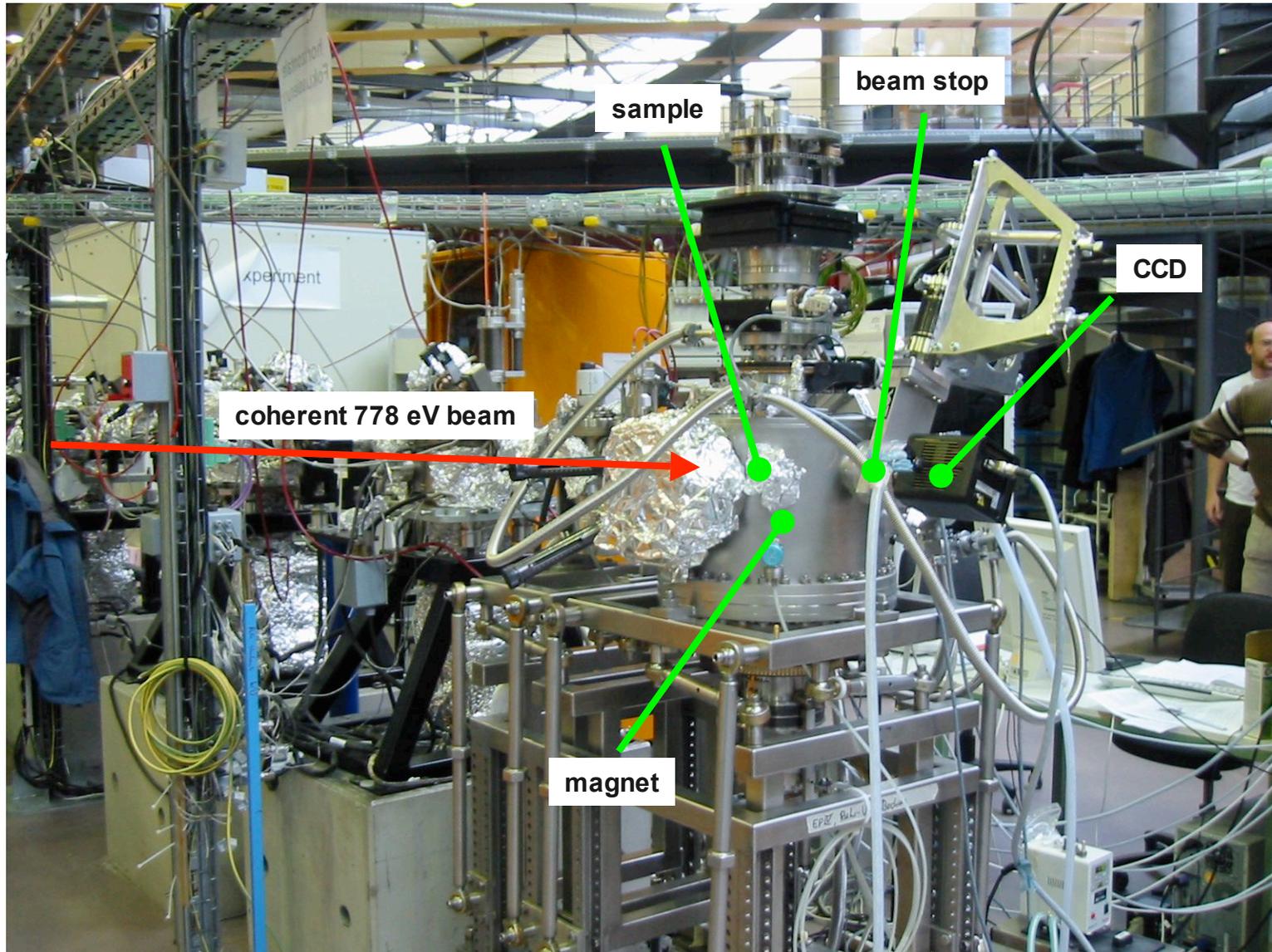
MFM, top view



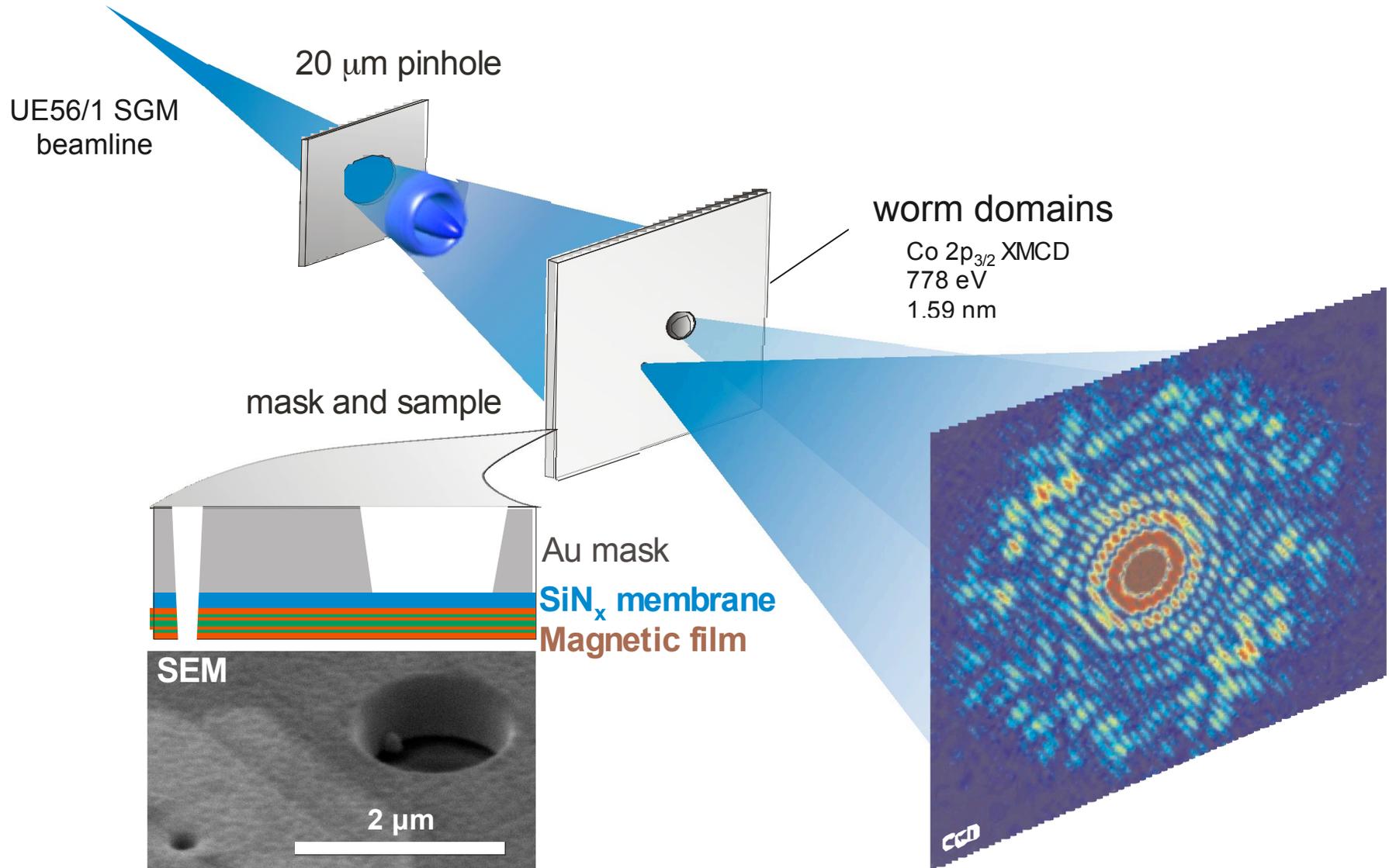
5 μm x 5 μm

continuous object

UE56-SGM beamline and ALICE

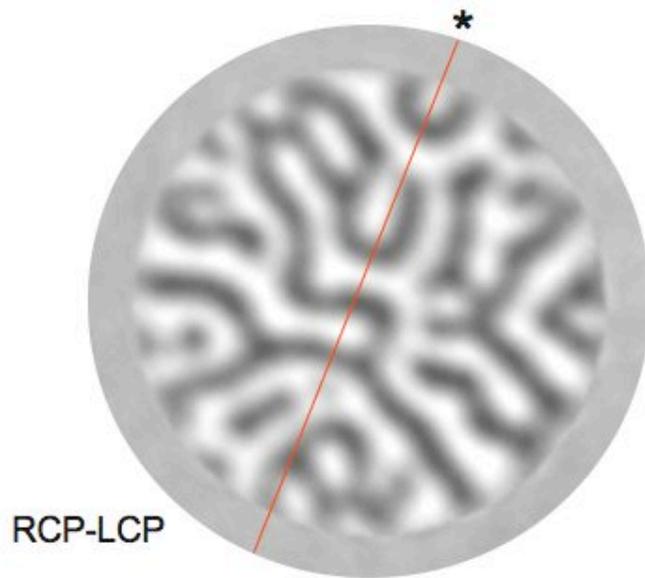


Pinhole mask method



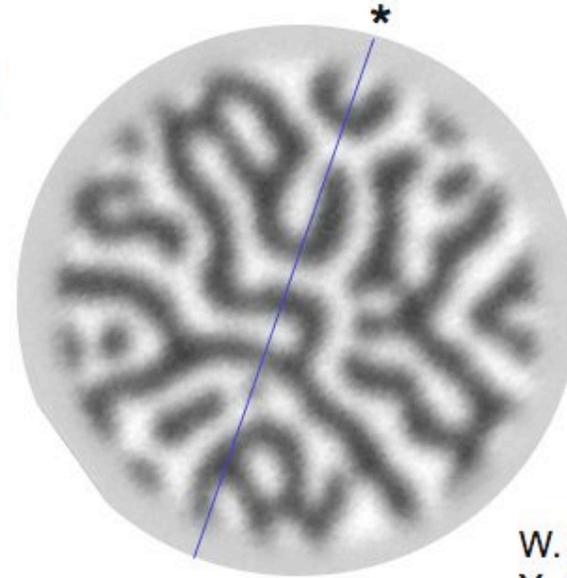
FTH

STXM



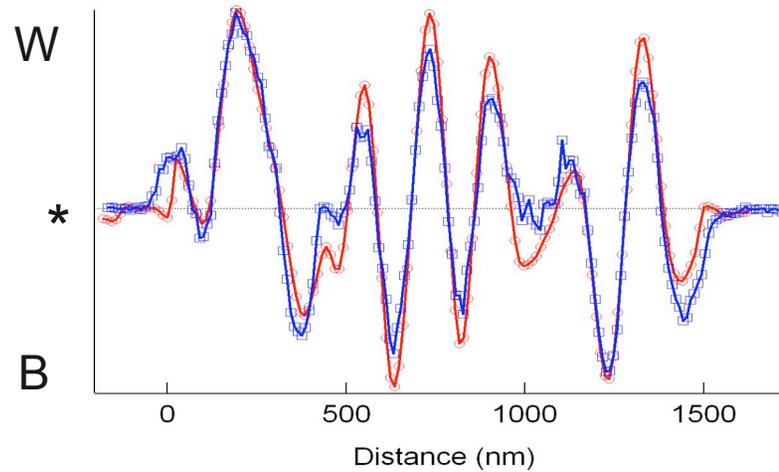
Ø 1.5 µm

100 nm



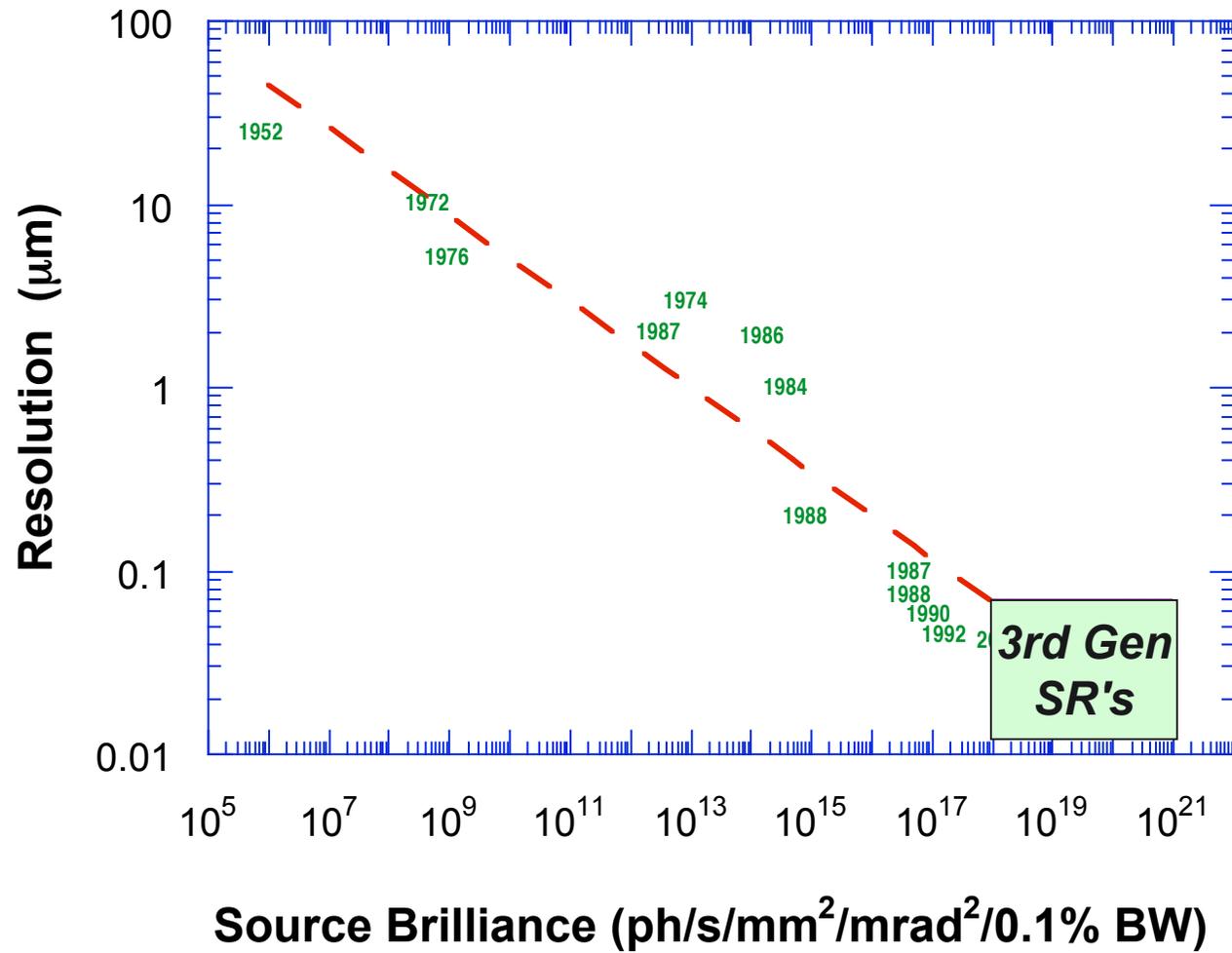
Reconstructed
resolution ~50 nm

Resolution
~35 nm



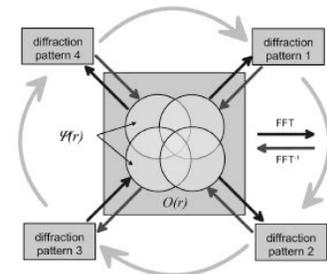
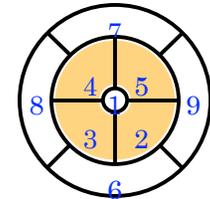
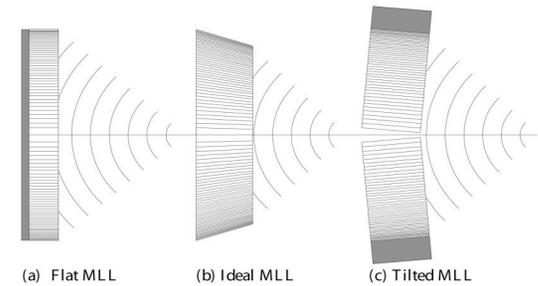
**S. Eisebitt, et al.,
Nature 432, 885 (2004)**

Imaging resolution by x-ray holography



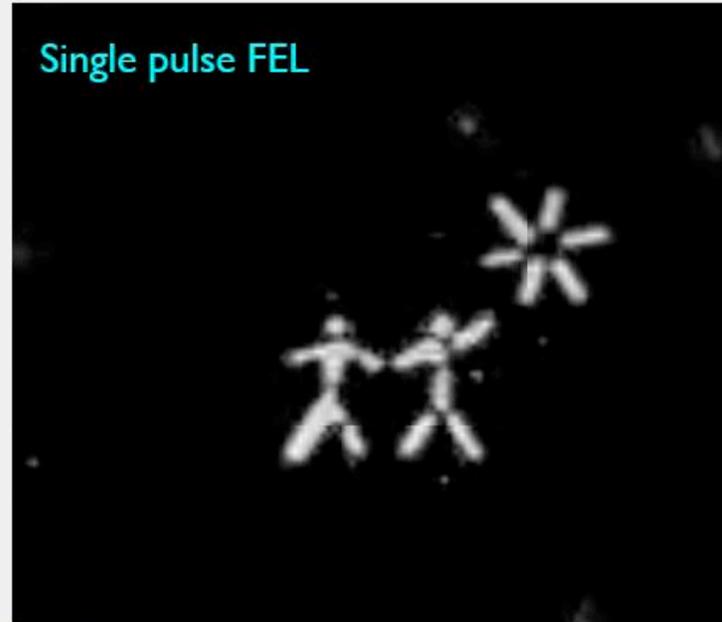
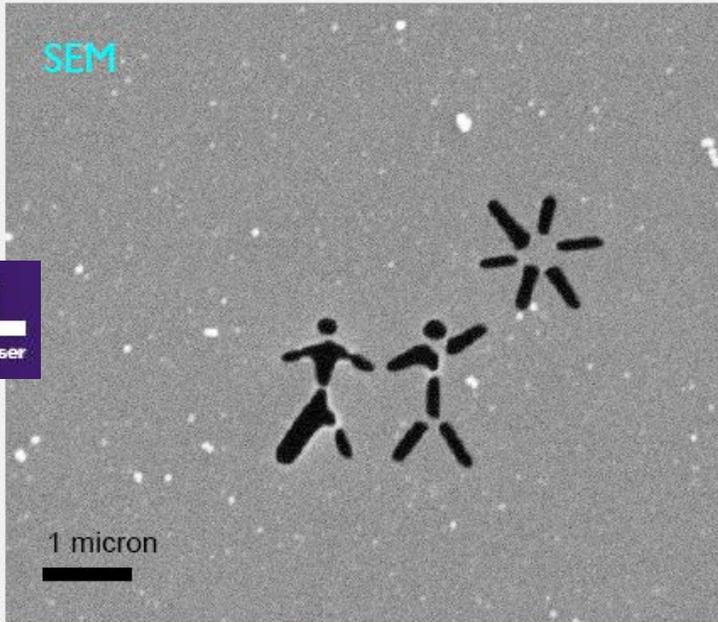
What's in store for the future?

- Resolution of x-ray optics is improving steadily
 - 30 nm is routine
 - < 5 nm looks possible using MLLs
- Commercial x-ray microscopes are proliferating
 - Precision full-field and scanning instruments
 - Multiple contrast mechanisms available
 - Cryo-preparation will become standard (as for TEM)
- Hybrid scanning (ptychography) and single-view (keyhole) coherent diffraction methods broaden range of applications
- Diffraction and holographic methods are attractive for x-ray lasers such as XFEL and LCLS !
 - Bypass radiation damage with a single few-fs flash
 - Use pump-probe methods to study ultrafast dynamics
 - No lens to limit resolution or get between sample, detector

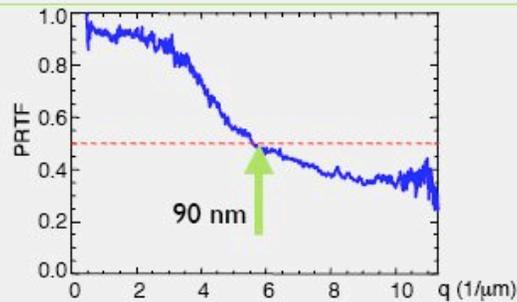


Ultrafast coherent diffraction with a free-electron laser

The reconstruction is carried out to the diffraction limit of the 0.26 NA detector



Phase-retrieval transfer function gives an estimate of the resolution of the reconstructed image

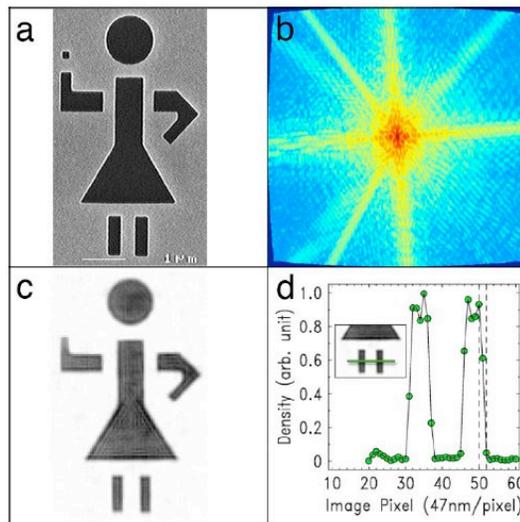
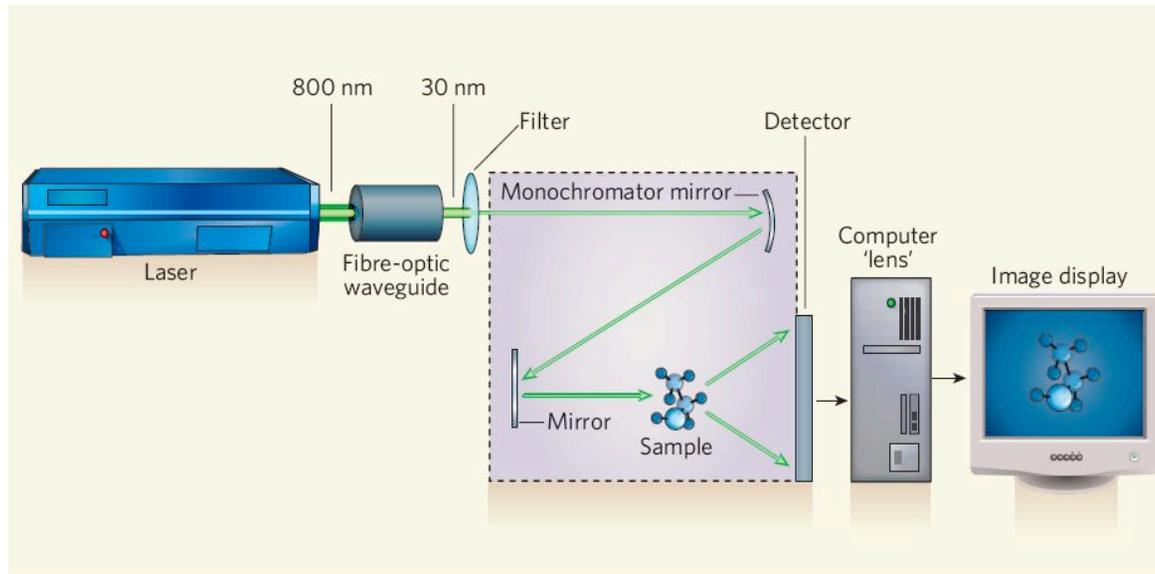


← → 32 nm, one wavelength

← → λ / NA

H. Chapman et al., *Nature Physics* 2, 839 (2006)

Now it can be done on a tabletop!



R. Sandberg et al., PRL 99, 098103 (2007)

J. Spence, Nature 449, 543 (2007)

R. Sandberg et al., PNAS 105, 24 (2008)

Summary

- **Resolution, contrast, sources, and optics for x-ray imaging**
- **Direct methods: projection, full-field, and scanning**
- **Indirect methods: microdiffraction, coherent diffraction, holography**

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