Powder X-ray Diffraction

Brendan J. Kennedy School of Chemistry The University of Sydney

Uses of Powder Diffraction

Qualitative Analysis Identification of single-phase materials Identification of multiple phases in microcrystalline mixtures Recognition of amorphous materials in partially crystalline mixtures

Quantitative Analysis Lattice Parameter Determination Phase Fraction Analysis

Peak Shape Analysis Crystallite Size Distribution Microstrain Analysis Extended Defect Concentration Structure Refinement Rietveld Method

Structure Solution Reciprocal Space Methods Real Space Methods

Thermal expansion and Phase Transitions

Three Unique Features of Synchrotron Radiation

•Intensity •Enables Rapid Data Collection Kinetics Unstable Compounds Environmental Cells -Enables Focussing Small Samples Small areas/volumes •Energy Range •Enables Spectroscopy –Elemental Identification –Bonding Studies

- -Speciation •Enables Optimal Conditions
- -Environmental Cells -Selected Elements

s •Low Divergence

Enables High Resolution
 Micro Beams
 Small Volumes

•Complex Materials

What is special about a crystal? Solid phases are often crystalline, but need not be e.g. glass an "amorphous material"

Glass

- Fractures into shards
- Takes on any shape, depending on preparation
- Properties do not vary with orientation.

Cleaves along preferred directions Grows with well developed crystal faces Properties depend on orientation in which they are measured.

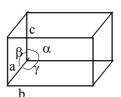
Crystal

•Si Oxygen

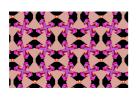
Crystal Structure

- CRYSTAL: Contains a periodical array of atoms/ions. This can be represented by a simple lattice of points.
- A group of atoms is associated with each lattice points.
- LATTICE: An infinite array of points in space, in which each point has identical surroundings to all others.
- CRYSTAL STRUCTURE: The periodic arrangement of atoms in the crystal.

The Unit Cell



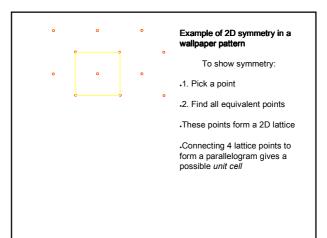
The unit cell is a basic parallelopiped shaped block from which the whole volume of the crystal may be built by repetition in 3 dimensions. Any point in the unit cell may be specified with respect to the origin by parameters x, y, z measured parallel to the unit cell axes and expressed as fractions.



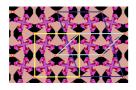
Example of 2D symmetry in a wallpaper pattern

To show symmetry: 1. Pick a point

2. Find all equivalent points



(http://www.clarku.edu/~djoyce/wallpaper/)



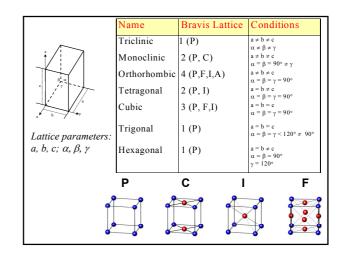
Example of 2D symmetry in a wallpaper pattern

• Connecting 4 lattice points to form a parallelogram gives a possible *unit cell*

• *Unit cell* – the basic unit that repeats in every direction

• Different *unit cells* can be chosen

•But some *unit cells* are preferable for higher symmetry



PCC Lattice



 α -Po is primitive-Centered Cubic Identical atoms at corners but nothing at the and body or face centers. Lattice type P **BCC Lattice**



 α-Iron is Body-Centered Cubic

 Identical atoms at corners and body center (nothing at face centers)

 Lattice type I

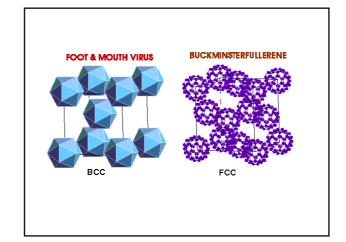
 Also Nb, Ta, Ba, Mo...



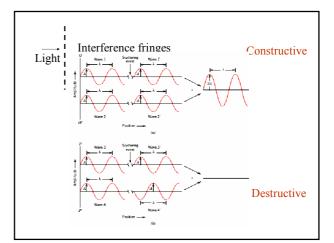


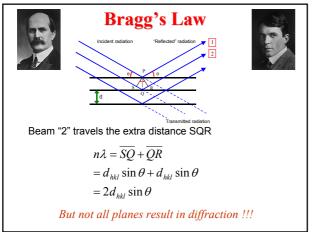
Sodium Chloride (NaCl) Na is much smaller than Cl Face Centered Cubic

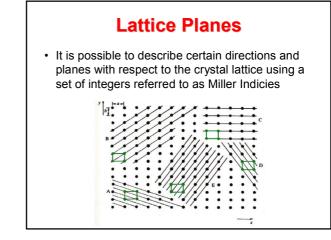
<u>Rocksalt structure</u> Lattice type F Also NaF, KBr, MgO....

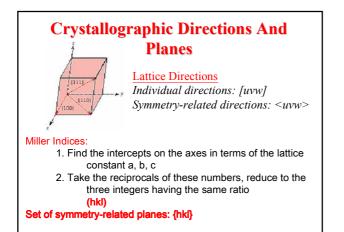


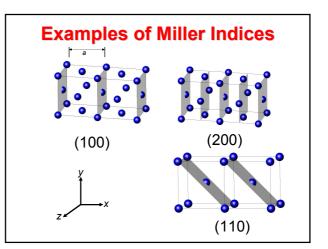


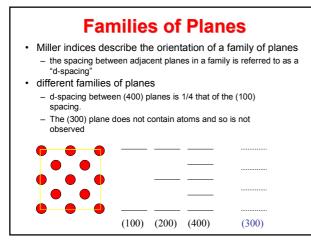


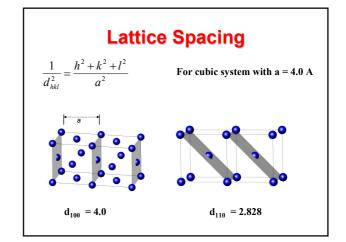


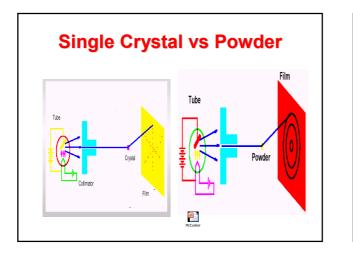


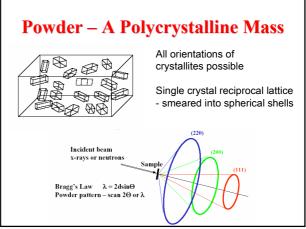


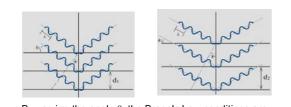




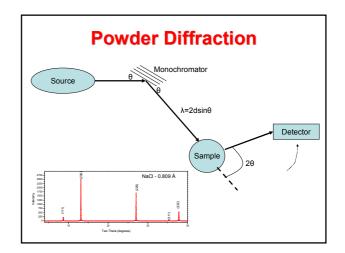


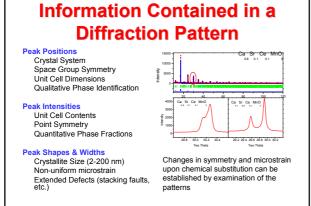


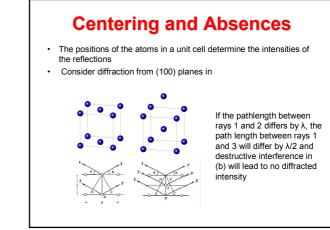




- By varying the angle θ, the Bragg's Law conditions are satisfied by different d-spacings in polycrystalline materials.
- Plotting the angular positions and intensities of the resultant diffracted peaks produces a pattern which is characteristic of the sample.



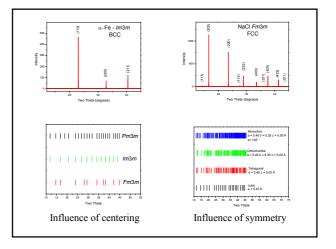




Centering and Absences

 We can extend these types of calculation to include other modes of lattice centering. They all lead to systematic absences

Bravais lattice	Reflections that must be absent
Simple (Primitive)	none
Base (C) centered	h and k mixed
Body (I) centered	(h+k+l) odd
Face (F) centered	h, k and I mixed



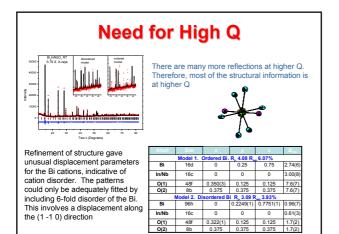
Multiplicity

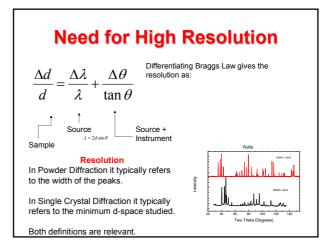
- For high symmetry materials the Bragg angles and d-spacings for different reflections may be equivalent to one another For example (100), (010), (001) etc are equivalent in a cubic material
- In a powder, all planes with the same d-spacing contribute to the scattered intensity at a given Bragg angle
- The number of planes that are symmetry equivalent is referred to as the multiplicity and its appears as a multiplicative term in powder diffraction intensity calculations
- The multiplicity of a reflection depends upon the symmetry of the crystal

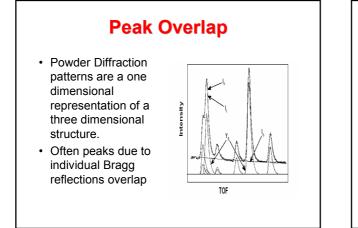
Multiplicity of {100} for cubic is 6, but for tetragonal it would only be 4 as (100) and (001) are not equivalent

Diffraction Patterns

- Spacing of peaks depends on size of unit cell and the space group.
- The bigger the unit cell and/or the lower the symmetry the more diffraction peaks are observed.
- Intensity of peaks depends on (amongst other things) the arrangement of the atoms in the unit cell.
- For two materials that had identical unit cells, the peak positions would be IDENTICAL, however their intensities would be DIFFERENT.



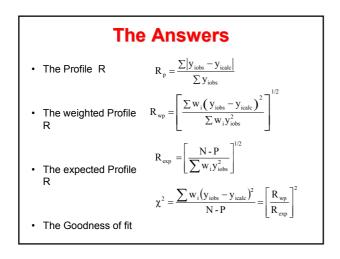


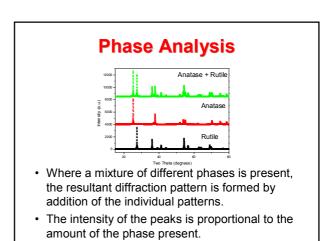


The Solution - Rietveld

$$\boldsymbol{y}_{icalc} = \boldsymbol{y}_{iback} + \sum_{p} \sum_{k=k_1^p}^{k_2^p} \boldsymbol{G}_{ik}^p \boldsymbol{I}_{i}^p$$

- y_{ic} the net intensity calculated at point i in the pattern,
- y_{iback} is the background intensity,
- G_{ik} is a normalised peak profile function,
- I_k is the intensity of the kth Bragg reflection,
- $k_1 \dots k_2$ are the reflections contributing intensity to point i,
- the superscript p corresponds to the possible phases present in the sample.





Quantitative Phase Analysis

Bragg scattering is proportional to N/V where N is the • number of unit cells and V the unit cell volume. There for the weight of a phase in the beam is:

$$W_P = \frac{(SZMV)_P}{\sum (SMPV)_P}$$

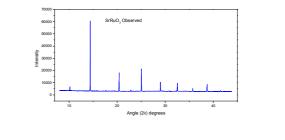
S - the scale factor

Z the number of formula unites per unit cell M the molecular weight of the formula unit I is the index running over all phases

Hence SZVM is proportional to the weight of the • diffracting sample

An Example

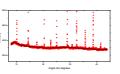
· Synchrotron X-ray Diffraction pattern for SrRuO₃



The background

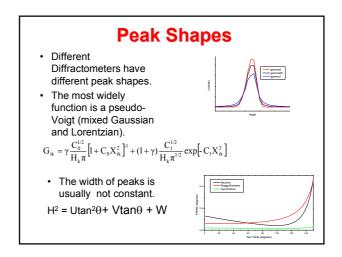
- · Fluorescent radiation from the sample
- · Diffraction from the continuous spectrum
- Diffuse scattering • - Incoherent
 - Temperature diffuse
 - Other materials - Specium holder
 - air etc

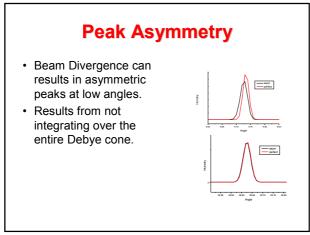
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- · Background can be either fitted or estimated.
- · Here the capillary is a feature.







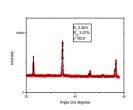
<section-header> The Simple Structural Model The fit to a single phase sample looks god BUT..... The detail of the fit is not satisfactory the model is missing something!

A Common Problem

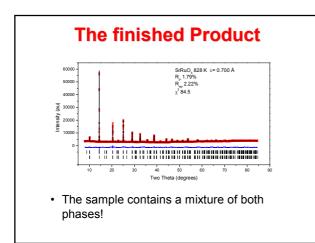
- If the structural model is wrong then the most common response of Rietveld programs is to:
 – broaden the peaks,
 - Increase the displacement parameters,
- The former is most noticeable at high angles where intensity is lowest.
- Due to absorption of the X-rays powder X-ray diffraction often yields poor displacement parameters

An Alternate Model

• The high angle splitting is well modeled by a tetragonal model - but this overestimates some intensities.



· The Truth lies somewhere in the middle



Strengths and Limitations of Powder X-ray Diffraction

Strengths

Non-destructive – small amount of sample

Relatively rapid

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Limitations

- Bulk technique generally unless a microfocus source is used
- Not a "stand-alone" technique often need chemical data
- .
- Relatively rapid Identification of compounds / phases not just elements Quantification of concentration of phases (sometimes) Classically for powders, but solids possible too Gives information regarding crystallinity, strain, crystallite size, and orientation
- Complicated appearance multiphase materials – identification

can be difficult

Experiment Design Issues

What Wavelength?

- · Absorption is your enemy!
- · Short Wavelengths are best! BUT
- · Consider required resolution. And
- · Avoid Absorption Edges.

What Size Capillary?

- Small capillaries reduce absorption AND • improve resolution.
- · BUT reduce amount of material.